

MATLAB NOTES DIGITAL SIGNAL PROCESSING



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Digital Signal Processing MATLAB Notes, First Edition

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MATLAB BASICS

Digital Signal Processing

DSP

* MATLAB :- Matrix Laboratory

* mainly used for analysing in \hookrightarrow domain

$\frac{O/P}{I/P}$ } efficiency $\eta \equiv$ Mech. power.
Gain \equiv electrical qty.
 $\frac{O/P}{I/P}$ } TF \equiv model of any control sys. represented in freq. domain.
V, I, P

for a TF.

freq. at which op of sys is zero. \therefore Zero's
is map \therefore Poles

Root Locus :- locⁿ of roots

* Gain margin & Phase margin :- How much to inc. gain & how much to change phase so that sys. is stabilized.

Time domain

freq. domain

Integration \equiv

Division \times Multiplicⁿ

Differentiation \equiv

Division

* NYQUIST Criterion :- Telling about stability

DSP LAB

Q Consider a TF :- $\frac{s^2 + 2s + 1}{s^3 + s^2 + 3s + 4}$ = $\frac{\text{NUM}}{\text{DEN}}$

* each line terminⁿ with ;
(If no ; the value typed will be shown again)

* CMD : WHO : to see all which all parameters of workspace
Cmd : CLC : Clear screen.

Writing a parameter :- α
syntax

$$\alpha = [1 \quad 2 \quad 3]$$

$$\left(\equiv \alpha = s^2 + 2s + 3 \right)$$

★ Root Locus :-

Cmd :- α locus (num, den)

Cmd :- help <fn name>

gives all cmds related to that fn cmd.

Cmd :- To see value of ~~no~~ roots :-

Zeros :- Zeros = roots (num)
poles = roots (den)

Cmd :- Put labels on x and y axis.

xlabel ('This is x axis label')
ylabel ('frequency')

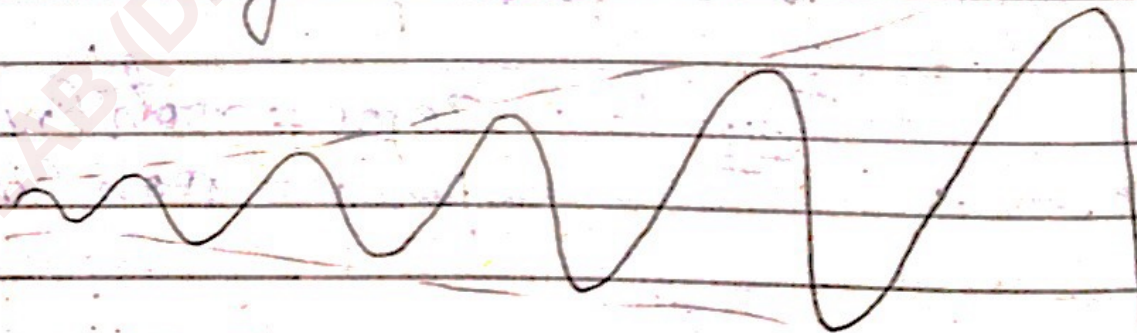
Cmd :- To give title :-

title('This is my first plot')

* ~~of~~ Cmd :- for step response

step(num, den)

* Consider a fn :-



Analysis :- fn is exponentially \uparrow or \downarrow :- e^{at} / e^{-at}
fn is oscillating :- $\sin \omega t$ / $\cos \omega t$

★ Whenever graph is plotted simultaneously,
use HOLD cmd, Undo hold :- HOLD OFF

★ To have 2 graphs in same screen

cmd :- subplot (~~2, 2, 1~~) (2, 1, 1)

↓
make 2 graphs & refer to

1st one out of 2

subplot (2), (2), (1)

Total
no. of
graphs

column
I want
to refer.

which row
I want
to refer

DSP Lab

* Finding poles & zeros of a TF

$$\text{Say, TF} = \frac{as^2 + bs + c}{ds^3 + es^2 + fs + g}$$

So, let ~~a~~ inputs be

$$A = [a \quad b \quad c]$$

$$B = [d \quad e \quad f \quad g]$$

So, to get a graph of poles & zeros,

Cmd :- `pzmap(A, B)`

To know the values of poles & zeros \rightarrow
let

$$C = \text{roots}(A) \leftarrow ; \text{ for zeros}$$

$$D = \text{roots}(B) \leftarrow ; \text{ for poles}$$

Inference :- If poles lie on the real axis,
then, response is not oscillatory

(either monotonically ↓ or ↑)
Pole lying on left half of s-plane

⇒ sth like $\frac{1}{s+a} \Rightarrow s = -a$ is a pole on left half

⇒ in freq $\rightarrow e^{-at} \rightarrow$ monotonically decreasing

⇒ it goes to zero i.e. finishes
⇒ stable sys

⇒ Poles on left half of s-plane : Stable
right half " : Unstable

★ Step response analysis

Consider a TF :- $G(s) = \frac{s^2 + 2s + 1}{2s^3 + 4s^2 + 3s + 5}$



Find steady state response from TF given a step IP.

↳ & finding initial & final value of a TF

As per graph, we get steady state at 0.2

$$\lim_{s \rightarrow 0} G(s) = \frac{1}{5} = 0.2$$

eg (2) TF = $\frac{s^2 + 2s + 2}{2s^3 + 4s^2 + 4s + 5}$

$$\lim_{s \rightarrow 0} (TF) = \lim_{s \rightarrow 0} \left(\frac{2}{5} \right) = 0.4$$

Finding ω

from the step response graph

Take 2 peaks, P_1 & P_2

See their time (sec), T_1 & T_2

Time diff = $T_2 - T_1$. freq = $\frac{1}{T_2 - T_1}$

$$f_{\text{rad}} = \omega = 2\pi \left(\frac{1}{T_2 - T_1} \right)$$

(To see from matlab, check the poles which are having a component in imaginary axis. That is ω)

* freq. of sp of a natural control sys. gives natural freq.

for eq (2),

$$\text{poles} = -1.6914, -0.1543 \pm 1.2059i$$

$$\text{zeros} = -1 + i, -1 - i$$

Finding oscillⁿ freq. from graph =

$$T_1 = 1.98 \text{ s}$$

$$T_2 = 7.19 \text{ s}$$

$$T_2 - T_1 = 5.21 \text{ s}$$

$$\Rightarrow f = \frac{1}{T_2 - T_1} = \frac{1}{5.21} = 0.1919 \text{ Hz}$$

$$\text{So, } \omega = 2\pi f = 2 \times 3.14 \times 0.1919$$

$$\omega = 1.2053 \text{ rad/s}$$

same as the complex part of poles.

* 2 plots on same graph :

step responses

① step (a, b) ←

held ←

② step (c, d) ←

Note 3:- Freq. response depends on pole freq.

Even if we change zeros to be complex, \exists no change in freq. of response. Only amp. changes.

* Pole freq: called as natural freq. of sys.

* Given a TF, find ^{magnitude} freq. response.

S1) Find magnitude from TF.

S2) Convert it to dB.

S3) Plot of magnitude vs ω .

~~Freq. response~~

Magnitude response: The magnitude of the o/p corresponding to diff^t values of freq. (ω).

Basically, for any TF, take diff^t values of ω & substitute in TF.

The o/p gives diff^t magnitudes.

Then, convert them to dB.

eg. let TF = $G(s) = \frac{s^2 + 2s + 1}{s^3 + 2s^2 + s + 1}$

Method 1:- DISCRETE Method.

$$a2 = [1 \ 2 \ 1];$$

$$b2 = [1 \ 2 \ 1 \ 1];$$

Step (a2, b2) ←

Take different points on graph for diff^t times T_1, T_2, T_3, T_4, T_5 & say

(S1)

let $T_1 = 2.92 \text{ s} \Rightarrow 0.342 \text{ Hz} \Rightarrow 2.15 \text{ rad/s } \omega_1$

$T_2 = 7.02 \text{ s} \Rightarrow 0.142 \text{ Hz} \Rightarrow 0.89 \text{ rad/s } \omega_2$

$T_3 = 11.5 \text{ s} \Rightarrow 0.086 \text{ Hz} \Rightarrow 0.546 \text{ rad/s } \omega_3$

$T_4 = 15.6 \text{ s} \Rightarrow 0.064 \text{ Hz} \Rightarrow 0.402 \text{ rad/s } \omega_4$

$T_5 = 19.9 \text{ s} \Rightarrow 0.050 \text{ Hz} \Rightarrow 0.3155 \text{ rad/s } \omega_5$

Taken from step response for step (a2, b2)

Now, finding diff magnitudes by substituting ω in TF

(S2)

$G(s) \Big|_{\omega_1} = 0.444 \quad \Delta_1 = 7.0523 \text{ dB}$

$\Big|_{\omega_2} = 0.854 \quad \Delta_2 = 1.370$

$\Big|_{\omega_3} = 1.0369 \quad \Delta_3 = 0.3147$

$\Big|_{\omega_4} = 1.098 \quad \Delta_4 = 0.8120$

$\Big|_{\omega_5} = 1.1194 \quad \Delta_5 = 0.9797$

Convert X to dB
 $\therefore -20 \log(X)$

S3 Plot D vs ω

So, Matlab:-

$$D = [7.0523 \quad 1.370 \quad -0.3147 \quad -0.812 \quad -0.9797]$$

$$W = [2.15 \quad 0.89 \quad 0.546 \quad 0.402 \quad 0.315]$$

Plot (D, W) ↙

Method 2: MATLAB

Take num & den. matrices again from given TF

$$a2 = [1 \quad 2 \quad 1];$$

$$b2 = [1 \quad 2 \quad 1 \quad 1];$$

Convert to magnitudes & frequencies

$$[h, W] = \text{freqs}(a2, b2)$$

Magnitude ↘ freq (W)

Convert Magnitude to dB

$$H = 20 * \log(\text{abs}(h))$$

Plot (H, W) ↙

absolute.

→ Doing convolution.

Cmd :- $\text{conv}(a, b) \leftarrow$

TF :- $[\text{num den}] = \text{sos2tf}(a, b);$

used for many TFs

$a = [\dots]$; $b = [\dots]$
COMBINING 2 TFs

Consider 2 TFs

$$\frac{a}{b} \quad \& \quad \frac{c}{d}$$

Now, find $\frac{ac}{bd}$

how?

$$\begin{array}{l} A = [a; c] \\ B = [b; d] \end{array} \left. \begin{array}{l} \text{appending} \\ \text{denom} \end{array} \right\}$$

Now, overall TF :-

$$[\text{num den}] = \text{sos2tf}([A; B])$$

makes TF to poly. form

So, now, we have combined TF in polynomial form.

PTD

eg. Consider 2 TFs $\frac{a}{b}$ and $\frac{c}{d}$ in parallel \Rightarrow $\frac{a}{b} + \frac{c}{d}$

$$TF_1 = \frac{a}{b} = \frac{s^2 + 2s + 1}{s^2 + 3s + 2} \quad \text{and} \quad TF_2 = \frac{c}{d} = \frac{2s^2 + s + 3}{s^2 + 3s + 1}$$

$$A = [a, c]; \quad B = [b, d];$$

So, we get $T = \frac{A}{B}$

$$A = [s^2 + 2s + 1] [2s^2 + s + 3]$$

$$B = [s^2 + 3s + 2] [s^2 + 3s + 1]$$

Now, converting to polynomial form
Using cmd:-

$$[\text{num} \quad \text{den}] = \text{sos2tf}(A, B)$$

we get

$$\text{num} = (s^2 + 2s + 1)(2s^2 + s + 3)$$

$$\text{den} = (s^2 + 3s + 2)(s^2 + 3s + 1)$$

$$\Rightarrow \frac{\text{num}}{\text{den}} = \frac{2s^4 + 5s^3 + 7s^2 + 7s + 3}{s^4 + 6s^3 + 12s^2 + 9s + 2}$$

MATLAB Assignment 1

Digital Signal Processing

23/9/13

DSP Lab

2 ml dsplab

@gmail.com

Assignment - 1

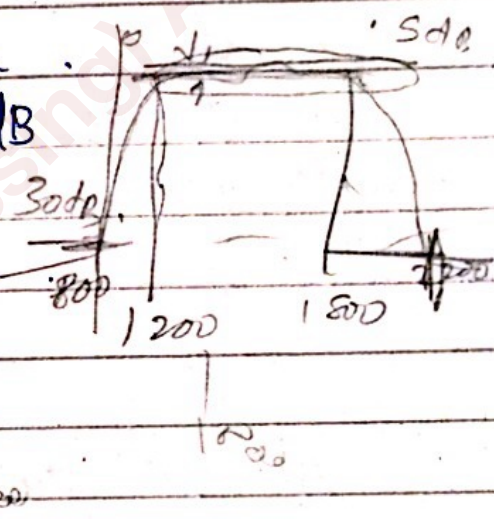
Q.1) Design an ~~low pass~~ analog filter to meet the specific^{ns} below:

Passband : 1200 - 1800 Hz

Stopband attenuation > 30 dB

Passband ripple < 0.5 dB

Transition width : 400 Hz



- (a) Butterworth filter
- (b) Chebyshev's filter
- (c) Elliptical filter

Plot the freq. response of the filters and compare their performance.

(a) for Butterworth
Idea : find order

help butter \leftarrow

$$[B, A] = \text{BUTTER}(N, W_n)$$

numerator denominator

Part (a)

def > ord. 2 of butterworth for s-domain

help buttdord

for s-domain

* INSTRUCTION ①

$[N, \omega_n] = \text{BUTTDORD}(\omega_p, \omega_s, R_p, R_s, 'S')$

natural freq
with which
filter operates

pass band
edge freq

Max loss
in pass
band

min
attenuation
of stop
band

stop band
edge freq

As per problem,

$$\omega_p = [1200, 1800]$$

$$\omega_s = [800, 2200]$$

$$R_p = 0.5 \text{ dB}$$

$$R_s = 30$$

entering these values, we get

$$n = 7$$

$$\omega_n = 1.0e+003^*$$

$$1.1441 \quad 1.8879$$

* Gain is multiplied
with 2 natural frequencies

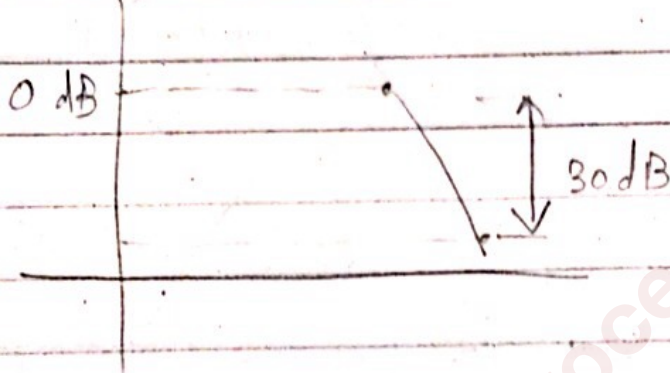
UNDERSTANDING THE BASICS.

★ Stopband attenuation > 30 dB



how much value should be attenuated at the stop band.

i.e., decrease



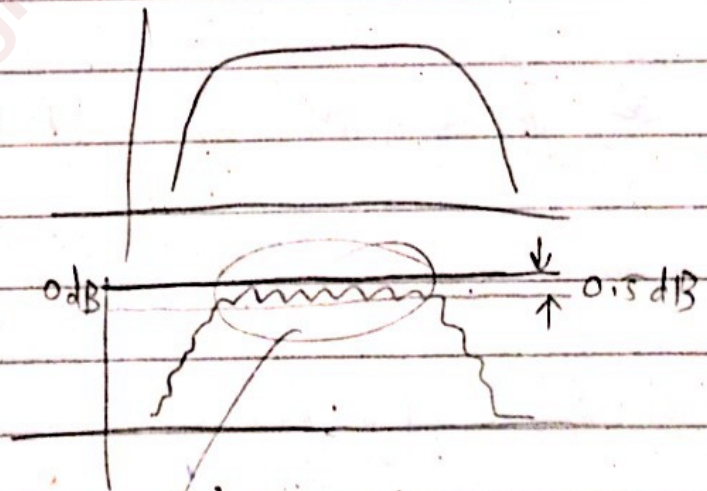
↓ decrease by 30 dB at stop band

★ Passband ripple < 0.5 dB



for any filter, say

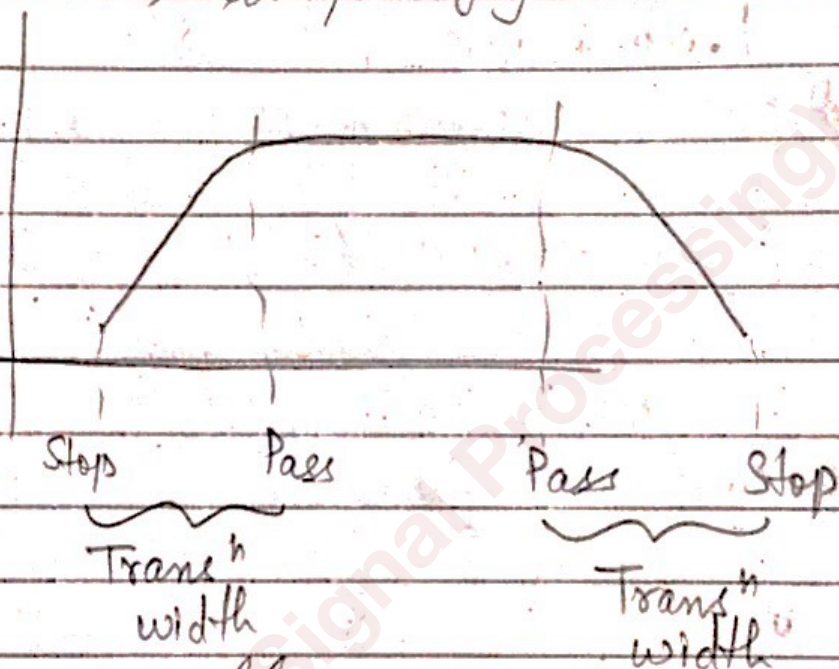
actually, it is:



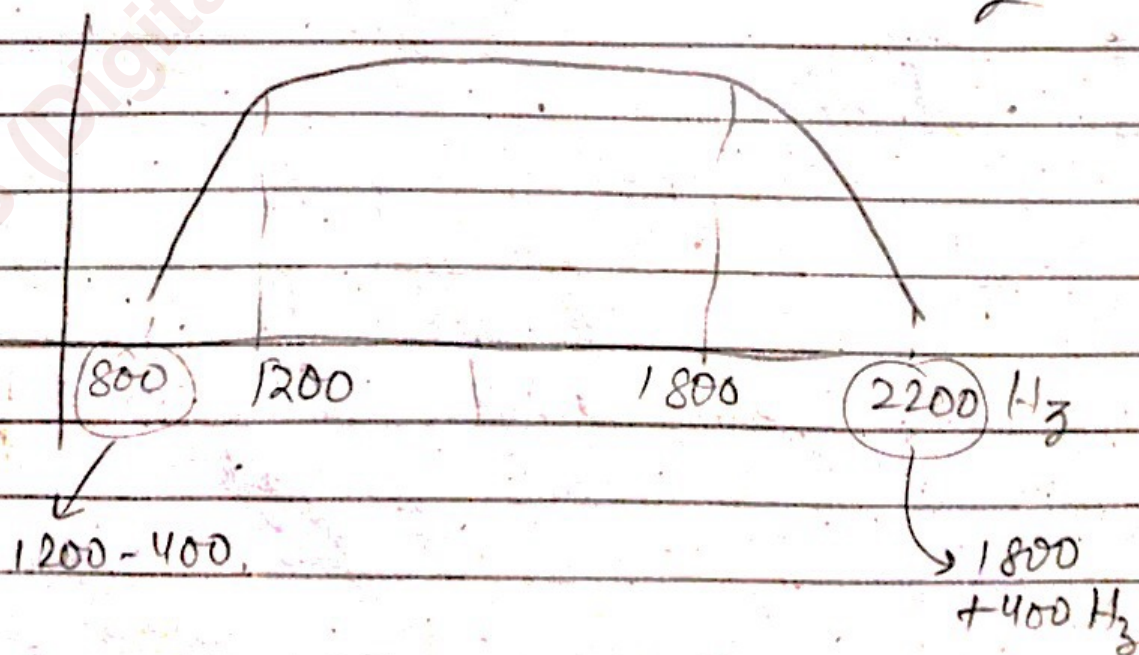
These ripples in passband can have amplitude (in dB) < 0.5 dB.

★ Transⁿ width = 400 Hz

Basically, the freq. req^d to change from passband to stopband.
 or, as per fig.



So, for our problem :- Transⁿ width = 400 Hz



* INSTRUCTION (2)

$[a, b] = \text{butter}(n, w_n, 's')$ \leftarrow

We get

$a =$
 $1.0e + 0.20$ * \rightarrow Gain
Columns 1 through 7
0 0 0 0 0

$b =$
 $1.0e + 0.44$ * \rightarrow Gain
0 0 0 0
Columns 8 through 14

Column 15
0

This instruction gives the TF of my filter $TF = \frac{b}{a}$

★ INSTRUCTION (3).

$$[h, f] = \text{freqs}(a, b) \leftarrow$$

h : coeff., f : frequency

We get different values of h & f on the screen.

$$TF = \frac{b}{a}$$

Put $a = 8(1)$.

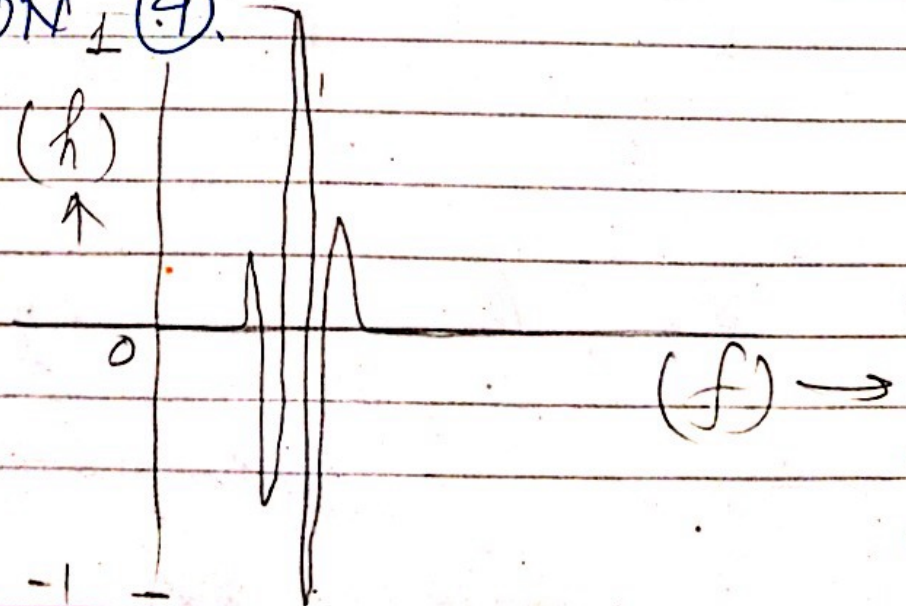
Then, output gives a poly in s .

The coeff. of s polynomial gives the coeff. of (h).

★ INSTRUCTION (4).

plot(f, h) (h)

We get this plot

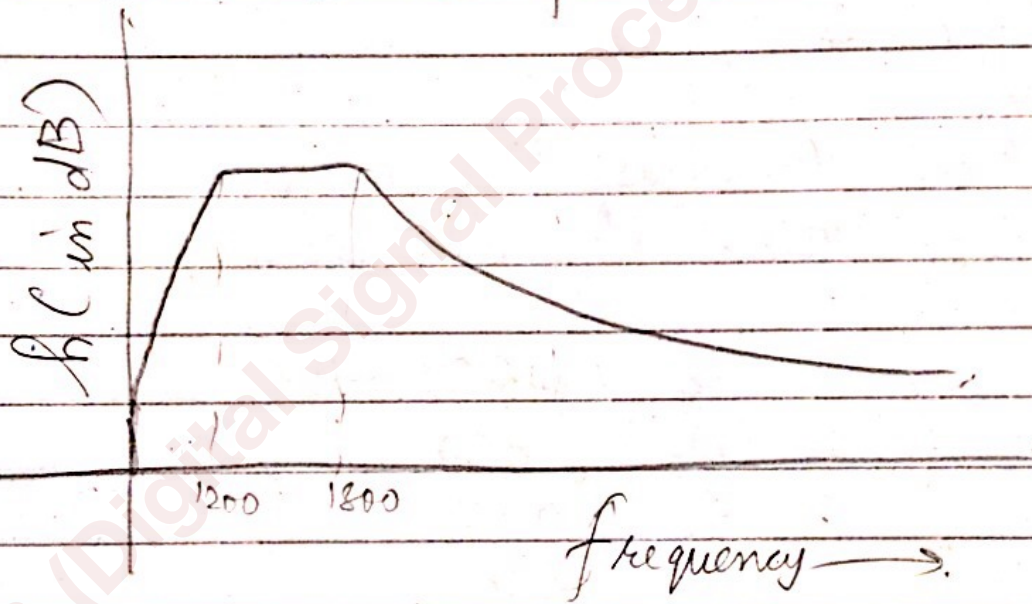


★ INSTRUCTION ⑤

plot (f, 20 * log 10 (abs(h))) ←

↓
gives a plot of $|h|$ in dB vs f .

Plot looks something like this :-



Part (b)

Chebyshev's

Instruction ①

$$[Nz, wnz] = \text{Cheb1ord}(\omega_p, \omega_s, R_p, R_s)$$

N : ord. of lowest ord. analog cheby.
Type - I filter

R_p : Max. loss in pass band

R_s : Min. attenuation in stop band

Using

$$\omega_p = [1200, 1800]$$
$$\omega_s = [800, 2200]$$
$$R_p = 0.5$$
$$R_s = 30.$$

We get

$$Nz = 4 \quad (\text{order})$$

$$wnz = \underbrace{1200 \quad 1800}$$

2 values of natural
freq.

Instruction (2)

$$[B, A] = \text{cheby1}(N, R, Wn, 's')$$

This gives value of numerator & den.
of TF

$$A = \text{---}, B = \text{---}$$

Instruction (3)

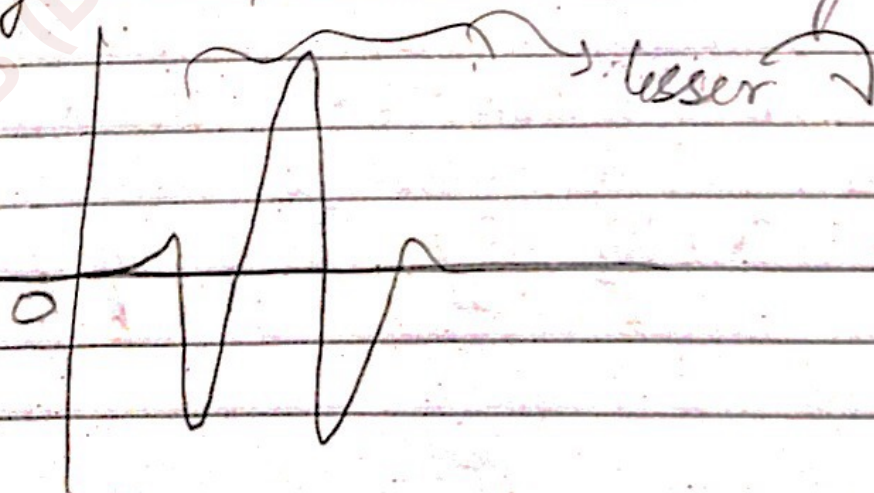
$$[h2, f2] = \text{freqs}(B, A)$$

This, just as before, gives many values of h, f

Instruction (4)

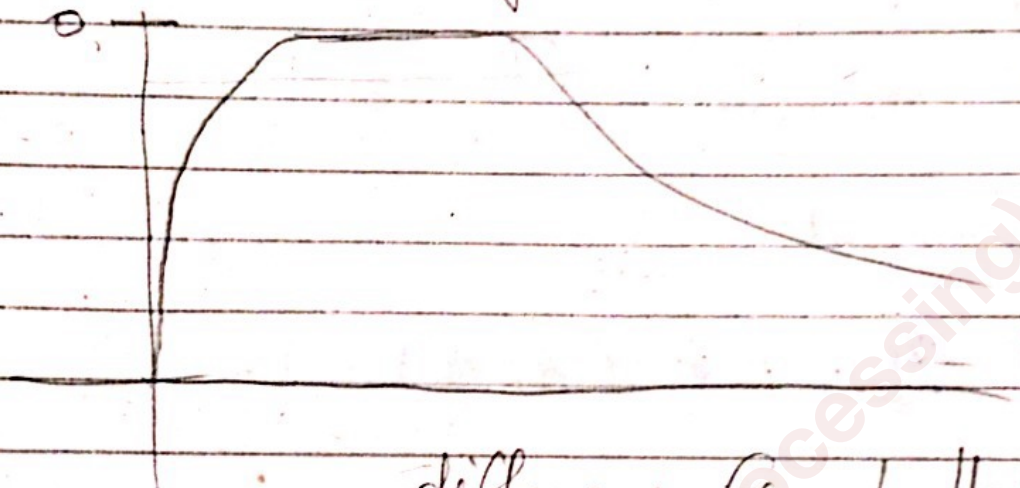
plot($f2, h2$)

We get a plot which is slightly different



Instruction (5)

plot $(f^2, 20 \cdot \log_{10}(\text{abs}(h_2))) \leftarrow$



difference from butterworth:
Touches 0 dB very nicely

Part (c) Elliptical

Instruction (1)

$[N1, Wn1] = \text{Ellipord}(w_p, w_s, R_p, R_s, 's')$

w_p, w_s, R_p, R_s (same as before)

We get ord. $N_1 = 3$.

$$W_n | = 1200 \quad 1800$$

Instruction (2).

$$[B1, A1] = \text{ELLIP}(N_1, R_p, R_s, W_n, 's') \leftarrow$$

We get a TFC :- $\frac{B1}{A1}$

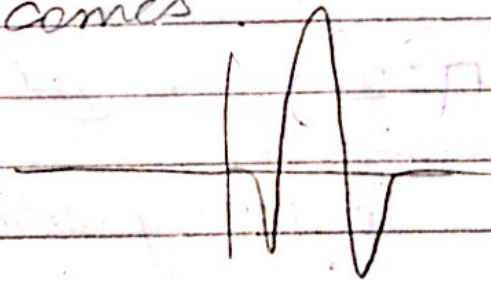
Instruction (3)

$$[h1, f1] = \text{freqs}(B1, A1)$$

values of $h1, f1$ comes

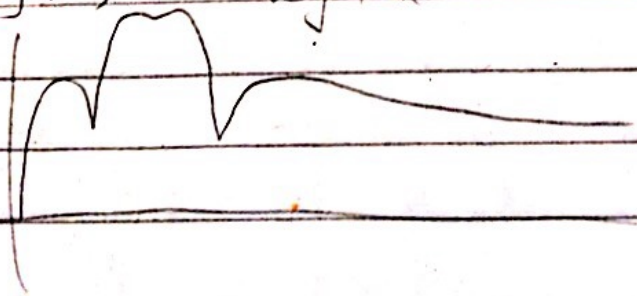
Instruction (4)

plot($f1, h1$)



Instruction (5)

$$\text{plot}(f1, 20 * \log_{10}(\text{abs}(h1))) \leftarrow$$



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Digital Signal Processing Lab

Assignment 1

Butterworth filter

Instructions -

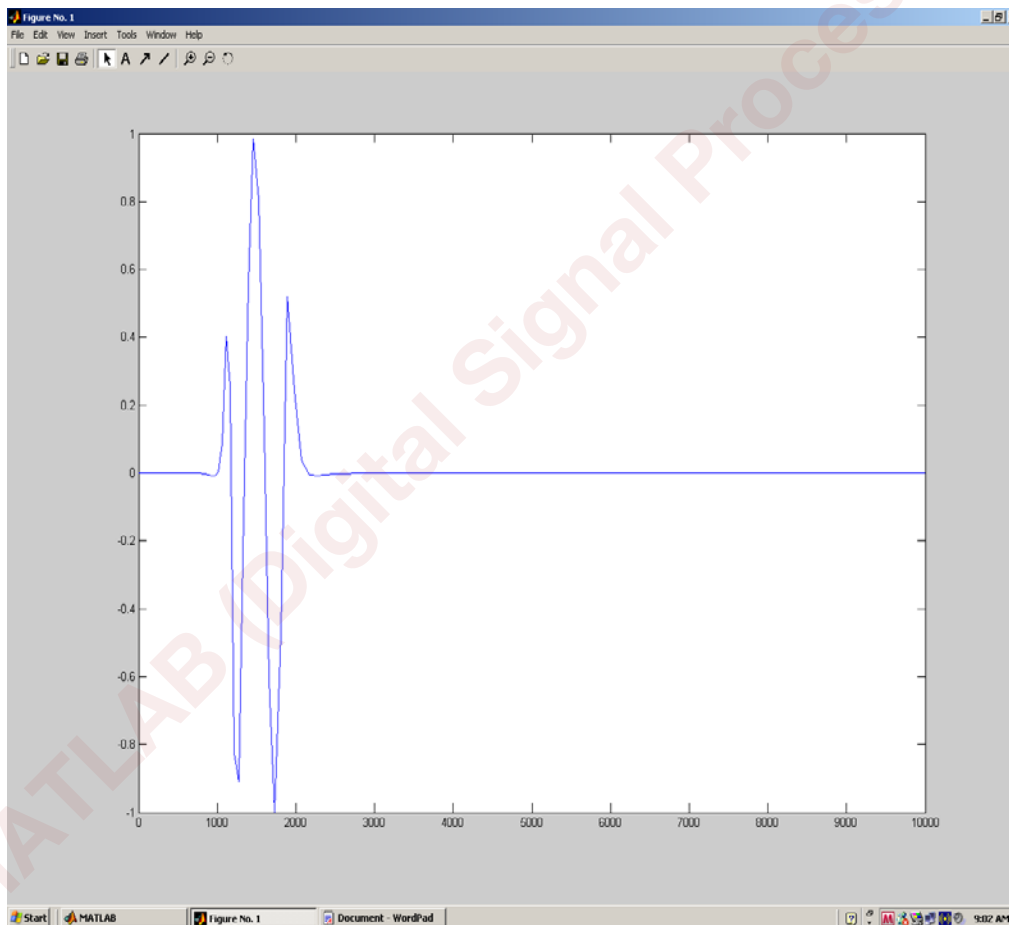
```
[N1,Wn1]=buttord([1200 1800],[800 2200],0.5,30,'s')
```

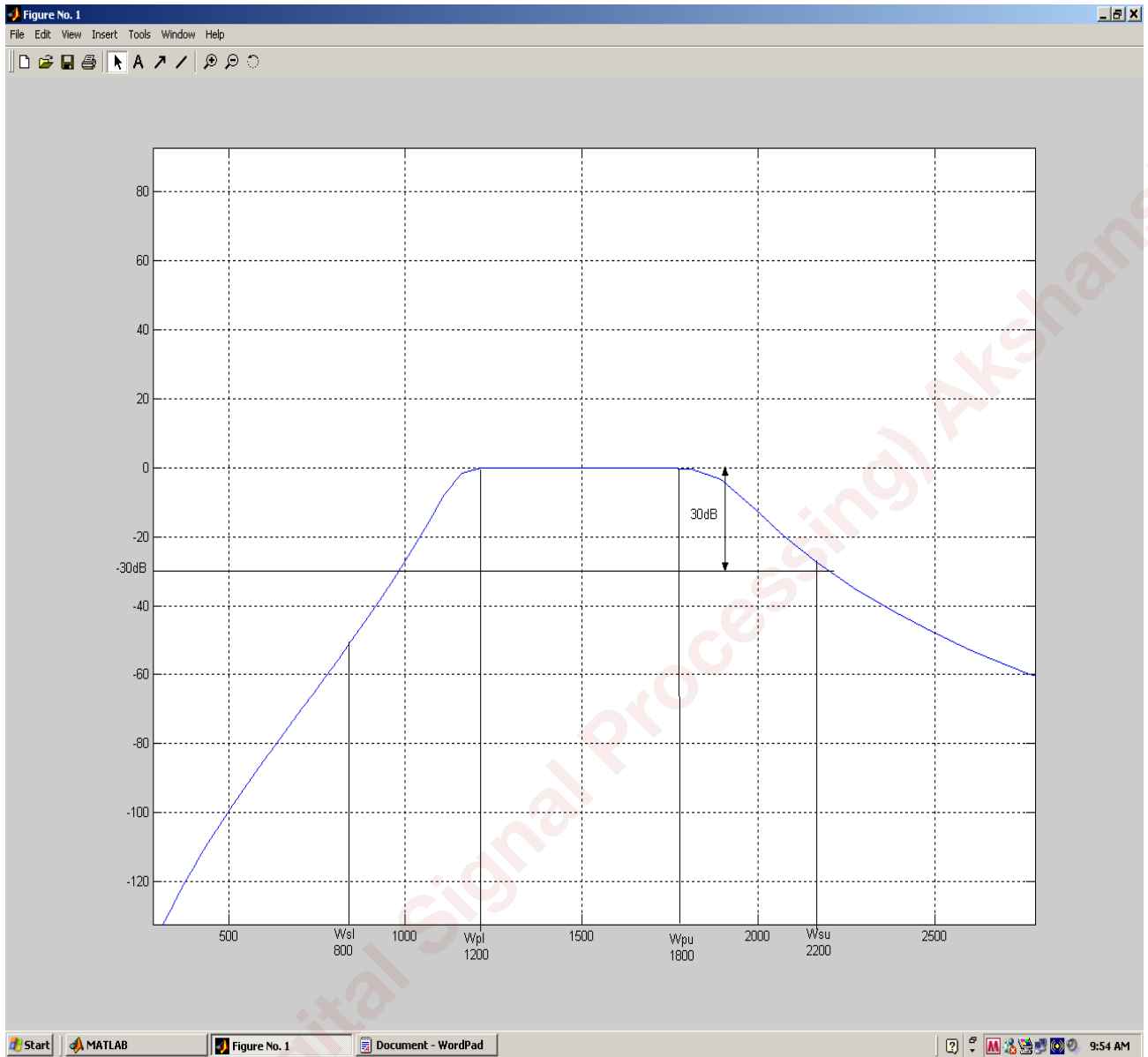
```
[B1,A1]=butter(N1,Wn1,'s')
```

```
[h1,f1]=freqs(B1,A1)
```

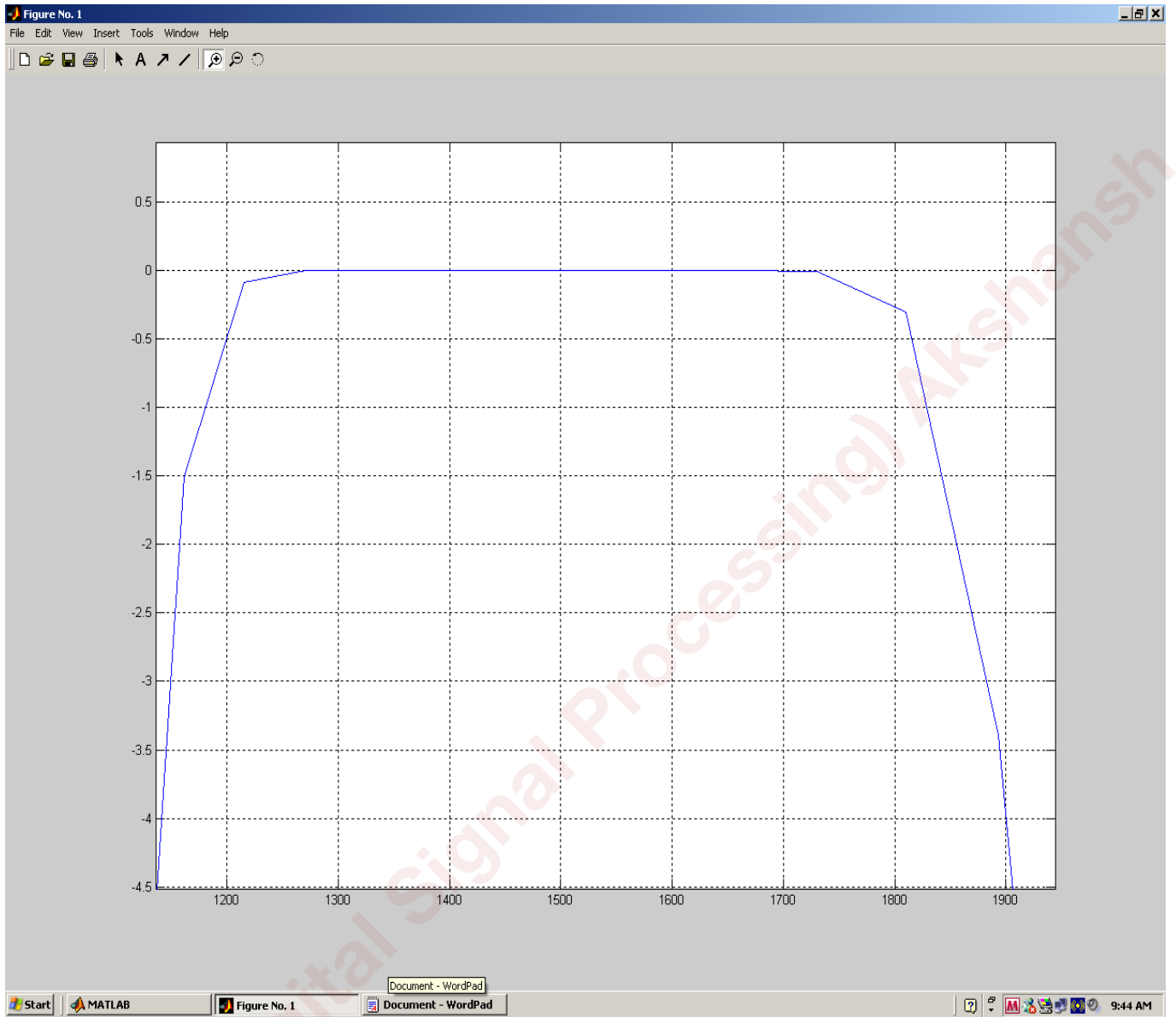
```
plot(f1,h1)
```

```
plot(f1,20*log10(abs(h1)))
```





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Chebyshev's filter

Instructions -

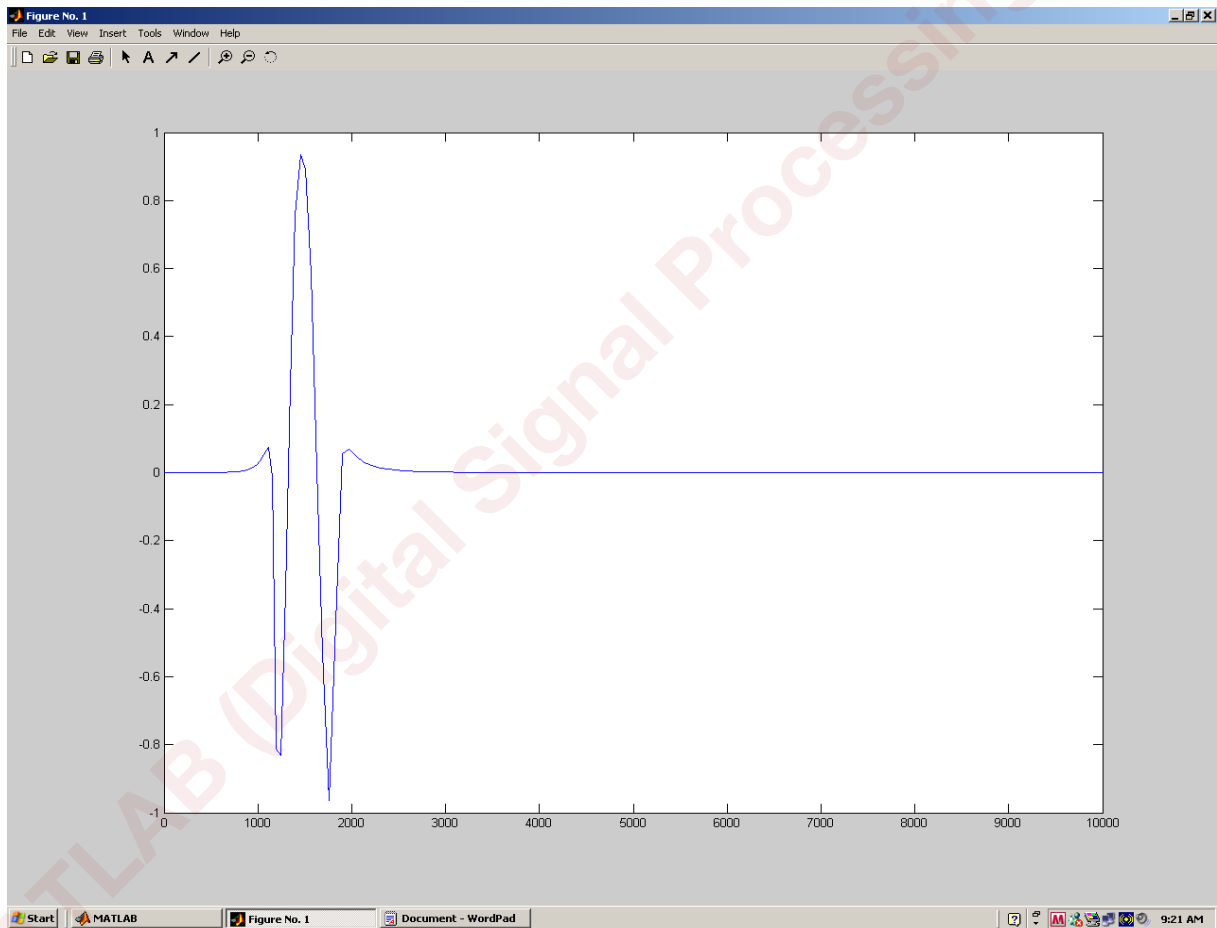
```
[N2,Wn2]=cheb1ord([1200 1800],[800 2200],0.5,30,'s')
```

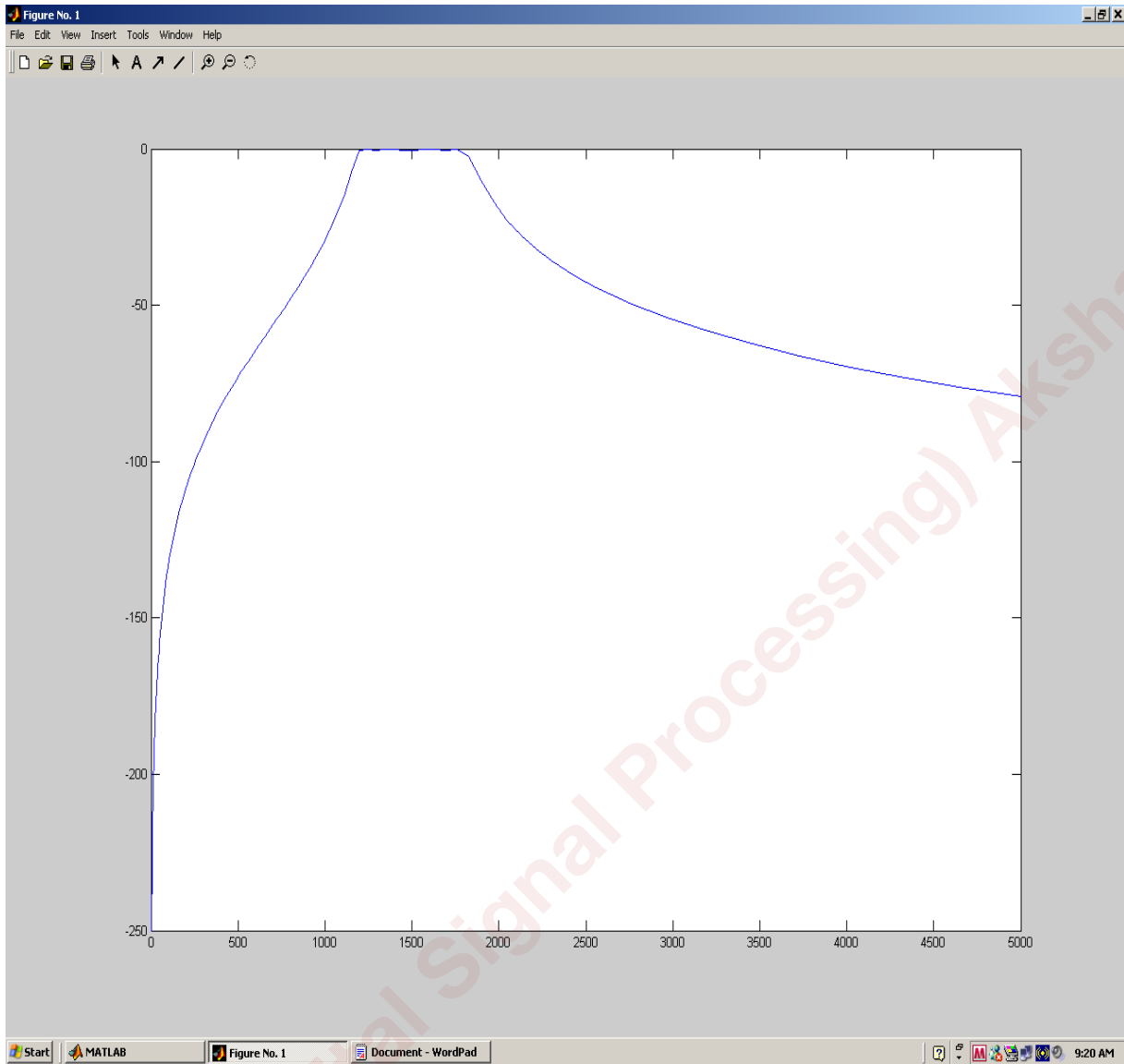
```
[B2,A2]=cheby1(4,0.5,[1200 1800],'s')
```

```
[h2,f2]=freqs(B2,A2)
```

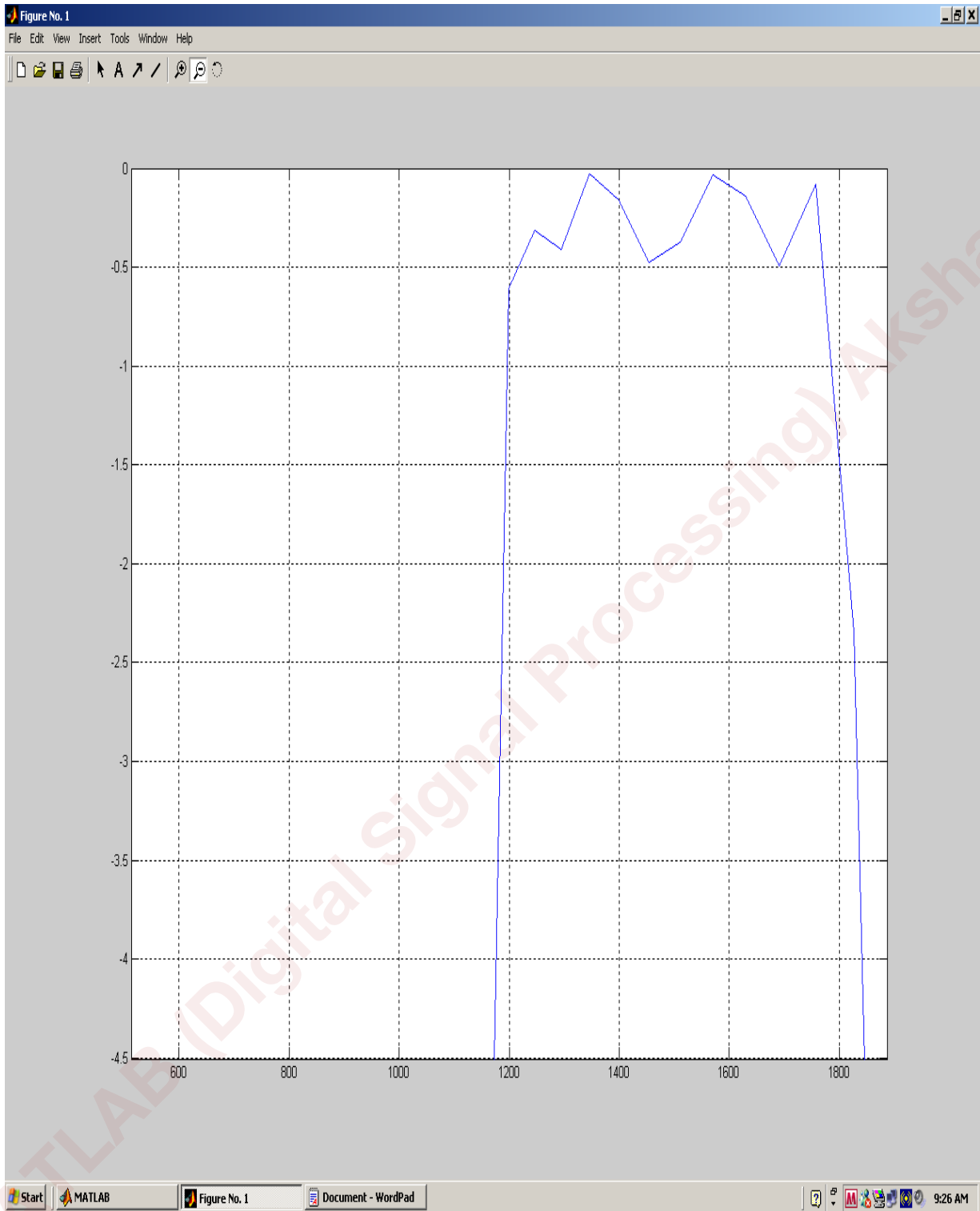
```
plot(f2,h2)
```

```
plot(f2,20*log10(abs(h2)))
```





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Elliptical filter

Instructions -

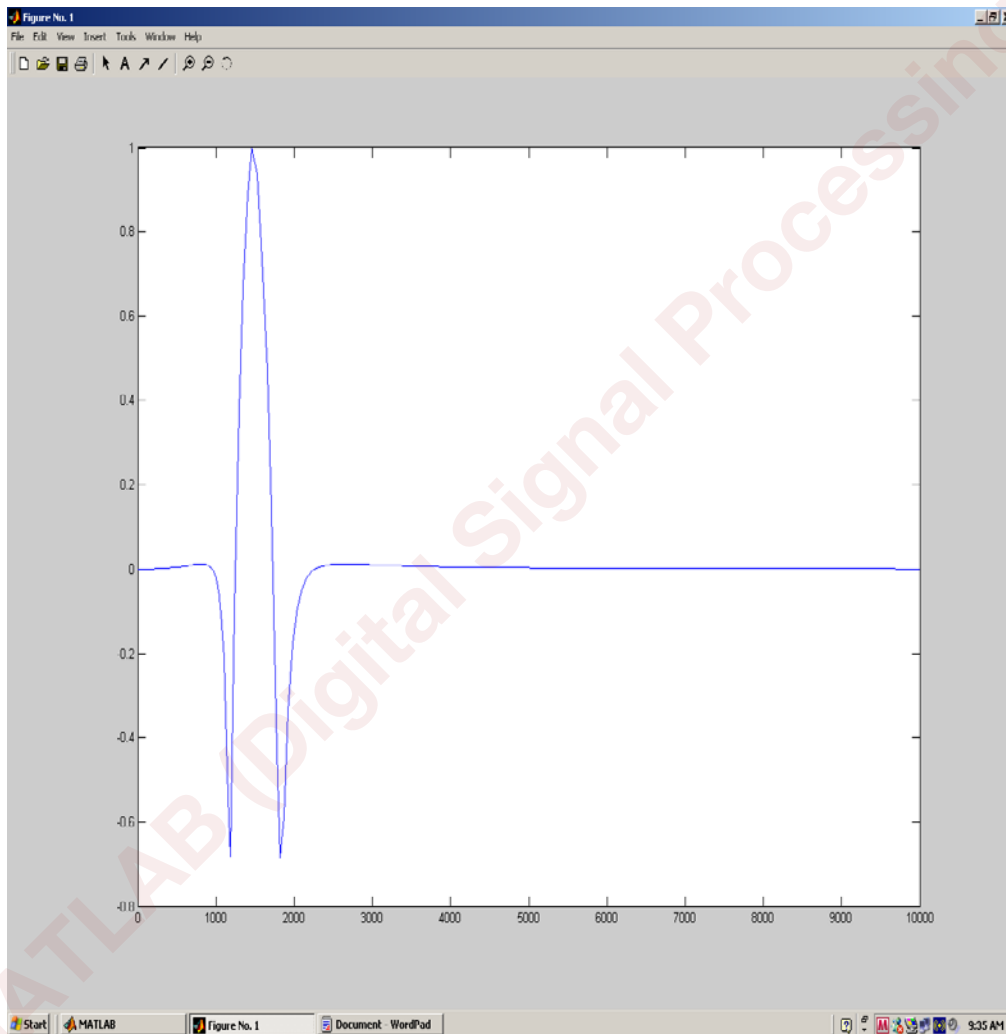
```
[N3,Wn3]=ellipord([1200 1800],[800 2200],0.5,30,'s')
```

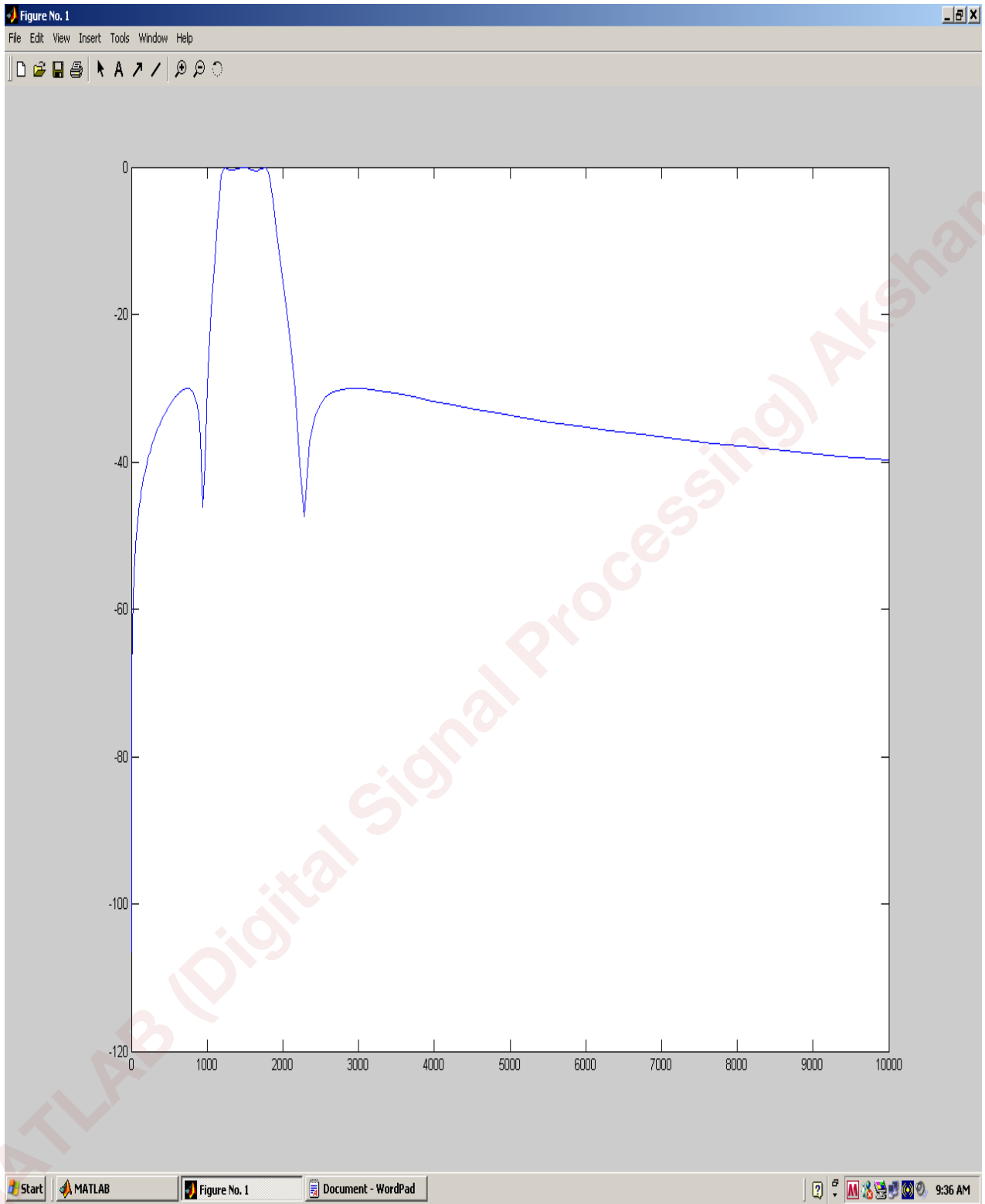
```
[B3,A3]=ellip(N3,0.5,30,[1200 1800],'s')
```

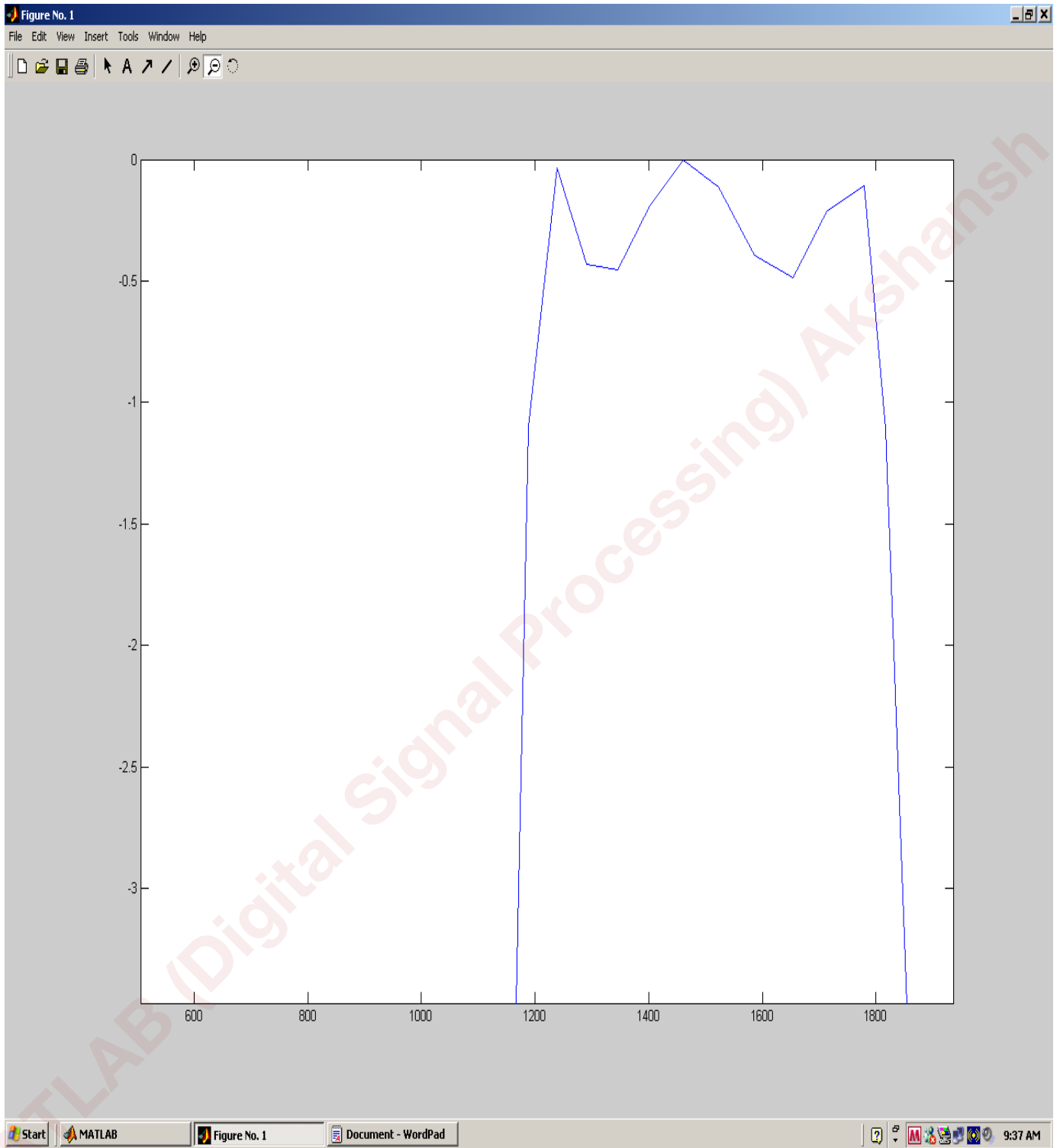
```
[h3,f3]=freqs(B3,A3)
```

```
plot(f3,h3)
```

```
plot(f3,20*log10(abs(h3)))
```







Comparison

As the order decreases, frequency decreases.

For Butterworth filter, $n=7$.

For Chebyshev's filter, $n=4$

For Elliptical Filter, $n=3$.

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MATLAB Assignment 2

Digital Signal Processing

DSP - Lab

Assignment - 2

Q. The TF of a discrete-time sys. is given

by
(TF1)

$$H(z) = \frac{z^2 - z}{z^2 - 0.9051z + 0.4096}$$

Determine location of poles and zeros.
Plot the pole zero map of function.

First, convert to -ve powers of z

So, $H(z) = \frac{z^2(1 - z^{-1})}{z^2(1 - 0.9051z^{-1} + 0.4096z^{-2})}$

(TF2)

Comparing with std. form.

$$H(z) = TF = \frac{b_0 + b_1 z^{-1} + \dots}{1 + a_1 z^{-1} + a_2 z^{-2} + \dots}$$

we get

$$b_0 = 1 \quad b_1 = -1$$

$$a_0 = 1 \quad a_1 = -0.9051 \quad a_2 = 0.4096$$

Using TF 2 : Taking coeff.

Numerator matrix gives zeros

Denominator matrix gives poles

So, f^n :- num = $\begin{bmatrix} 1 & -1 \end{bmatrix}$ \rightarrow highest power = 1
den = $\begin{bmatrix} 1 & -0.9051 & 0.4696 \end{bmatrix}$ \rightarrow power = -1
 a_0 a_1 a_2

* Some useful commands:-

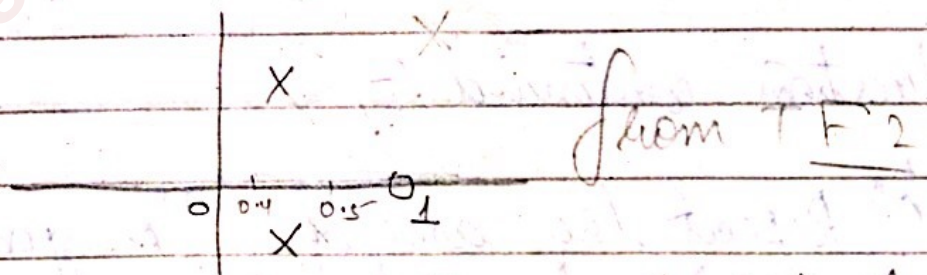
for superimposing s-plane & z-plane grids for root locus or pole/zero maps

S-grid z-grid

* Now, for plotting poles & zeros on z-plane

cmd :- pzmap(num, den)

we get



Conclusion :- Poles are outside unit circle of z-plane.
So, sys. is unstable with z powers in TF.

Using TF (1) : Taking coeff

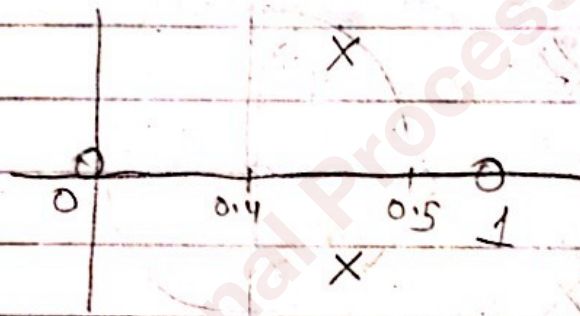
writing coeff. of TF (1) in matrix

$$a = [1 \quad -1 \quad 0]$$

$$b = [1 \quad -0.9051 \quad 0.4096]$$

pzmap. (a, b)

we get



Conclusion:

Poles are inside ^{unit circle} z plane. So, sys. is stable with +ve powers of z in TF

Question continued :-

(b) Repeat the same if f^n is given by

$$H(z) = 1 - z^{-1}$$

$$1 - 0.9051z^{-1} + 0.4096z^{-2}$$

- (c) plot pole-zero diagram of $H(z)$ in both cases
- (i) with numerator & denominator polynomial coefficients as inputs.
 - (ii) with poles and zeroes as inputs.

- (d) Plot the frequency response of the DT sys. with a sampling frequency of
- (i) 1 kHz
 - (ii) 10 kHz
 - (iii) 100 kHz

Digital Signal Processing
MATLAB Assignment 2
Akshansh Chaudhary
Id no. – 2011AAPS300U

Question: The transfer function of a discrete time system is given by

- (a) $H(z) = (z^2 - z) / (z^2 - 0.9051z + 0.4096)$
 Determine the location of poles and zeroes.
 Plot the pole zero map of function.
- (b) Repeat the same if function is given by
 $H(z) = (1 - z^{-1}) / (1 - 0.9051z^{-1} + 0.4096z^{-2})$
- (c) Plot pole-zero diagram of $H(z)$ in both cases
 - (i.) With numerator and denominator polynomial coefficients as inputs
 - (ii.) With poles and zeroes as inputs
- (d) Plot the frequency response of the DT system with a sampling frequency of
 - (i.) 1 kHz
 - (ii.) 10kHz
 - (iii.) 100kHz

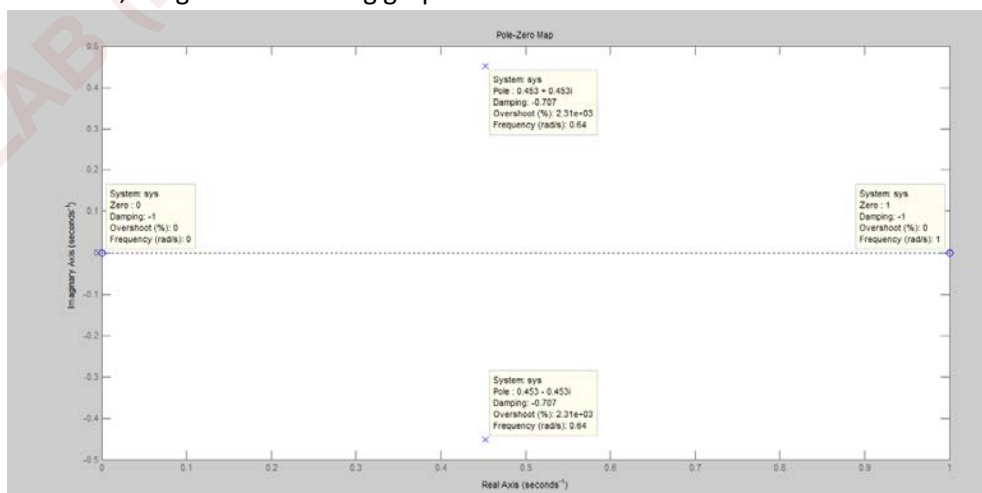
Solution:

Let the transfer functions be named as

- (a) $TF1 = (z^2 - z) / (z^2 - 0.9051z + 0.4096)$
- (b) $TF2 = (1 - z^{-1}) / (1 - 0.9051z^{-1} + 0.4096z^{-2})$

Subpart 1: Polynomial coefficients of TF1 and TF2 as inputs:

- a. For TF1,
 Commands:
 $A = [1 -1 0]; B = [1 -0.9051 0.4096];$
`pzmap(A,B)`
 From this, we get the following graph –



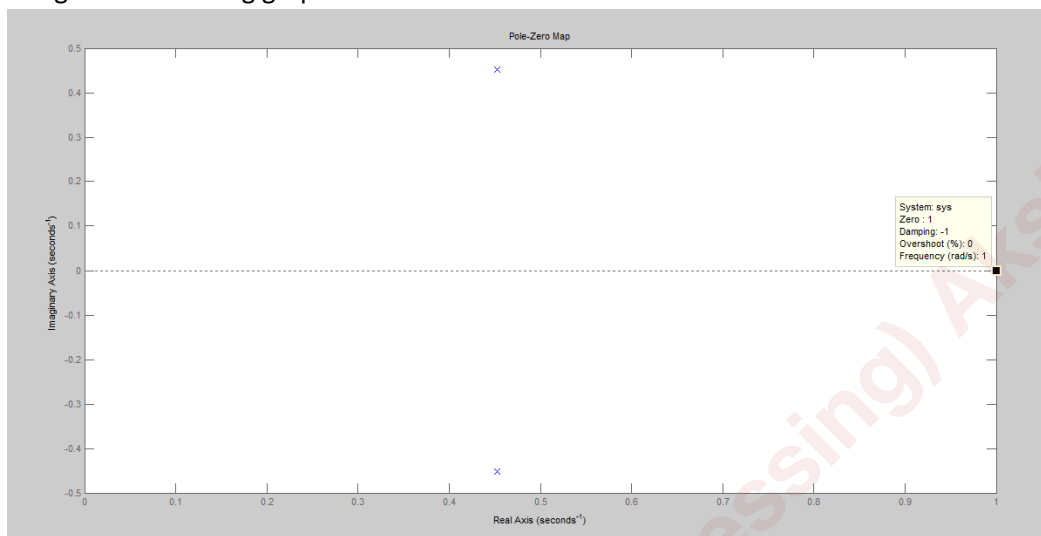
b. For TF2,

Commands:

```
num=[1 -1]; den=[1 -0.9051 0.4096];
```

```
pzmap(num,den)
```

We get the following graph –



Subpart 2: Poles and Zeroes as inputs:

a. For TF1,

Finding the poles and zeroes of the TF.

Commands:

```
>> A1=roots(A)
```

```
A1 =
```

```
0
```

```
1
```

```
>> B1=roots(B)
```

```
B1 =
```

```
0.4526 + 0.4525i
```

```
0.4526 - 0.4525i
```

b. For TF2,

Commands:

```
>> num1=roots(num)
```

```
num1 =
```

```
1
```

```
>> den1=roots(den)
```

```
den1 =
```

```
0.4526 + 0.4525i
```

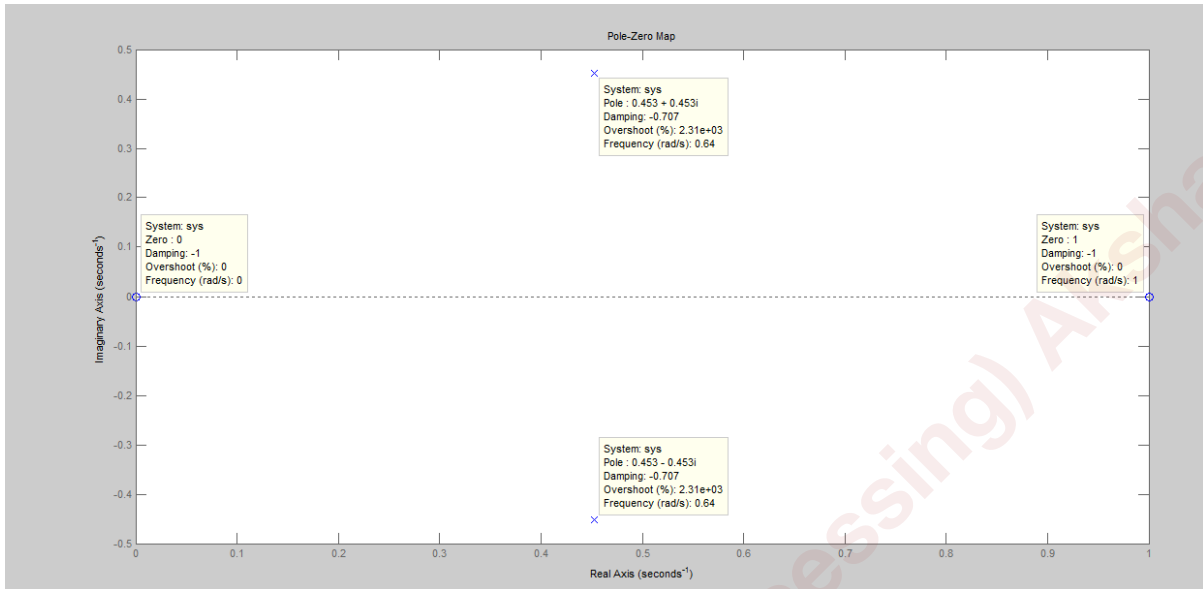
```
0.4526 - 0.4525i
```

Now, commands for making the pole zero plot for Subpart 2:

Commands:

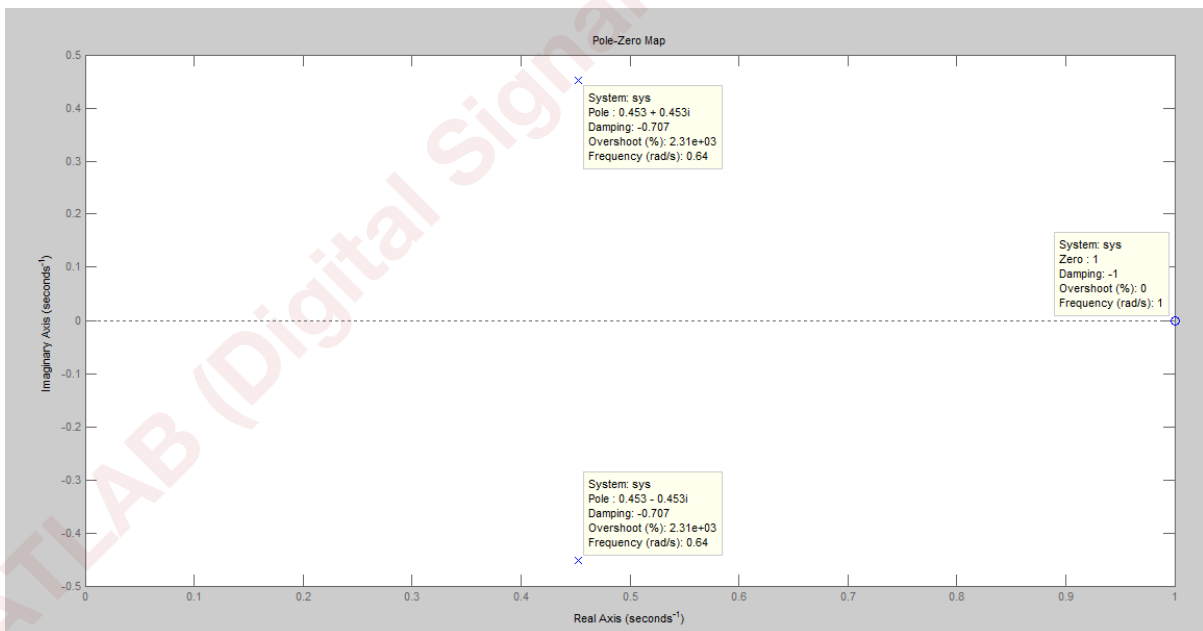
a. For TF1

>> pzmap(B1,A1)



b. For TF2

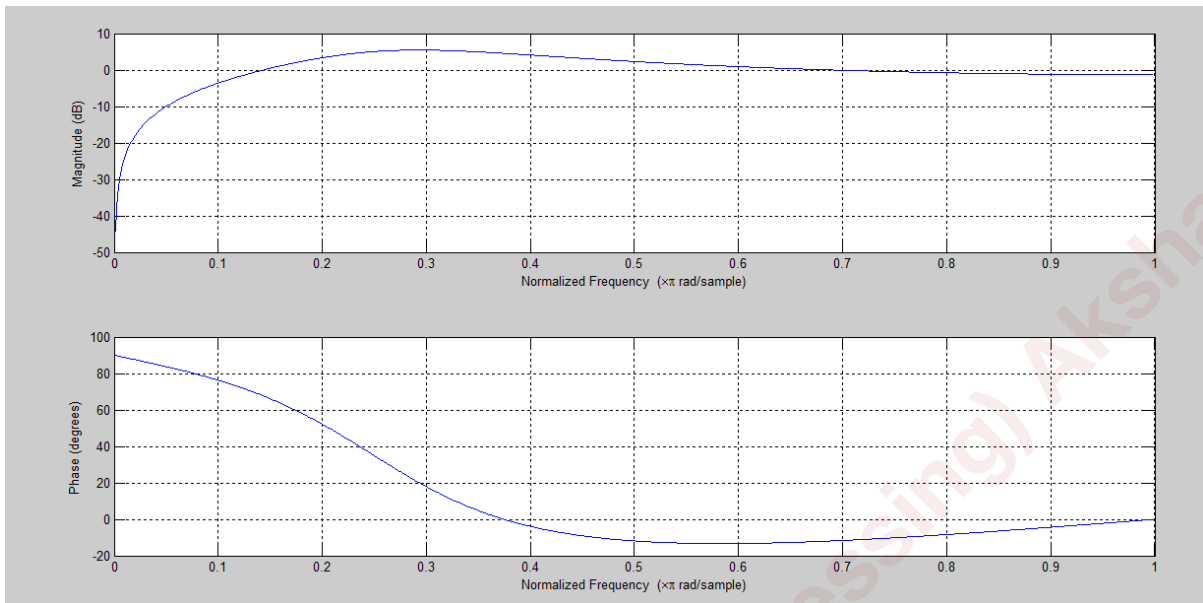
>> pzmap(den1,num1)



Part (d). Finding frequency response of DT system with a sampling frequency of

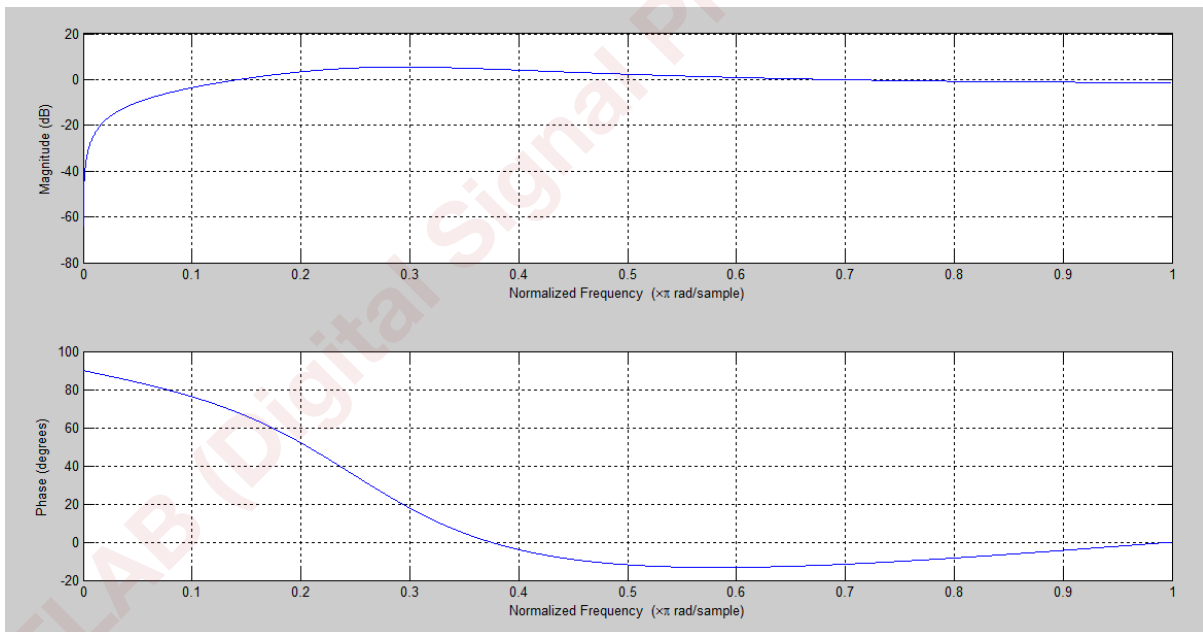
i. 1kHz

Command: `freqz(num,den,1000)`

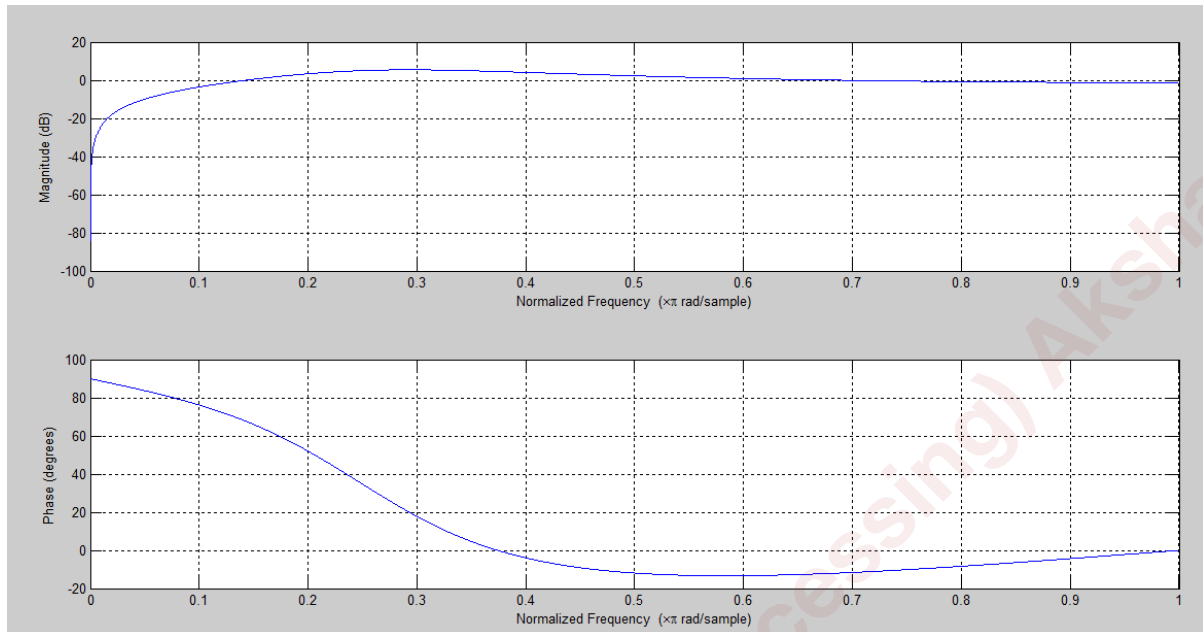


ii. 10kHz

Command: `freqz(num,den,10000)`



- iii. 100kHz
Command:
Freqz(num,den,100000)



Observation and Analysis –

It was found that the order of the given transfer function (in z domain) changes when the transfer function is rearranged from positive powers of z to negative powers of z.

So, TF1 (positive powers of z) has order =2 (w.r.t numerator)

And, TF2 (negative powers of z) has order =1 (w.r.t numerator)

Also, it was found that the pole zero plot using the coefficients of the transfer function as matrix and the poles and zeroes as matrix is same for both TF1 and TF2.

Finally,

In the frequency response plots, the plots for both TF1 and TF2 were found to be the same. And, on seeing the plots on different frequencies, the plots were nearly the same with little difference in the magnitude part of the plot on changing the frequency.

MATLAB Assignment 3

Digital Signal Processing

DSP-Lab

Assignment - 3

- Q. Compare impulse invariant and bilinear z-transform methods in terms of
- the Nyquist effect on the magnitude, phase & group delay responses.
 - Distribution for pole-zero diagrams.
- Do this for LP, HP, BP & BS filters.

Case ①

LP

Given:-
following
specs

Passband	0 - 1 kHz
Stopband	3 - 5 kHz
passband ripple	1 dB
stopband attenuation	60 dB
Sampling frequency	10 kHz

Now, we have to make

- | | | |
|-----------------------|-------|---|
| (a) Magnitude Plot | } for | (i) Impulse Invariant
&
(ii) BZT. |
| (b) Phase plot | | |
| (c) Group Delay | | |
| (d) Pole-zero diagram | | |

- (a) $\text{freqz}(b_z, a_z, f_s)$ (i) $[b_z, a_z] = \text{impinvar}(b, a, f_s)$
num den.
- (b) $\text{phasedelay}(b_z, a_z, \omega)$
- (c) $\text{grpdelay}(b_z, a_z, \omega)$ (ii) $[b_1, a_1] = \text{bilinear}(b, a, f_s)$
- (d) $\text{zplane}(b_z, a_z)$

codes to convert analog to digital & plotting

Case (4) :- BS filter

Given specs :- passband 0-15 kHz
 30-50 kHz
 stopband 20-25 kHz
 passband ripple 0.2 dB
 stopband attenuation = 40 dB
 sampling freq. = 100 kHz

Idea :- for any case, first, it is told that we have to use Elliptical filter

Then, we are given specs.

So, just like in assignment 1, design an analog filter using these specs.

After that convert it into digital domain

by using (i) Impulse invariant }
 (ii) BZT method. } codes given above

Solving case (4)

Part (1) :- Designing analog elliptical filter.

Part (2) :- Converting analog to digital using
(i) Impulse invariant method
↳ Find poles (a), (b), (c), (d)
(ii) BZT method
↳ Find poles (a), (b), (c), (d)

Part (1)

Instruction (1)

$[NI, WNI] = \text{ellipord}(Wp, Ws, Rp, Rs, 's')$

$$Wp = [15000/50000, 30000/50000]$$

$$Ws = [20000/50000, 25000/50000]$$

$$Rp = 0.2$$

$$Rs = 40$$

$$fs = 100000$$

Instruction gives value of WNI & NI ,

$$WNI = 0.3333 \quad 0.6$$

$$NI = 4$$

Instruction ②

$$[B1, A1] = \text{ellip}(N1, Rp, Rs, wn1, 'stop')$$

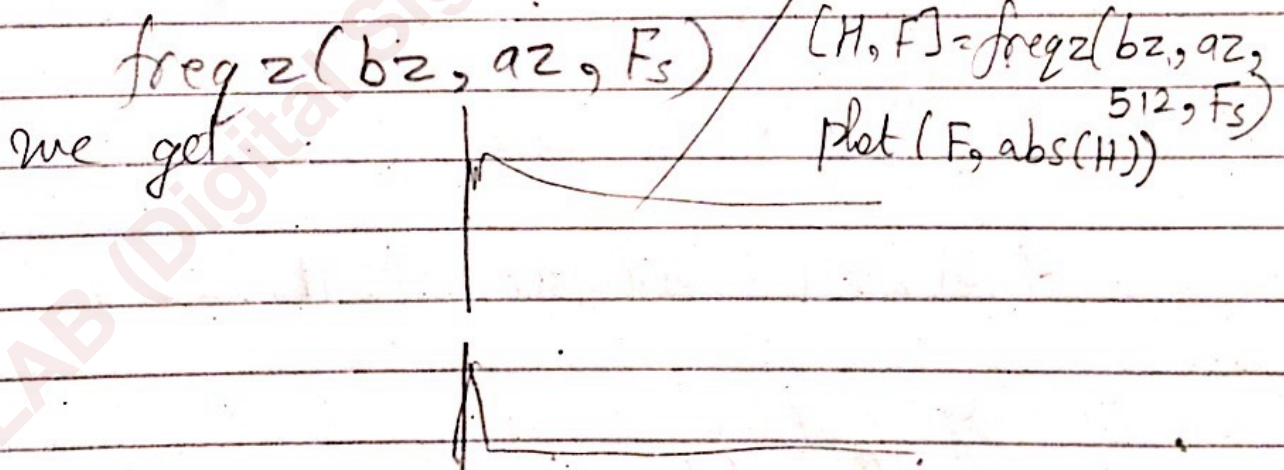
we get $B1 = \dots$
 $A1 = \dots$

Conversion to analog done

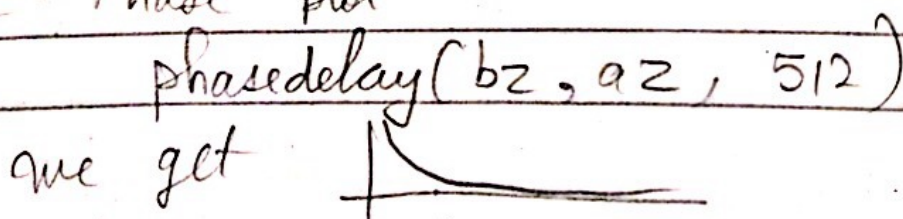
Part ② :- (i) Impulse invariant method.

$$[bz, az] = \text{impinvar}(B1, A1, Fs)$$

(a) Magnitude plot



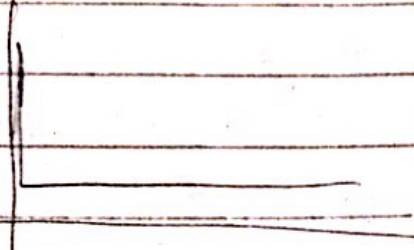
(b) Phase plot



(c) Group delay

group delay (b_2, a_2, ω)

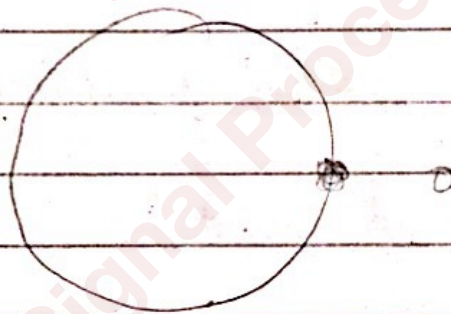
we get :



(d) Pole zero diagram

z-plane (b_2, a_2)

we get



(ii) BZT method

$[b_1, a_1]$ = bilinear (B_1, A_1, F_s)

(a) Magnitude plot

freqz (b_1, a_1, F_s)

(b) Phase plot
phasedelay (b1, a1, 512)

(c) Group delay
grpdelay (b1, a1, 512)

(d) Pole zero diagram
zplane (b1, a1)

Assignment 3

Akshansh Chaudhary

ID – 2011AAPS300U

Dated - 7.10.2013

Question-

Given the specifications of a band stop filter, make it an analog filter and convert it to digital filter using impulse invariant method and Bilinear z transform method. Also, find the magnitude plot, phase plot, group delay and pole zero diagrams for both the methods.

Solution -

Part (1)

Making analog elliptical filter

Initializing the value of W_p, W_s, R_p, R_s for the elliptical filter

```
Rp=0.2
Rp =
    0.2000
>> Rs=40
Rs =
    40
>> Fs=100000
Fs =
    100000
>> Wp=[15000/50000, 30000/50000]
Wp =
    0.3000    0.6000
```

```
>> Ws=[20000/50000,25000/50000]
Ws =
    0.4000    0.5000
```

Instructions after initialization

```
>> [N1,Wn1]=ellipord(Wp,Ws,Rp,Rs,'s')
N1 =
     4
Wn1 =
    0.3333    0.6000
```

```
[B1,A1]=ellip(N1,Rp,Rs,Wn1,'stop')
B1 =
Columns 1 through 3
    0.3198   -0.4313    1.3982
Columns 4 through 6
   -1.2748    2.1536   -1.2748
Columns 7 through 9
    1.3982   -0.4313    0.3198
A1 =
Columns 1 through 3
    1.0000   -0.9838    1.9828
Columns 4 through 6
   -1.4369    1.8869   -0.8671
Columns 7 through 9
    0.7043   -0.2039    0.1459
```

Part (2)

Converting to Digital

(i.) Impulse Invariant Method

```
[bz,az]=impinvar(B1,A1,Fs)
```

```
bz =
```

```
1.0e-003 *
```

```
Columns 1 through 8
```

```
0.0029 -0.0238 0.0859 -0.1772 0.2284 -0.1882 0.0968 -0.0284
```

```
Column 9
```

```
0.0037
```

```
az =
```

```
Columns 1 through 8
```

```
1.0000 -8.0000 28.0000 -56.0001 70.0002 -56.0002 28.0001 -8.0000
```

```
Column 9
```

```
1.0000
```

(a.) Magnitude Plot

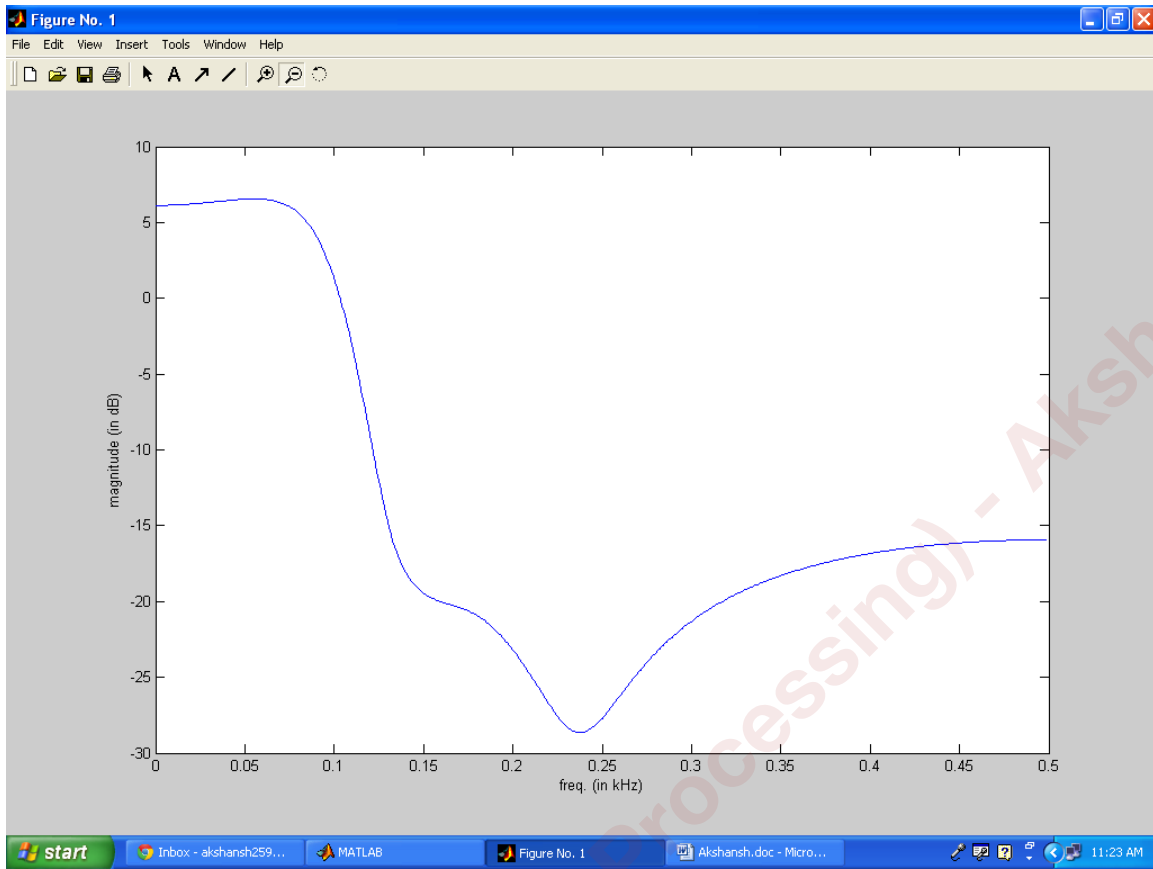
```
>> [H,F]=freqs(bz,az)
```

```
>> plot(F,20*log10(abs(H)))
```

```
>> xlabel('freq. (in kHz)')
```

```
>> ylabel('magnitude (in dB)')
```

(Note: Graphs got in one version of MATLAB may differ in other versions)



Observations from the graph:

The stop band is between 0.2 and 0.25 kHz as required.

Pass band is between 0-0.15 kHz and then 0.3-0.5 kHz as in problem.

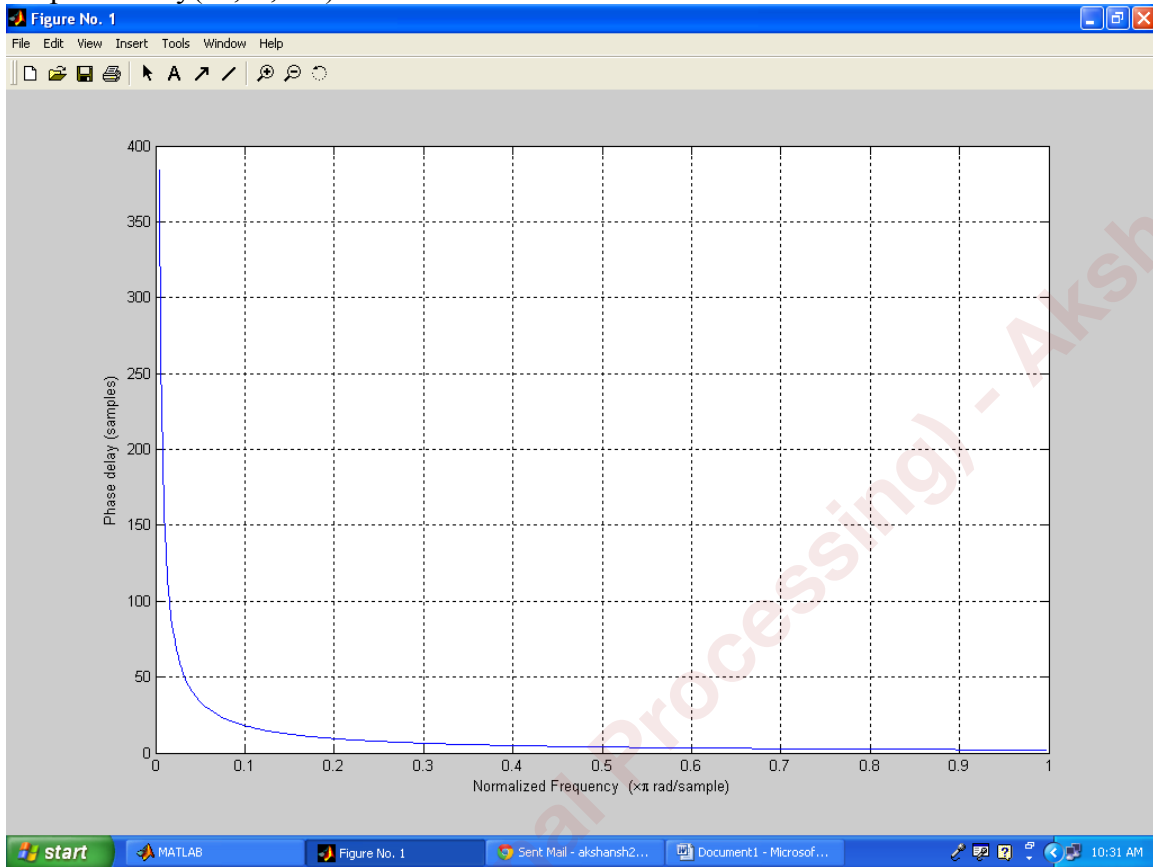
The pass band ripple is nearly 0.2 (after zooming the pass band area)

The stop band ripple has a little deviation. Its coming as 30 db (instead of 40 dB given.)

The problem becomes more ideal when the sampling frequency is increased.

(b.) Phase delay

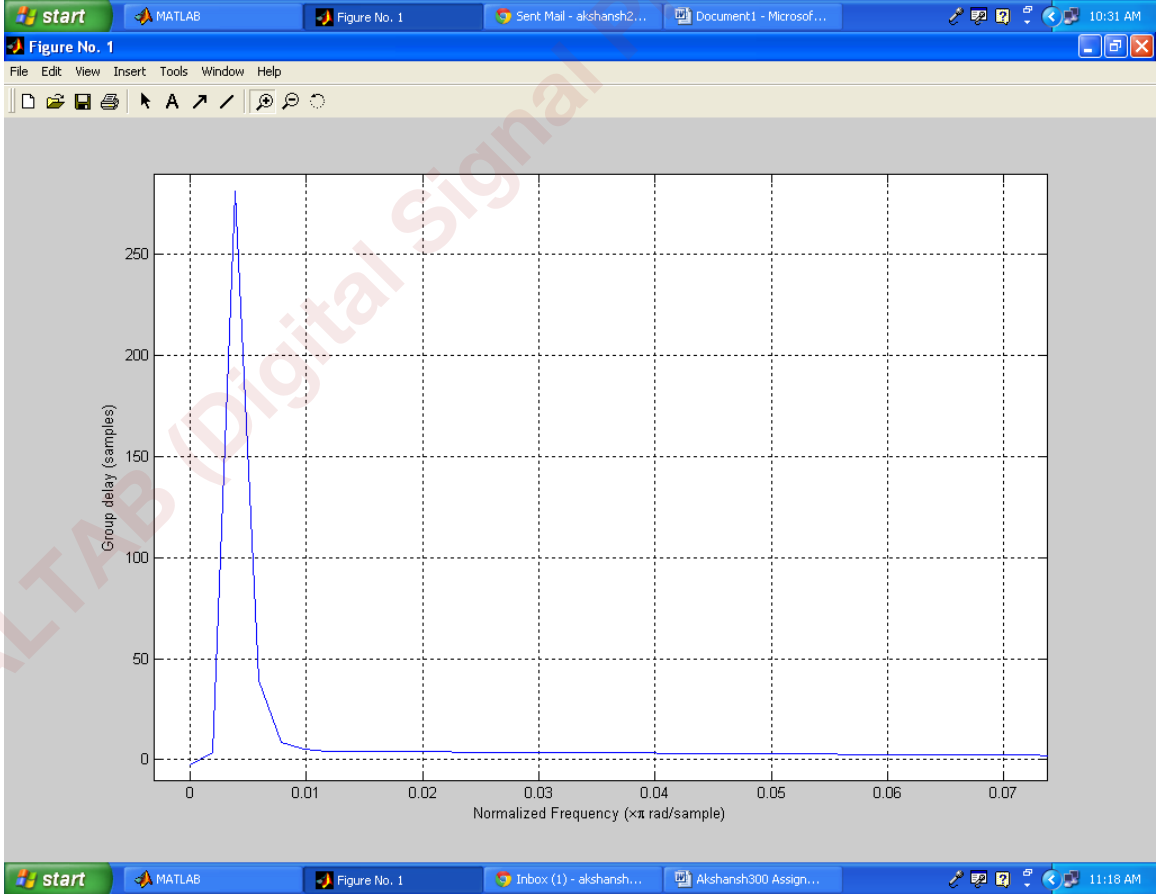
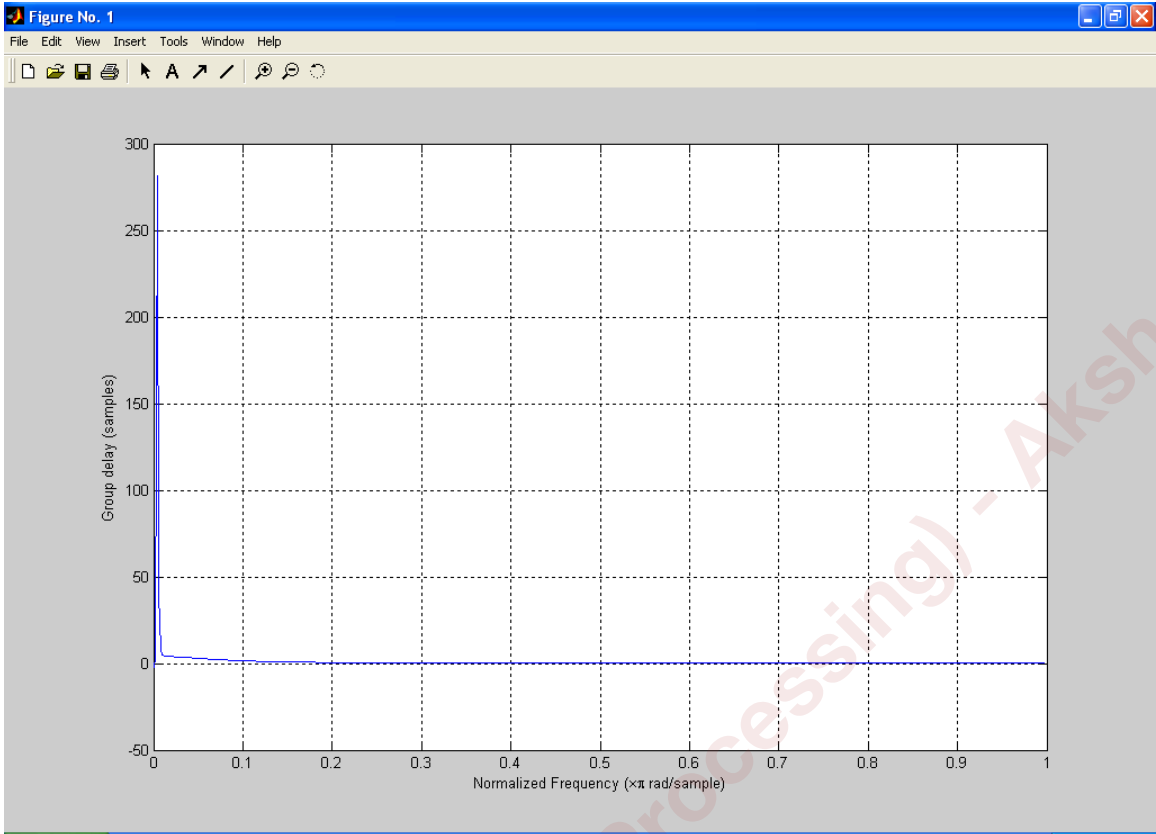
```
>> phasedelay(bz,az,512)
```



(c.) Group Delay

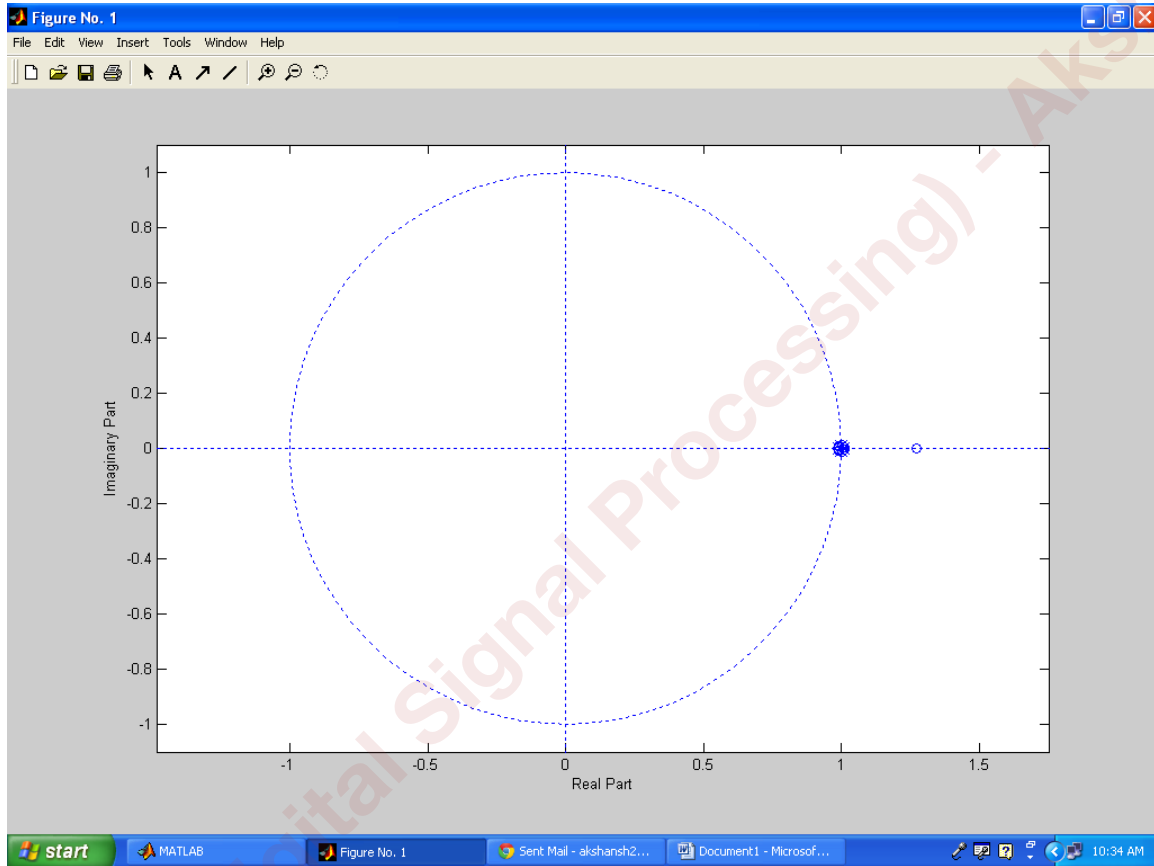
```
>> grpdelay(bz,az,512)
```

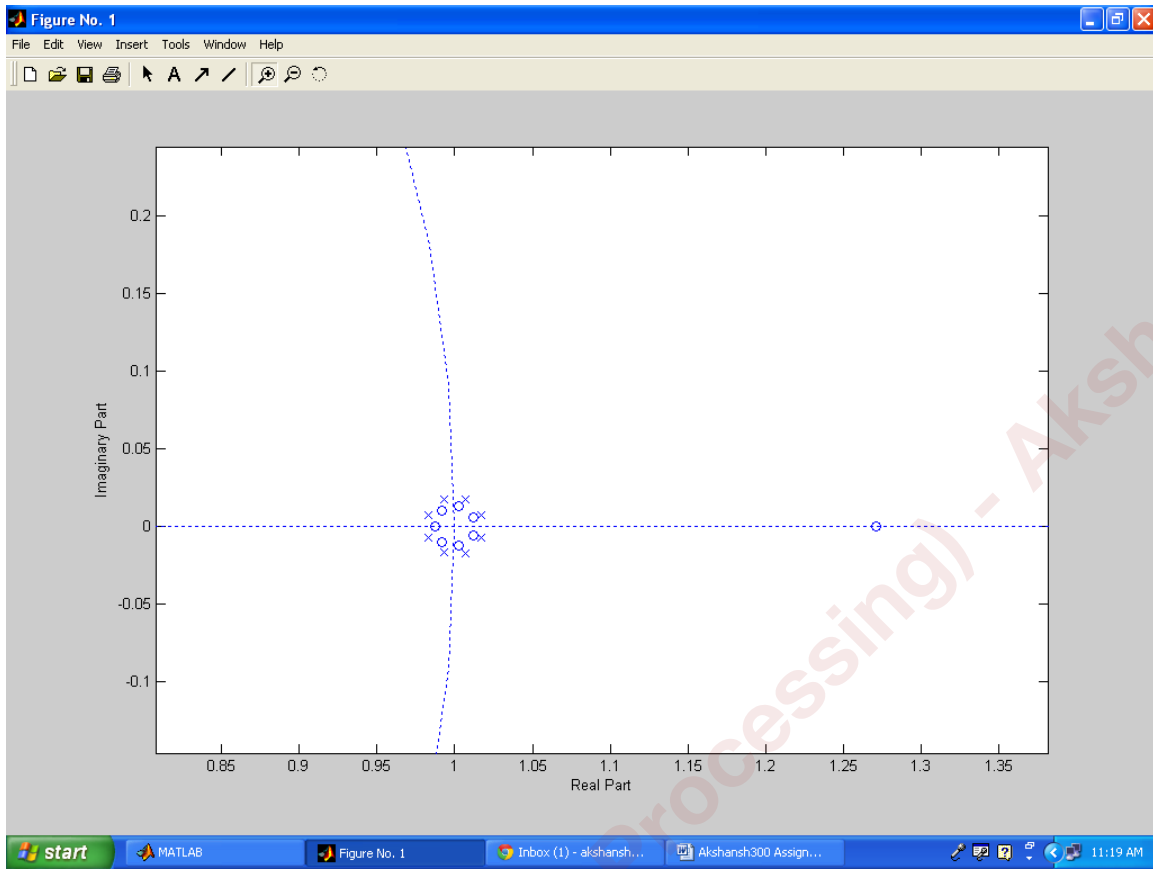
```
>>
```



(d.) Pole zero diagrams

`zplane(bz,az)`





(ii.) BZT Method

```
>> [b1,a1]=bilinear(B1,A1,Fs)
```

```
b1 =
```

```
Columns 1 through 8
```

```
0.3652 -2.9218 10.2263 -20.4526 25.5658 -20.4527 10.2263 -2.9218
```

```
Column 9
```

```
0.3652
```

```
a1 =
```

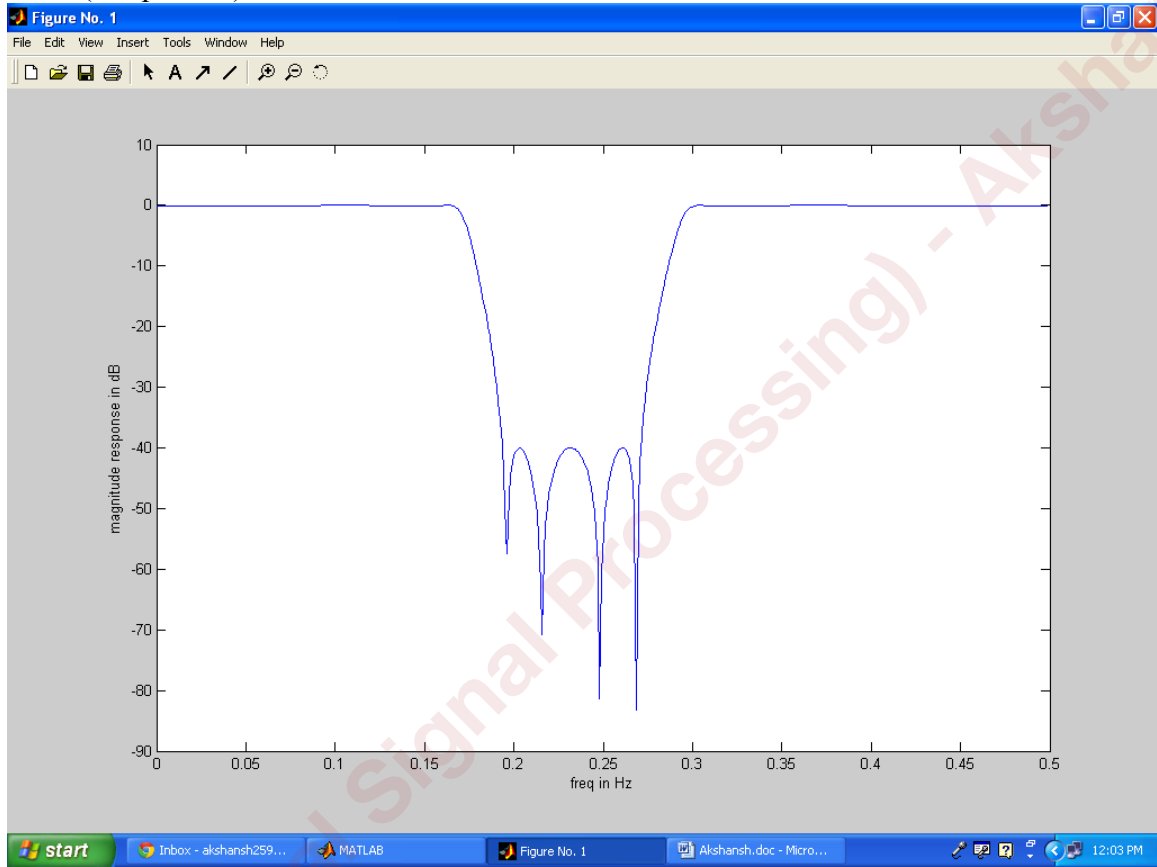
```
Columns 1 through 8
```

```
1.0000 -8.0000 28.0000 -56.0001 70.0002 -56.0002 28.0001 -8.0000
```

```
Column 9
```

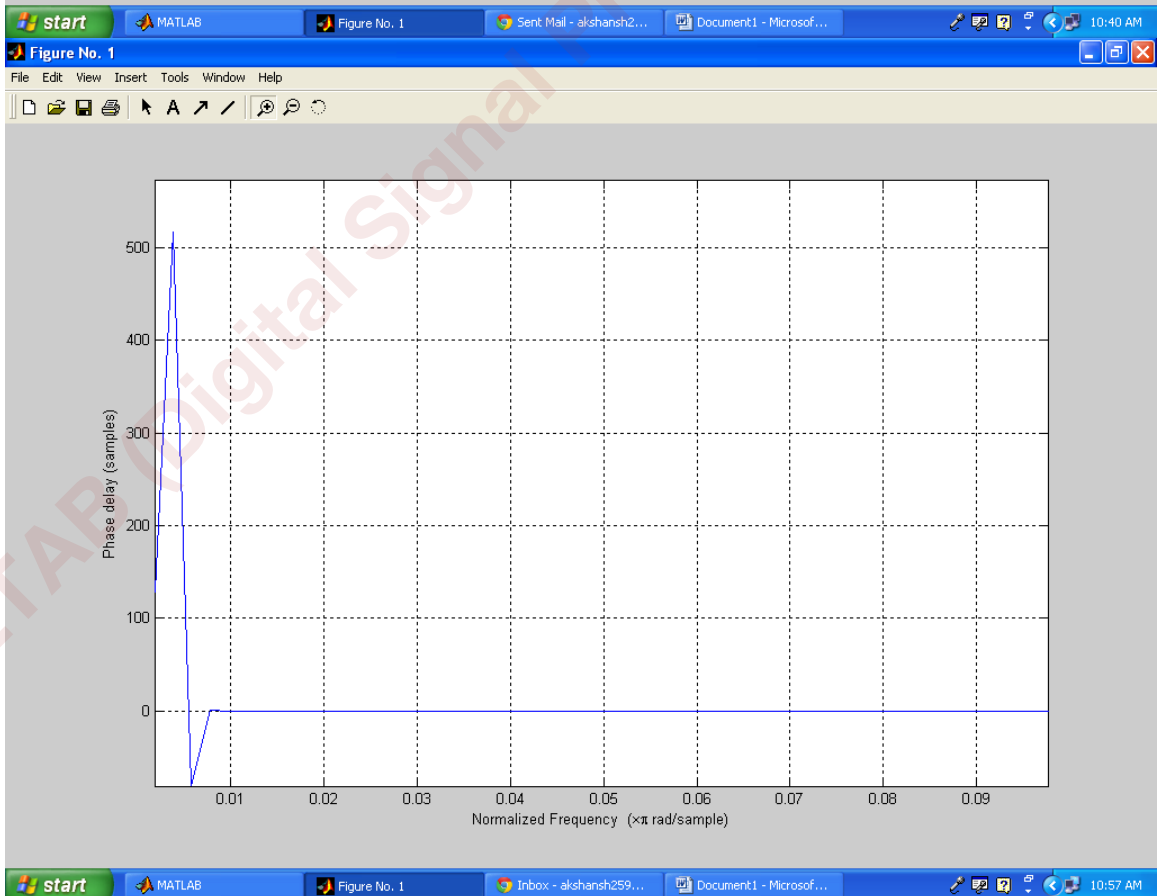
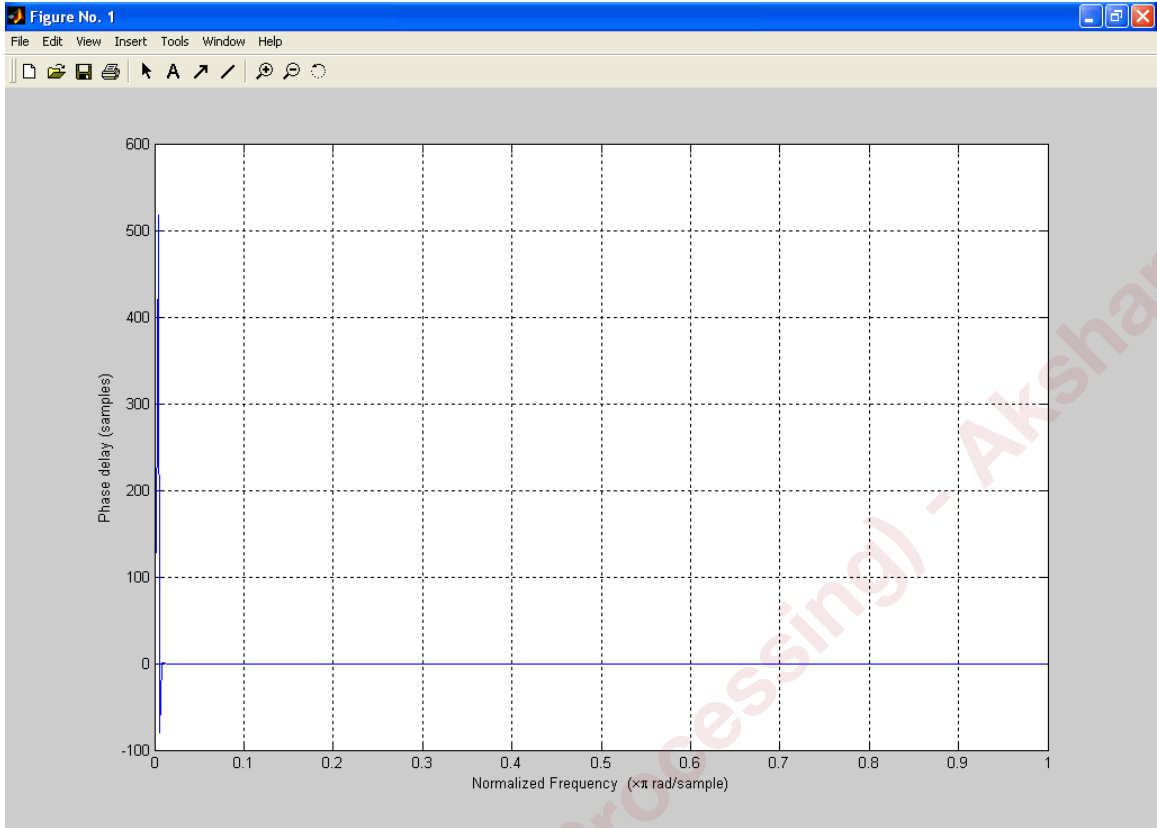
(a) Magnitude Plot

```
>> [H,F]=freqz(B1,A1,512,Fs)
>> plot(F,20*log10(abs(H)))
>> ylabel('magnitude response in dB')
>> xlabel('freq in Hz')
```



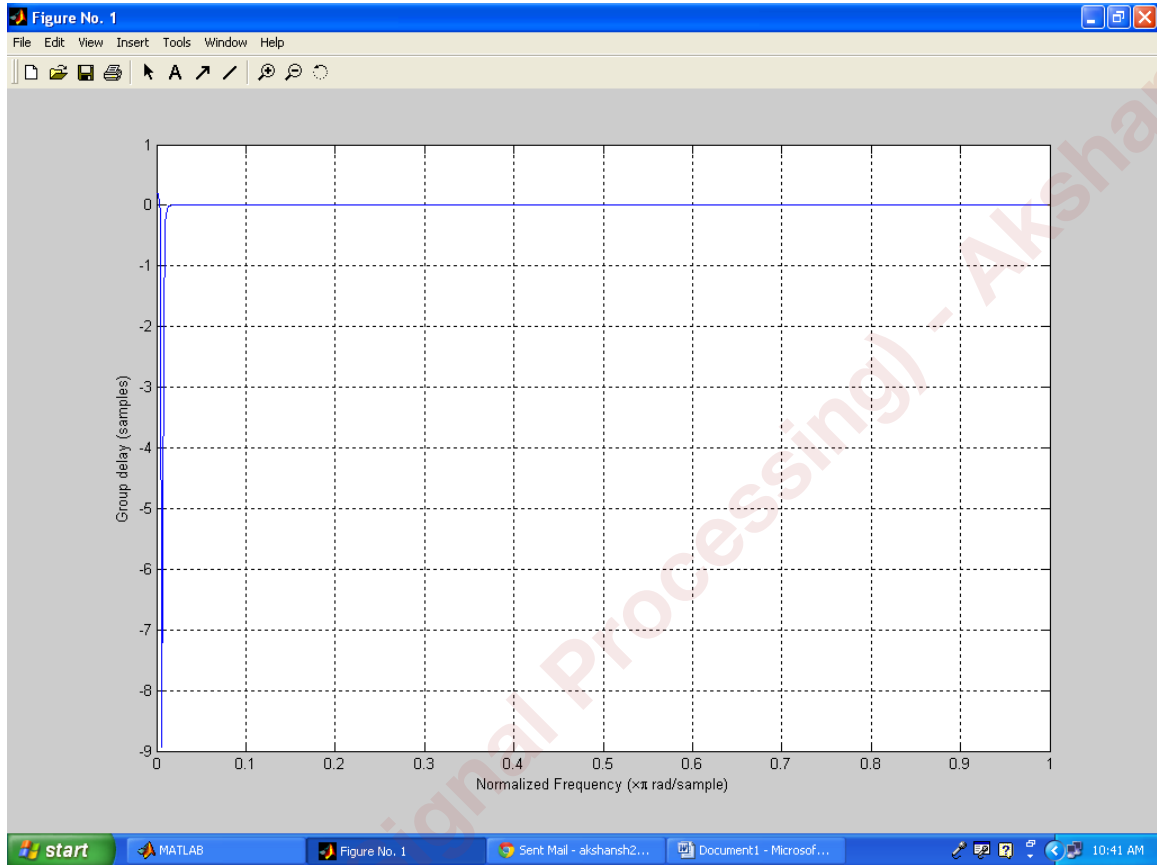
(b.) Phase Plot

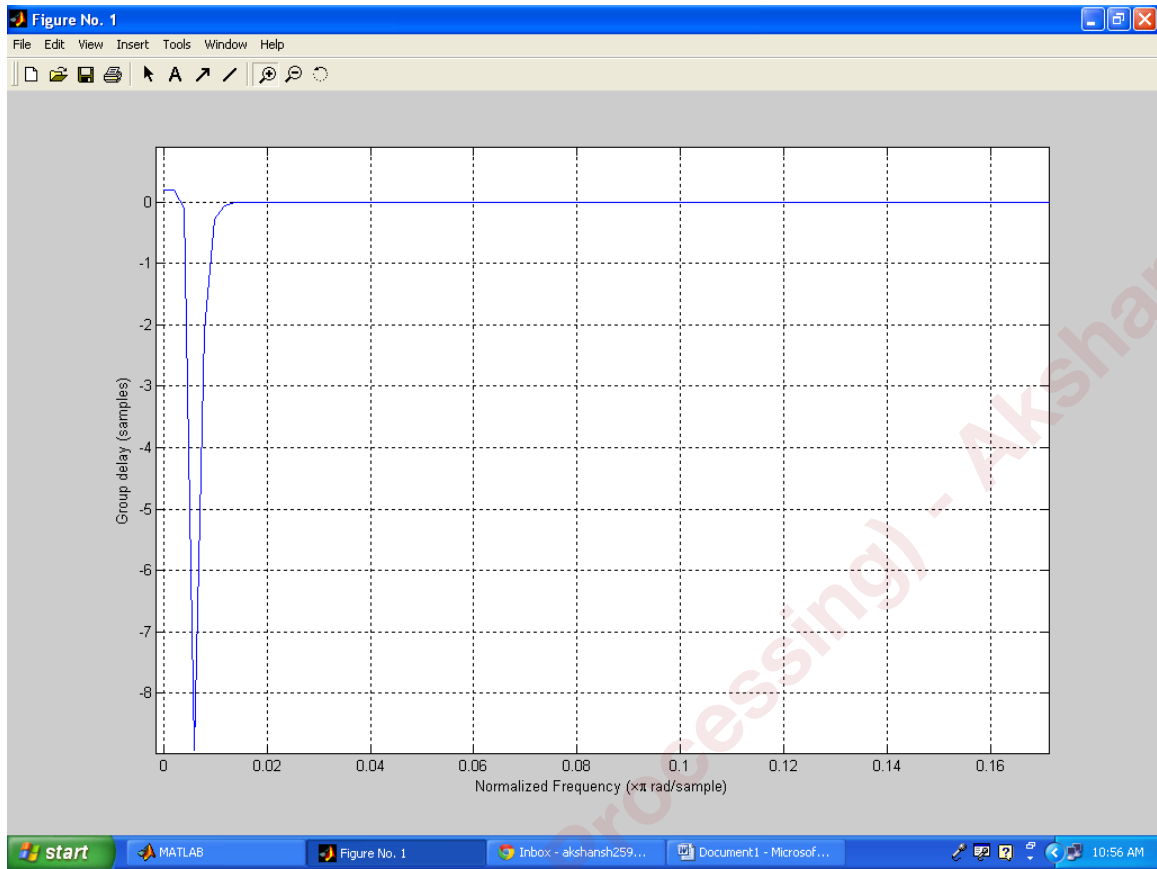
```
>> phasedelay(b1,a1,512)
>>
```



(c.) Group Delay

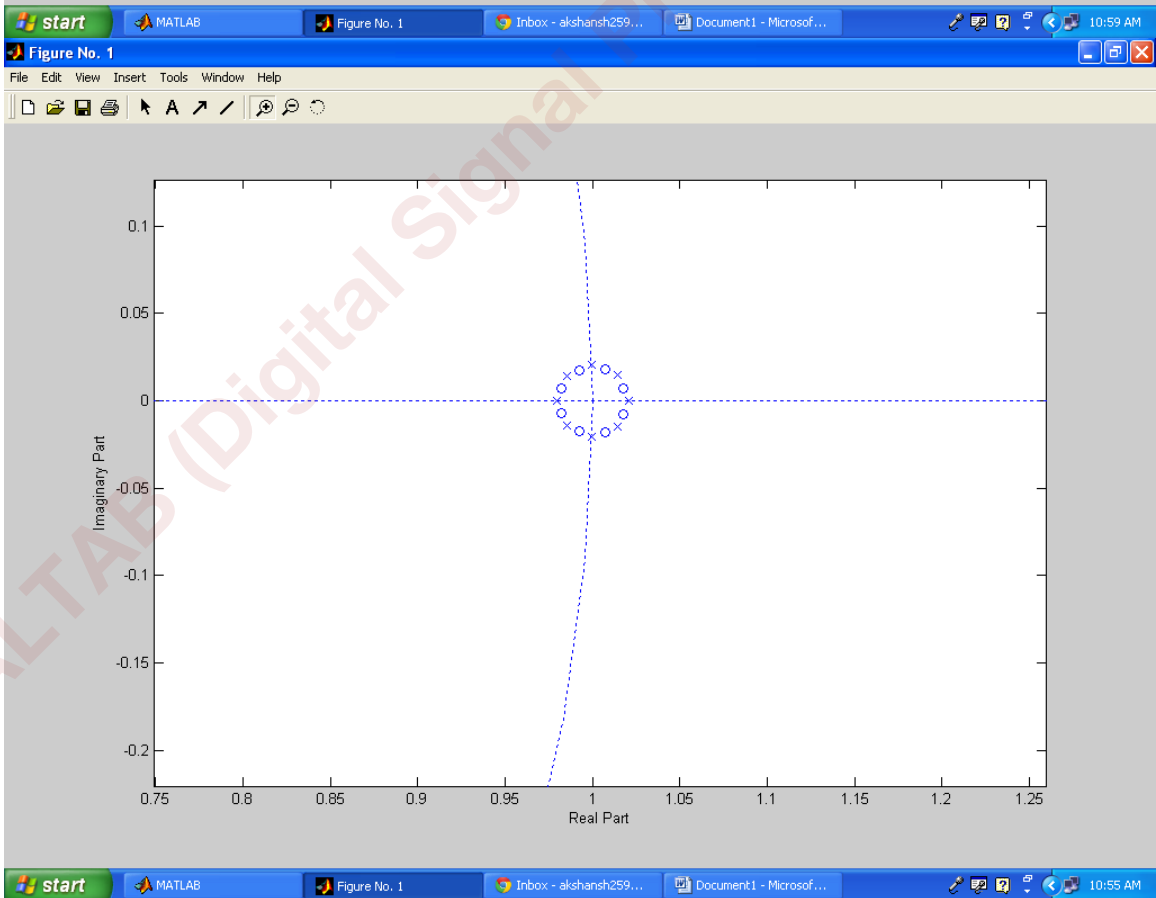
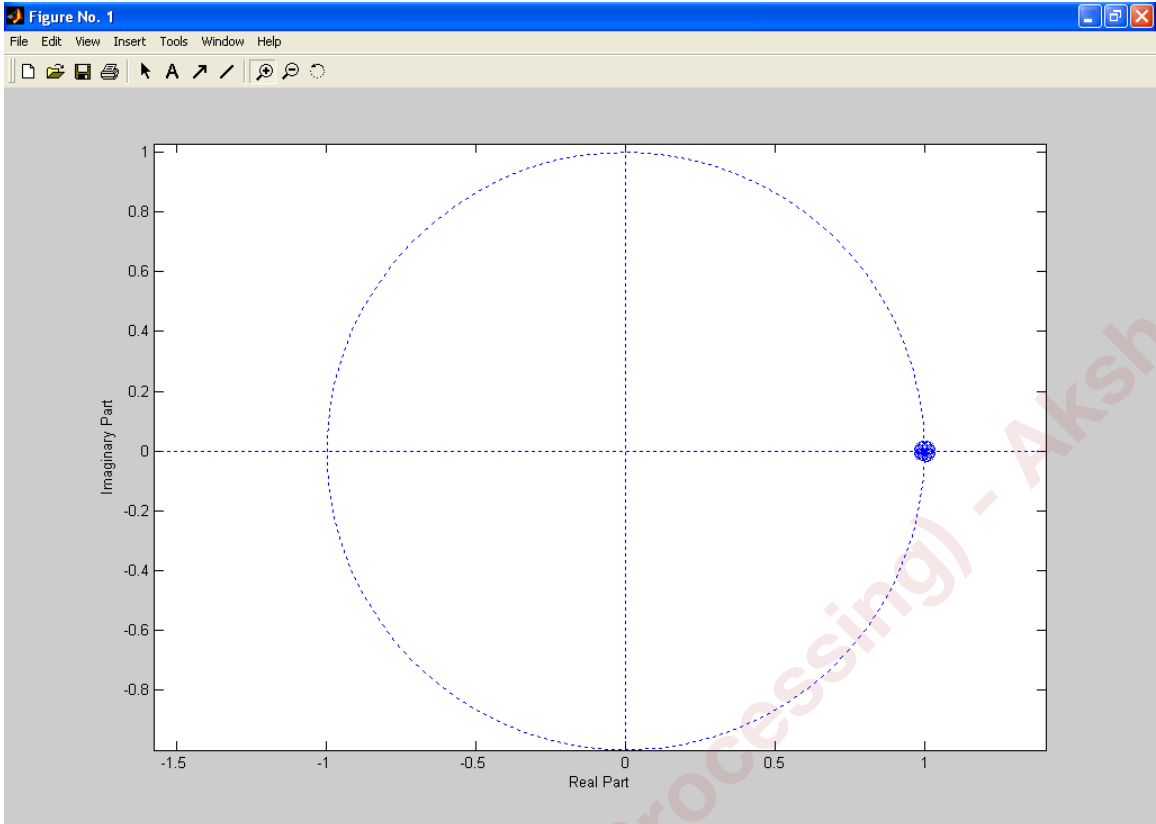
```
>> grpdelay(b1,a1,512)
```





(d.) Pole Zero Plot

```
>> zplane(b1,a1)
```



Showing that we have Band Stop Filter

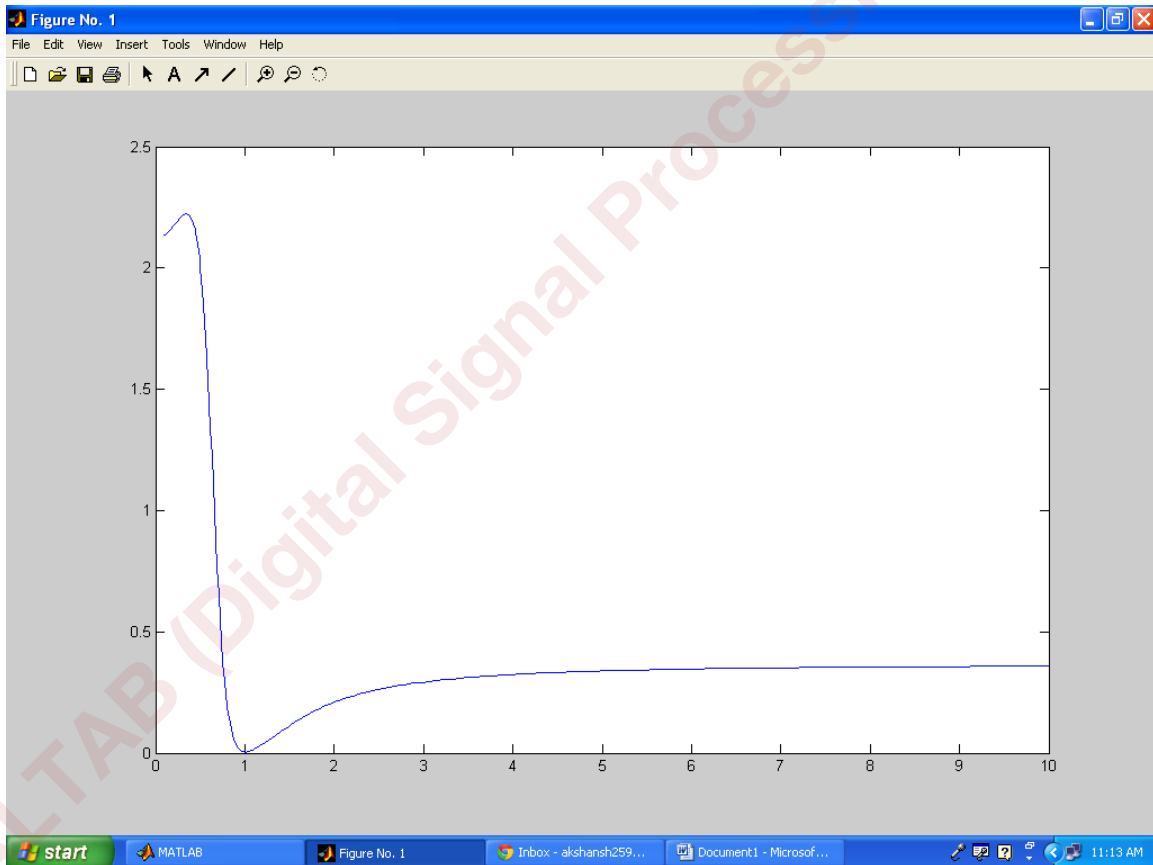
(Seeing in s domain)

```
>> [N1,Wn1]=ellipord(Wp,Ws,Rp,Rs,'s')
```

```
>> [B1,A1]=ellip(N1,Rp,Rs,Wn1,'stop')
```

```
>> [H,F]=freqs(B1,A1)
```

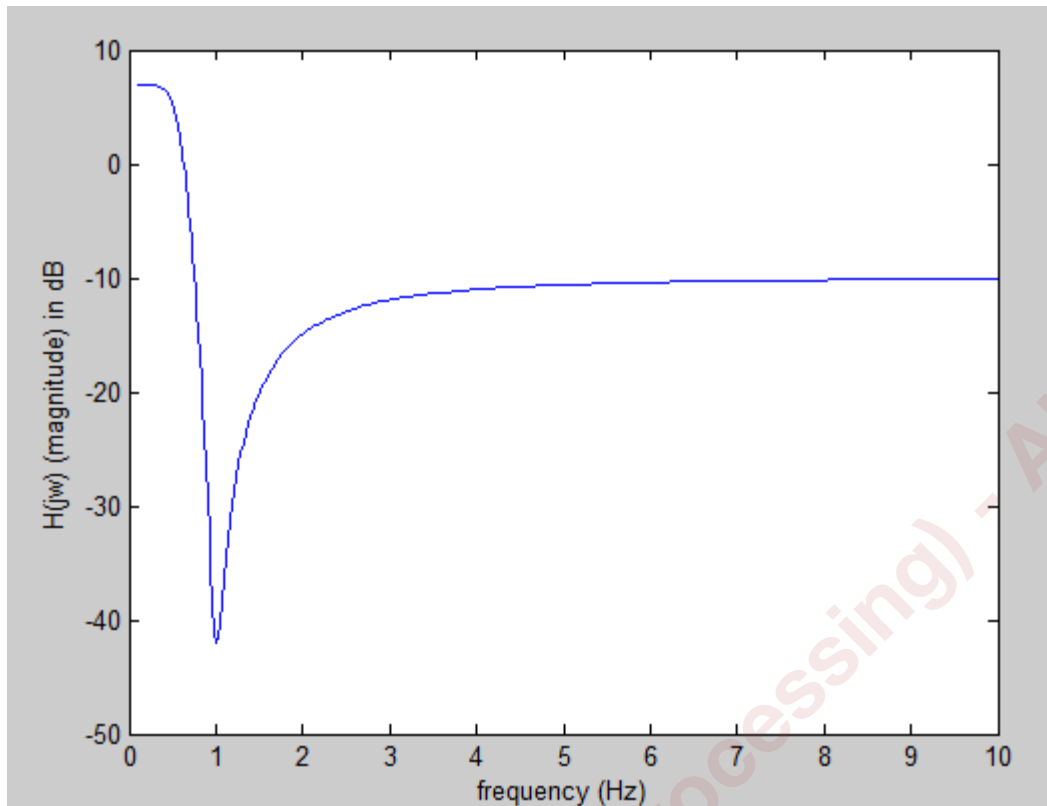
```
>> plot(F,abs(H))
```



```
>> plot(F, 20*log10(abs(H)))
```

```
>> ylabel('H(jw) (magnitude) in dB')
```

```
>> xlabel('frequency (Hz)')
```



The figure shows the magnitude plot for elliptical filter with the given specifications in the ANALOG DOMAIN.

From the figure, it is visible that it's a band stop filter.

Conclusion

In the analog domain, the sampling interval is from 0 to infinity.

But, as we change it to the digital domain, the sampling interval changes from 0 to the sampling frequency. Basically, this reduces the sampling interval, or, in a way, compresses it.

In such a condition, we find distortion in the magnitude, phase, group and phase delay plots.

This effect is called as **Nyquist effect**.

Matlab Assignment 4

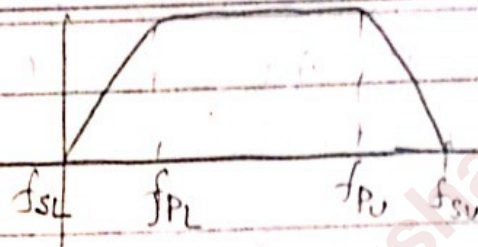
Digital Signal Processing

Q. 7.28 (i) Assignment 4

(1) Doing on paper

We are given $f_{PL} = 200 \text{ Hz}$

$f_s = 2000 \text{ Hz}$; $f_{su} = 500 \text{ Hz}$



Now f can't be -ve. So, assume $f_{SL} = 0 \text{ Hz}$

Hence, Transⁿ width = $f_{PL} - f_{SL} = 200 \text{ Hz}$

So, $f_{su} - f_{pu} = 200 \text{ Hz}$

$$\Rightarrow 500 - f_{pu} = 200 \text{ Hz}$$

$$\Rightarrow f_{pu} = 300 \text{ Hz}$$

So,

let $f_{c1} = \frac{(200-100)}{2000} \text{ Hz}$ & $f_{c2} = \frac{(300+100)}{2000} \text{ Hz}$

Smearing effect

Given Bandpass filter, so,

Normalizing wrt f_c

$$h_D(n) = \begin{cases} \frac{2f_2 \sin(n\omega_2)}{n\omega_2} - \frac{2f_1 \sin(n\omega_1)}{n\omega_1} & ; n \neq 0 \\ 2(f_2 - f_1) & ; n = 0 \end{cases}$$

&, for hamming window,

$$w(n) = 0.54 + 0.46 \cos\left(\frac{2\pi n}{N}\right)$$

Now, finding coefficients,

$$h(n) = h_D(n) \times w(n)$$

for 7 point, $n = 0, 1, 2, 3$

(\because its symmetric)
So don't find for 4, 5, 6

$$\left. \begin{array}{l} h(0) = h(6) \\ h(1) = h(5) \\ h(2) = h(4) \\ h(3) = h(3) \end{array} \right\}$$

for $n=0$

$$h_D(0) = 2 \left(\frac{300+100}{2000} - \frac{200-100}{2000} \right) = h_D(6)$$

$$w(0) = 0.54 + 0.46(1) = 1 = w(6)$$

Now

$$h(0) = h_D(0) \times w(0) = h(6)$$

So, lly, find all coeff.

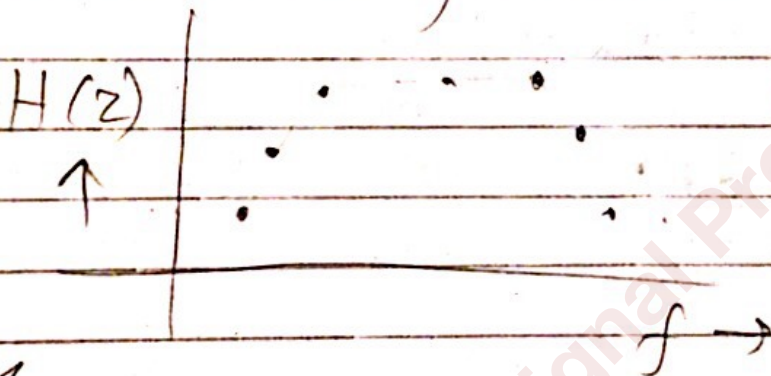
Taking Z transform of $h(n)$, we get $H(z)$ values. Now, we have $\omega(0) \dots \omega(6)$
 We know

$$\omega = 2\pi f$$

So, $f(0) \dots f(6)$, ✓

Now, plot for

$H(z)$ vs f values.

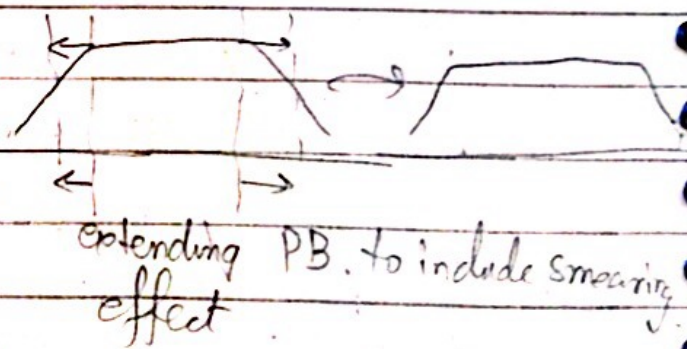


We should get something like this

★ Smearing effect

$$\Delta f = \text{Trans}^n \text{ width} = 200$$

$$\frac{\Delta f}{2} = \frac{1}{2} (T\omega) = \frac{200}{2} = 100$$



$$f_{c1})_{\text{new}} = 200 - \frac{\Delta f}{2} = 100$$

$$f_{c2})_{\text{new}} = 300 + \frac{\Delta f}{2} = 400,$$

② Doing in MATLAB

```
fs = 2000;           % sampling freq  
fn = fs/2;           % Nyquist freq  
N = 7
```

```
fc1 = 300/fn;
```

```
fc2 = 400/fn;
```

```
FC = [fc1 fc2];
```

```
hn = fir1(N-1, FC, 'hamming(N)');
```

```
[H, f] = freqz(hn, 1, 512 * fs);
```

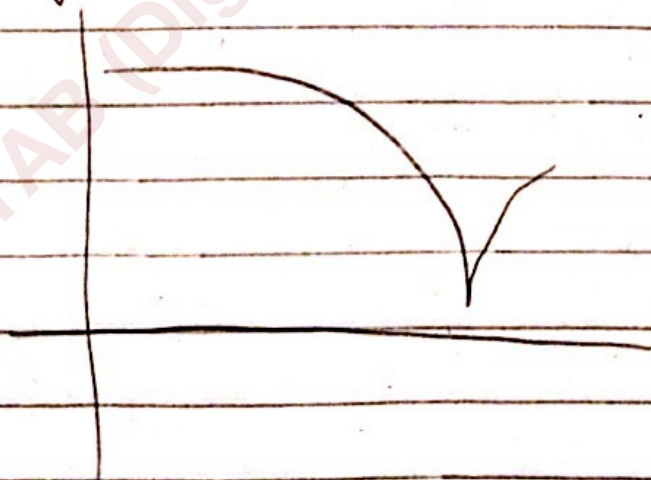
```
mag = 20 * log10(abs(H));
```

```
plot(f, mag), grid on
```

```
xlabel('Freq. (Hz)');
```

```
ylabel('Magnitude Response (dB)');
```

Using this, we get a graph



Corresponding to
 $N = 7$.

Now, changing N.

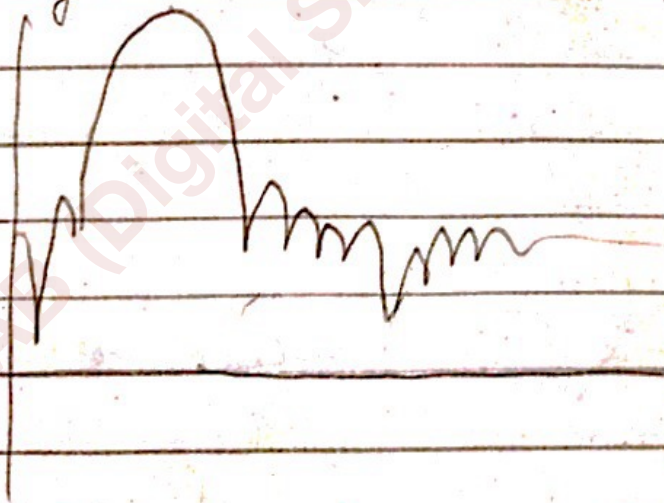
we have $\Delta f = \text{frame}^n \text{ width} = 200$.

$$\Delta f = \frac{3.3}{N} = \frac{200}{2000}$$

$\frac{200}{2000}$
SS \rightarrow Sampling freq.

$$\Rightarrow N = \frac{3.3}{200} \times 2000 = 33$$

So, Using same commands for $N=33$,
we get



Band pass ✓

Extra:

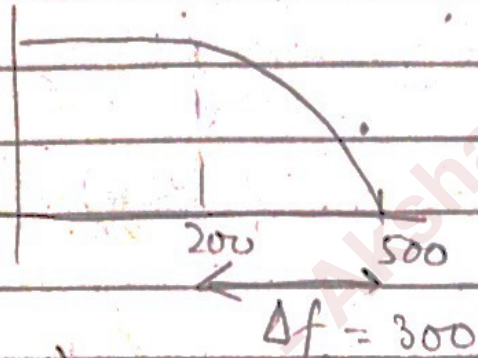
Assuming low Pass from given specs

$$f_s = 2000;$$

$$N = 7;$$

$$f_n = f_s/2;$$

$$f_c = \frac{450}{1000};$$



$h_n = \text{fir1}(N-1, f_c, \text{hamming}(N));$ So, including smearing effects

$$[H, f] = \text{freqz}$$

$$(h_n, 1, 512, f_s);$$

$$\text{mag} = 20 \log_{10}(\text{abs}(H));$$

$$f_c = (f_{c1} + f_{c2}) = \frac{\Delta f + \Delta f}{2}$$

new passband

$$f_s/2$$

$$= \frac{300 + 150}{2000/2}$$

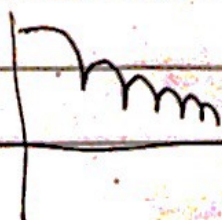
$$\Rightarrow f_c = \frac{450}{1000}$$

$$\text{So, } N = \frac{3.3}{300} \times 2000 = 22$$

$\text{plot}(f, \text{mag}); \text{grid on};$
we get
for $N = 7$ $N = 8$



for $N = 22$



Q. 7.29 given $N = 41$

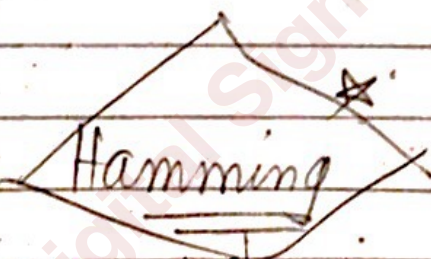
$$H(f) = \begin{cases} 1 & f \in [2 \text{ kHz}, 4 \text{ kHz}] \\ 0 & \text{otherwise} \end{cases}$$

↓

$$\begin{aligned} f_{P1} &= 2000 \text{ Hz} \\ f_{P2} &= 4000 \text{ Hz} \end{aligned} \left\{ \begin{array}{l} \text{without including} \\ \text{normalization} \\ \text{smearing effect} \end{array} \right.$$

Assume sampling freq = 10 kHz
(not given)

Now,

Case (1) :-  Hamming

$$\text{So, } \Delta f \Big|_{\text{normalised}} = \frac{3.3}{N} = \frac{3.3}{41} = 0.0804$$

$$\& \Delta f \Big|_{\text{denormalised}} = 0.0804 \times 10 \text{ kHz} \approx 804 \text{ Hz}$$

$$\text{So, } \frac{\Delta f}{2} = 402 \text{ Hz}$$

Now, including normalizⁿ & smearing effect?

Taking Nyquist effect

$$f_{p1} = \frac{2000 - 402}{(10000/2)} = 0.3196$$
$$f_{p2} = \frac{4000 + 402}{(10000/2)} = 0.8804$$

Now, plotting for BP, using commands

$$f_s = 10000;$$

$$N = 41;$$

$$f_{p1} = 0.3196$$

$$f_{p2} = 0.8804$$

$$f_p = [f_{p1} \ f_{p2}];$$

$$h_n = \text{fir4}(N-1, f_p, \text{hamming}(N));$$

$$[H, f] = \text{freqz}(h_n, 1, 512, f_s);$$

$$\text{mag} = 20 \cdot \log_{10}(\text{abs}(H));$$

$$\text{plot}(f, \text{mag}, 'magenta'); \text{grid on};$$

Case (2) :- Rectangular

$$\Delta f / \text{normalised} = \frac{0.9}{N} = \frac{0.9}{41} = 0.02195$$

$$\Delta f / \text{denormalised} = \frac{0.9}{41} \times 10000 = 219.512$$

$$\frac{\Delta f}{2} = 109.756$$

So, including normalisation & smearing effect

$$f_{c1} = \frac{2000 - 109.756}{(10000/2)} = 0.37804$$

$$f_{c2} = \frac{4000 + 109.756}{(10000/2)} = 0.81756 \rightarrow \text{Taking Nyquist effect}$$

Now, plotting BP using commands;

$$f_s = 10000;$$

$$N = 41$$



↓

$$f_{c1} = 0.37804$$

$$f_{c2} = 0.81756$$

$$f_c = [f_{c1} \ f_{c2}];$$

$$h_{n2} = \text{fir1}(N-1, f_c, \text{rectwin}(N));$$

$$[H2, f2] = \text{freqz}(h_{n2}, 1, 512, fs);$$

$$\text{mag2} = 20 * \log_{10}(\text{abs}(H2));$$

$$\text{plot}(f2, \text{mag2}, 'green'); \text{grid on};$$

Assignment 4

MATLAB problems

7.28 Use MATLAB to compute the coefficients, plot the magnitude–frequency response in dB, and determine the locations of the zeros of each of the following window-based filters (assume a sampling frequency of 2 kHz and a Hamming window function):

- (1) A 7-point, bandpass FIR filter with pass- and stopband edge frequencies of 200 Hz and 500 Hz.
- (2) An 8-point, bandpass FIR filter with pass- and stopband edge frequencies of 200 Hz and 500 Hz.

In the given problem, it has been told that the pass band frequency is given as 200 Hz and stop band frequency is given as 500 Hz.

Now, as it's told to design a band pass filter, are left to assume it as:

- a. A low pass filter with pass band edge frequency of 200 Hz and stop band edge frequency of 500 Hz
- b. A band pass filter with lower stop band frequency of 0 Hz, lower pass band frequency of 200 Hz and upper stop band frequency of 500 Hz.

Note: it is left to the designer to choose how to design the filter using the specs given.

Now, assuming the case, b. we assume:

$W_{sl} = 0$ Hz

$W_{pl} = 200$ Hz

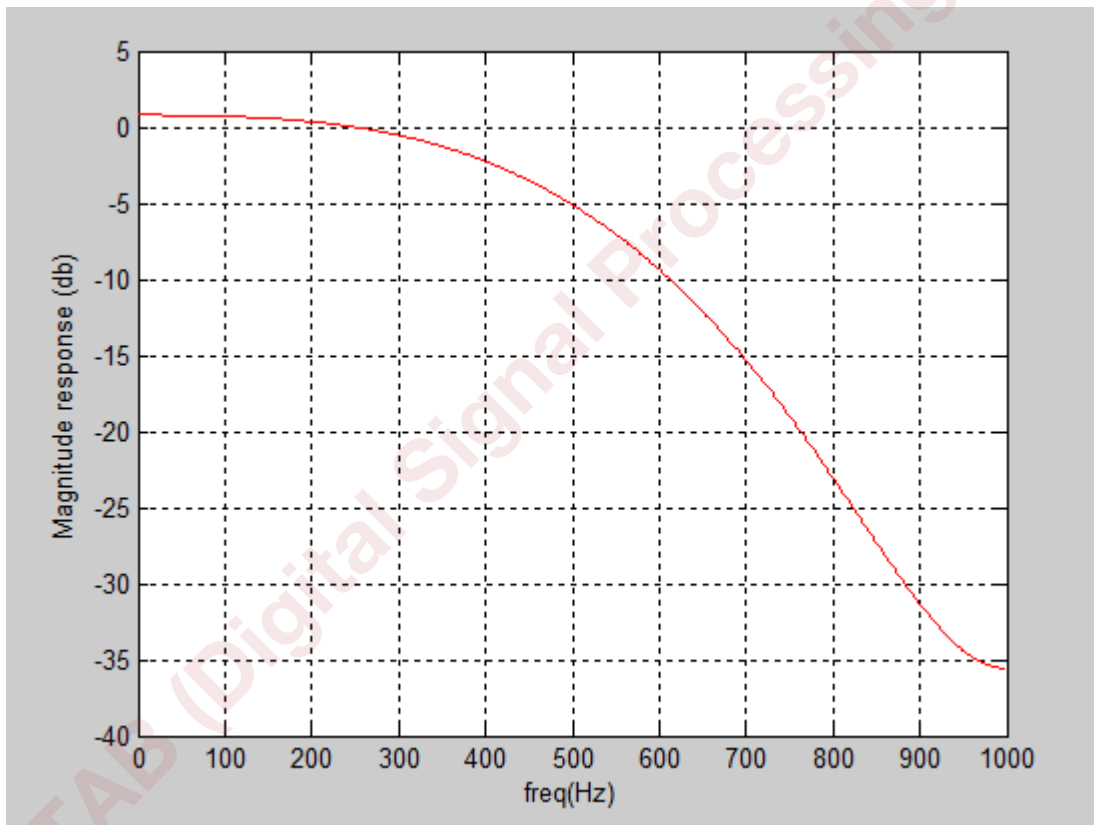
That means, the transition width ($W_{pl} - W_{sl}$) = Δf (denormalised) = 200 Hz

$W_{su} = 500$ Hz

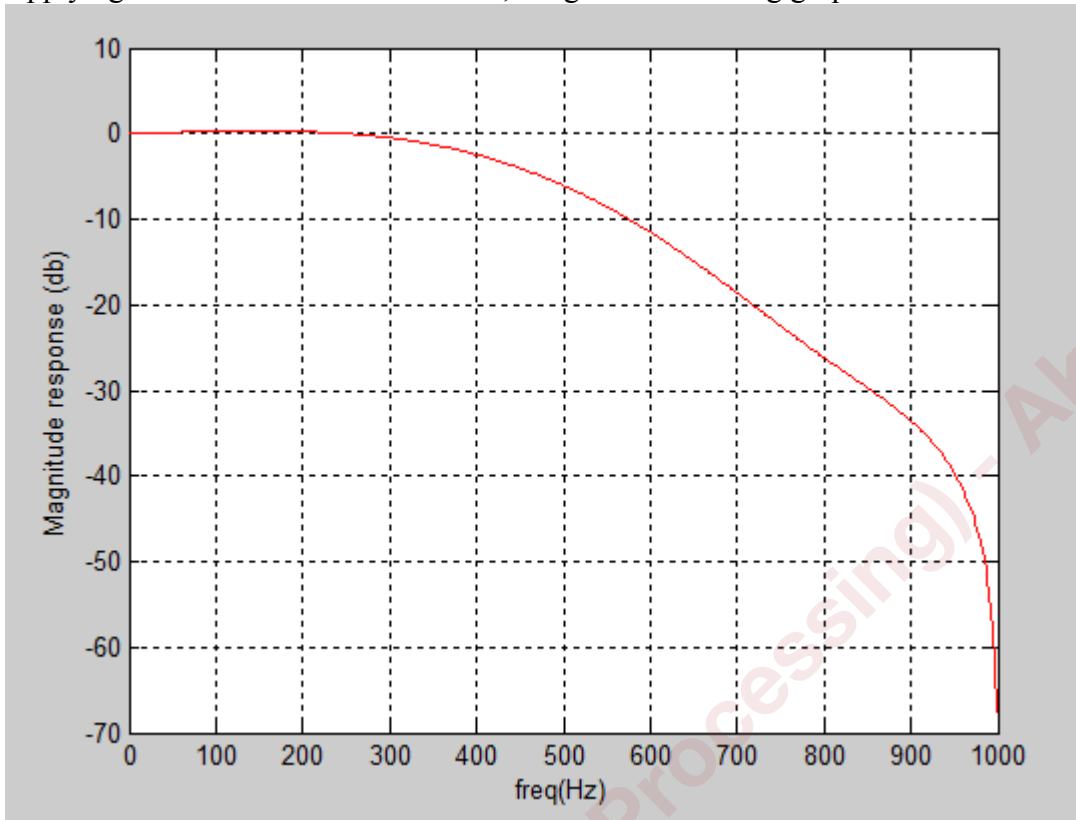
So, $W_{pu} = W_{su} - 200$ Hz = 300 Hz

Commands:

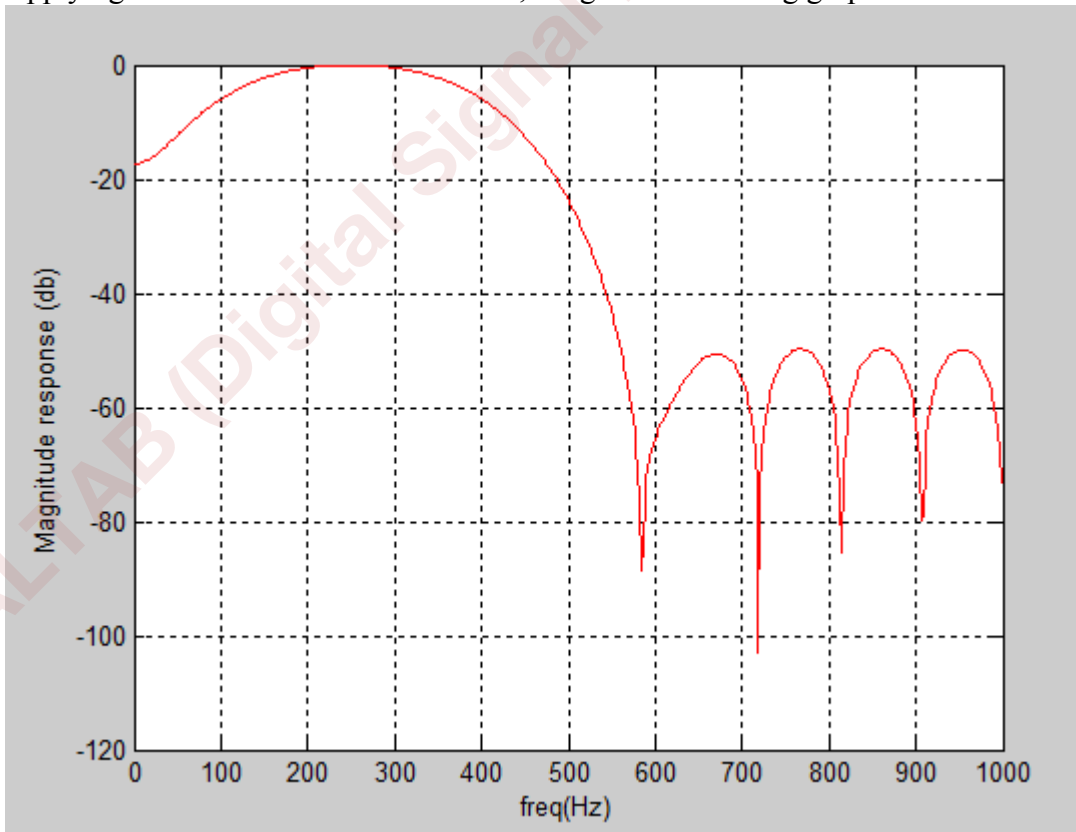
```
>> fs=2000;
>> fn=fs/2; % fn= Nyquist freq.
>> N=7;
>> fc1=100/fn; % 100, as its Wpl - (delta f/2); and /fn, as normalising w.r.t nyquist
>> fc2=400/fn; % 400, as its Wpu + (delta f/2)
>> FC=[fc1 fc2];
>> hn=fir1(N-1, FC, hamming(N));
>> [H,f]=freqz(hn, 1,512,fs);
>> mag=20*log10(abs(H));
>> plot(f,mag,'red');
grid on;
xlabel('freq(Hz)')
>> ylabel('Magnitude response (db)')
>>
```



Applying the same commands for $N=8$, we get the following graph



Applying the same commands for $N=22$, we get the following graph



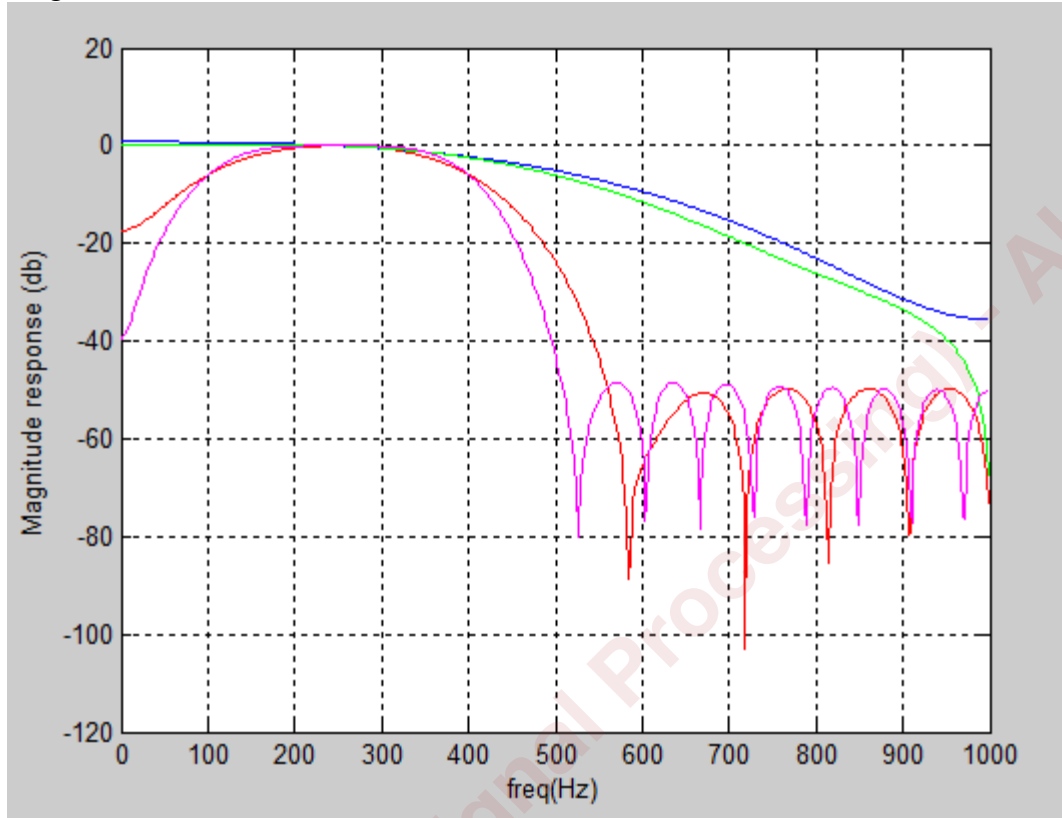
Proceeding similarly and then, holding all the graphs together, we see:

Blue: $N=7$

Green: $N=8$

Red: $N=22$

Magenta: $N=33$



Note: finding N by using Δf formula for hamming window

$\Delta f = 3.3/N$

Where $\Delta f = 200/f_s$

Using this, we get $N=33$

7.29 A 41-point bandpass FIR filter is to be designed to approximate the following ideal magnitude response characteristics using the window method:

$$H(f) = \begin{cases} 1 & 2 \text{ kHz} \leq f \leq 4 \text{ kHz} \\ 0 & \text{otherwise} \end{cases}$$

Determine the impulse response coefficients of the filter and plot its magnitude and phase frequency responses with the aid of MATLAB for each of the following cases:

- (1) Using a rectangular window.
- (2) Using a Hamming window.

Clearly, here $f_{p1}=2\text{kHz}$ and $f_{pu}=4\text{kHz}$.

For the given problem, assume the sampling frequency as 10kHz , as its not mentioned.

(We know that for denormalizing using Nyquist theorem, we have to divide the frequencies by $(f_s/2)$, where f_s is the sampling frequency.

Also, the sampling frequency should be greater than 4kHz .)

For hamming window

$N=41$;

```
>> fp1=0.3196; % value got after normalizing it w.r.t Nyquist, and using smearing effect
```

```
>> fp2=0.8804;
```

```
>> fs=10000;
```

```
>> fp=[fp1 fp2];
```

```
>> hn=fir1(N-1,fp,hamming(N));
```

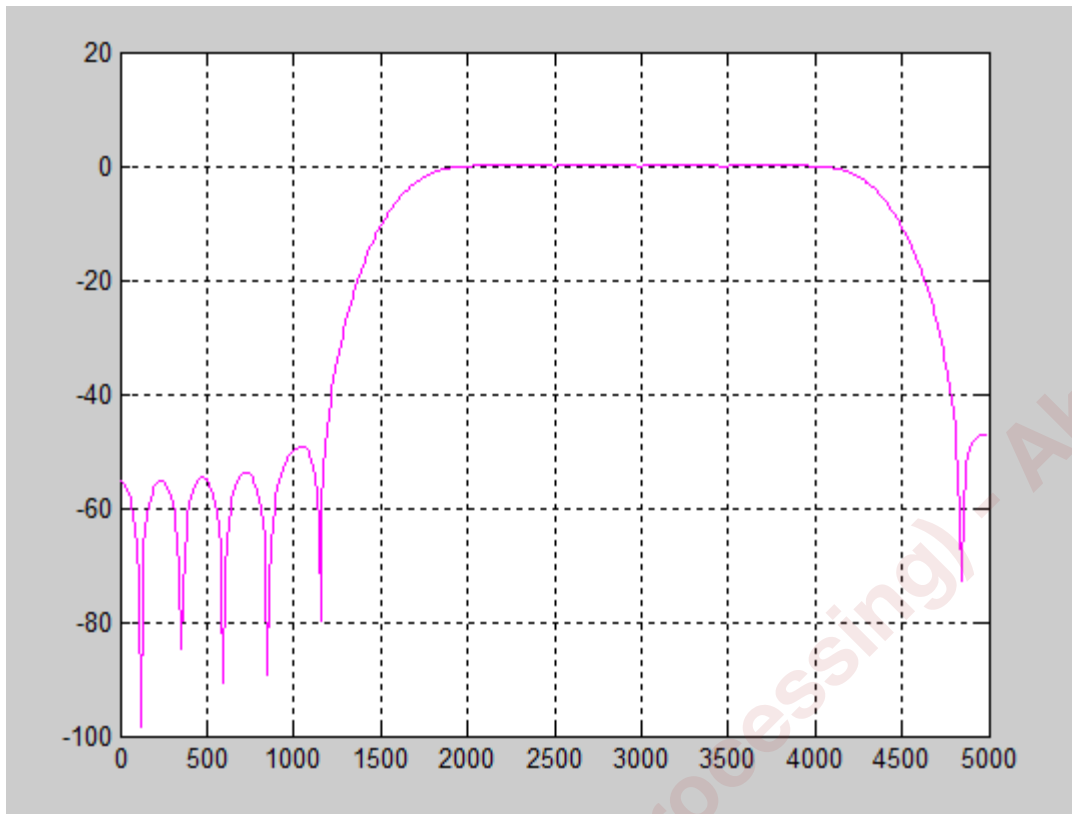
```
>> hn=fir1(N-1,fp,hamming(N));
```

```
>> [H,f]=freqz(hn,1,512,fs);
```

```
>> mag=20*log10(abs(H));
```

```
>> plot(f,mag,'magenta'); grid on;
```

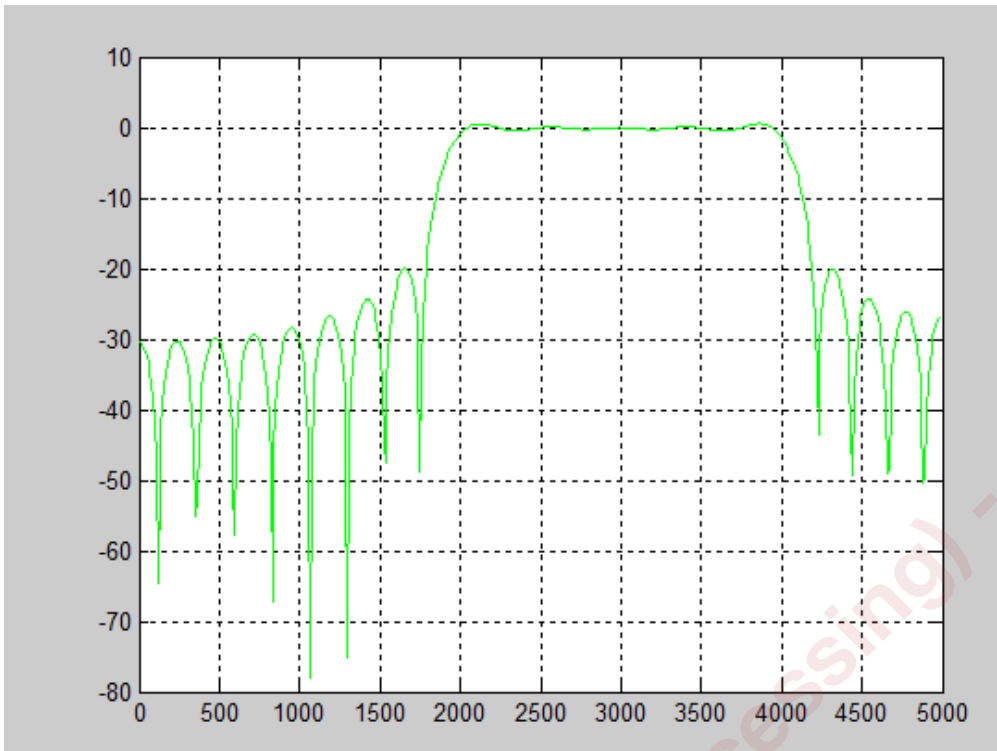
```
>>
```

Clearly, it is visible that the pass band is between 2000 to 5000 Hz (nearly)

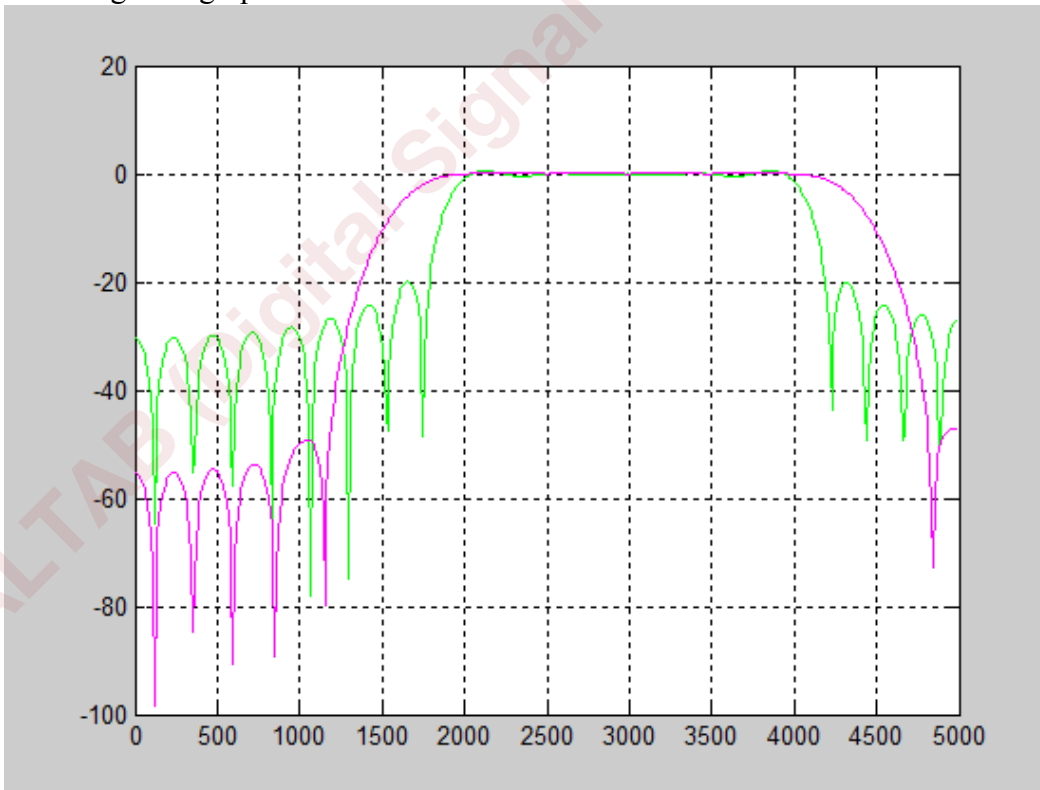
For rectangular window

```
>> fc1=0.37804;
>> fc2=0.81756;
>> fc=[fc1 fc2];
>> hn2=fir1(N-1,fc,rectwin(N));
>> [H2,f2]=freqz(hn2,1,512,fs);
>> mag2=20*log10(abs(H2));
>> plot(f2,mag2,'green');grid on;
```



It is also having pass band in 2000 to 5000 Hz.

Including both graphs –



Inference:

It can be clearly seen that increasing the no. of samples (N) makes the frequency response more ideal.

Moreover, the graph compresses as N is increased.

MALTA B (Digital Signal Processing) - Akshansh

Matlab Assignment 5

Digital Signal Processing

DSP - MATLAB

Assignment - 5

Teacher : Q. 7.30

LPF

Given :- $N = 21$

$$\left. \begin{array}{l} f_p = 2 \text{ kHz} \\ f_c = 3 \text{ kHz} \\ f_s = 10 \text{ kHz} \end{array} \right\} \Rightarrow \text{TW} = \Delta f = 1 \text{ kHz}$$

Idea : Finding FIR filter coeff. use 'remez' command.

Syntax :-

$$b = \text{remez}(N-1, F, M)$$

N : filter length.

F : Vector of normalised band edge freqs.

M : " of desired magnitude response of filter

If weight is specified,

$$b = \text{remez}(N-1, F, M, WT)$$

→ vector.

First, normalise given freq (wrt Nyquist freq)

i.e.,

0 - 2 kHz	PB
2 - 3 kHz	Trans ⁿ
3 - 10 kHz	SB

$$F = \begin{pmatrix} 0 & 2000 & 3000 & 10000 \\ 10000/2 & 10000/2 & 10000/2 & 10000/2 \end{pmatrix}$$

$$\text{So, } F = [0, 0.4, 0.6, 1]$$

$N = 21$:- % telling no. of filters

$$F_s = 10000$$

Now, For ideal LPF, the magnitude is $1 \rightarrow$ PB
 $0 \rightarrow$ Transⁿ
 $0 \rightarrow$ SB

So,

$$M = [1 \ 1 \ 0 \ 0]$$

Now, computing filter coeff,

$$b = \text{remez}(N-1, F, M);$$

Computing freq. response :-

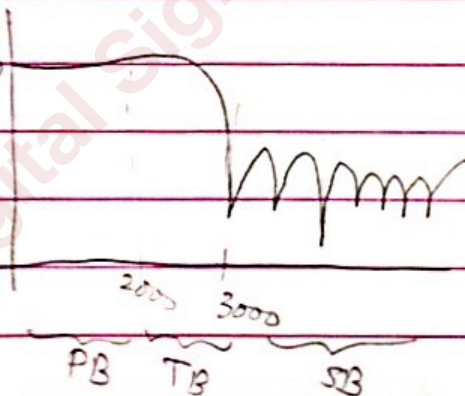
$$[H, f] = \text{freqz}(b, 1, 512, Fc)$$

Plotting freq. response in dB.

✓ % for Magnitude response

$$\text{plot}(f, 20 * \log_{10}(\text{abs}(H)));$$

we get :-



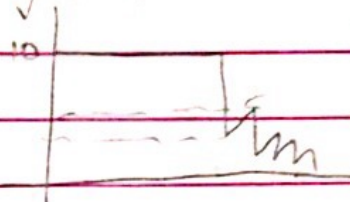
Now, use the command for finding all plots:
 % numerator coeff.

$$\text{fvtool}(b, 1);$$

% den. eqⁿ is not there for FIR

It displays separate buttons & plots

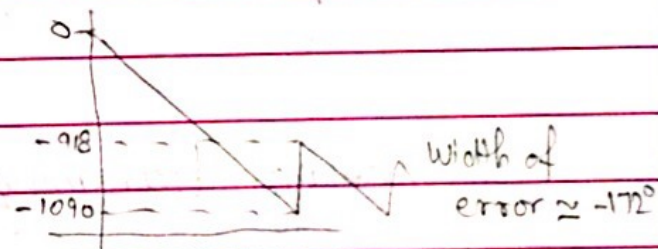
✓ For finding phase delay,
 >> phase delay (b, 1, 512)
 We get



✓ Seeing impulse response :-
 Command : `impz(b)`;

✓ Pole zero plot (z-domain)
`zplane(b, 1)`
 (s-domain)
`pzmap(b, X)`
 $X = [0 \ 0 \ \dots \ 1]$

✓ Phase response
`phasez(b, 1)`



✓ Group delay
`grpdelay(b, 1, 512)`

MATLAB Assignment 6

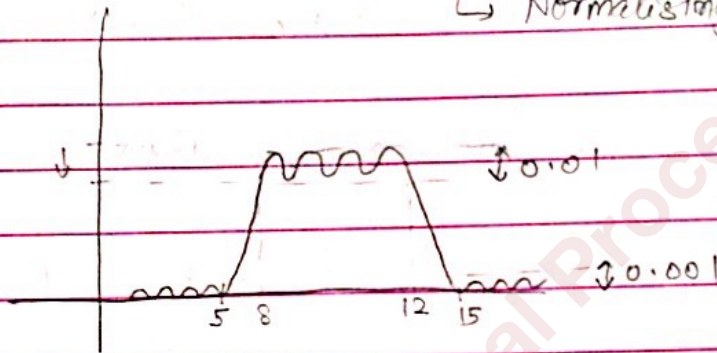
Digital Signal Processing

DSP LAB

Assignment - 6

Q. 7.32 * Given a linear phase FIR BANDPASS filter
 with:
 passband 8 - 12 kHz
 SB ripple 0.001
 PB ripple 0.01
 f_s 48 kHz
 $\Delta f =$ Transⁿ width 3 kHz

↳ Normalising wrt Nyquist = $\frac{3}{48/2} = \frac{3}{24}$



(1) Using Hamming Window

$$\text{Trans}^n \text{ width} = \frac{3 \cdot 3}{N} \Rightarrow \frac{3 \cdot 3}{N} = \frac{3}{48} \quad \text{Normalising}$$

$$\Rightarrow N = 1.1 \times 48 = 52.8$$

So, n varies from -26 to 26.

Now, normalising all freq w.r.t Nyquist + including smearing effect

$$f_{SL} = \frac{5}{48/2}$$

$$f_{PL} = \frac{8}{48/2} - \frac{\Delta f}{2} = \frac{16}{48} - \frac{3}{48} = \frac{13}{48} ;$$

$$f_{PU} = \frac{12}{48/2} + \frac{\Delta f}{2} = \frac{24}{48} + \frac{3}{48} = \frac{27}{48} ;$$

$$f_{SU} = 15/48 ;$$

Now, the cut off freq. will be f_{PL} & f_{PU}
This can be entered in an array,

$$f_c = [f_{PL} \quad f_{PU}]$$

$$N = 53; \text{ (filter length)}$$

$$f_s = 48000;$$

For making truncated impulse response, $h_D(n)$,
use :-

$$h_D = \text{fir1}(N-1, f_c, \text{boxcar}(N));$$

The same formula in theory becomes

$$h_D(n) = \begin{cases} \frac{2f_2 \sin(n\omega_2) - 2f_1 \sin(n\omega_1)}{n\omega_2 - n\omega_1}, & n \neq 0 \\ 2(f_2 - f_1), & n = 0 \end{cases}$$

Now, finding $w(n)$

use :-

$$w(n) = \text{hamming}(N);$$

In theory, for hamming window, we use

$$w(n) = 0.54 + 0.46 \cos\left(\frac{2\pi n}{N}\right)$$

Now, finding coeff, $h(n)$

use :-

$$h(n) = \text{fir1}(N-1, f_c, w(n));$$

In theory, we do $h(n) = h_D(n) \times w(n)$
 $\forall n \in (0, N)$

→ Now, obtaining freq response
i.e., we have $h(\omega)$ values.
Find its dB values.

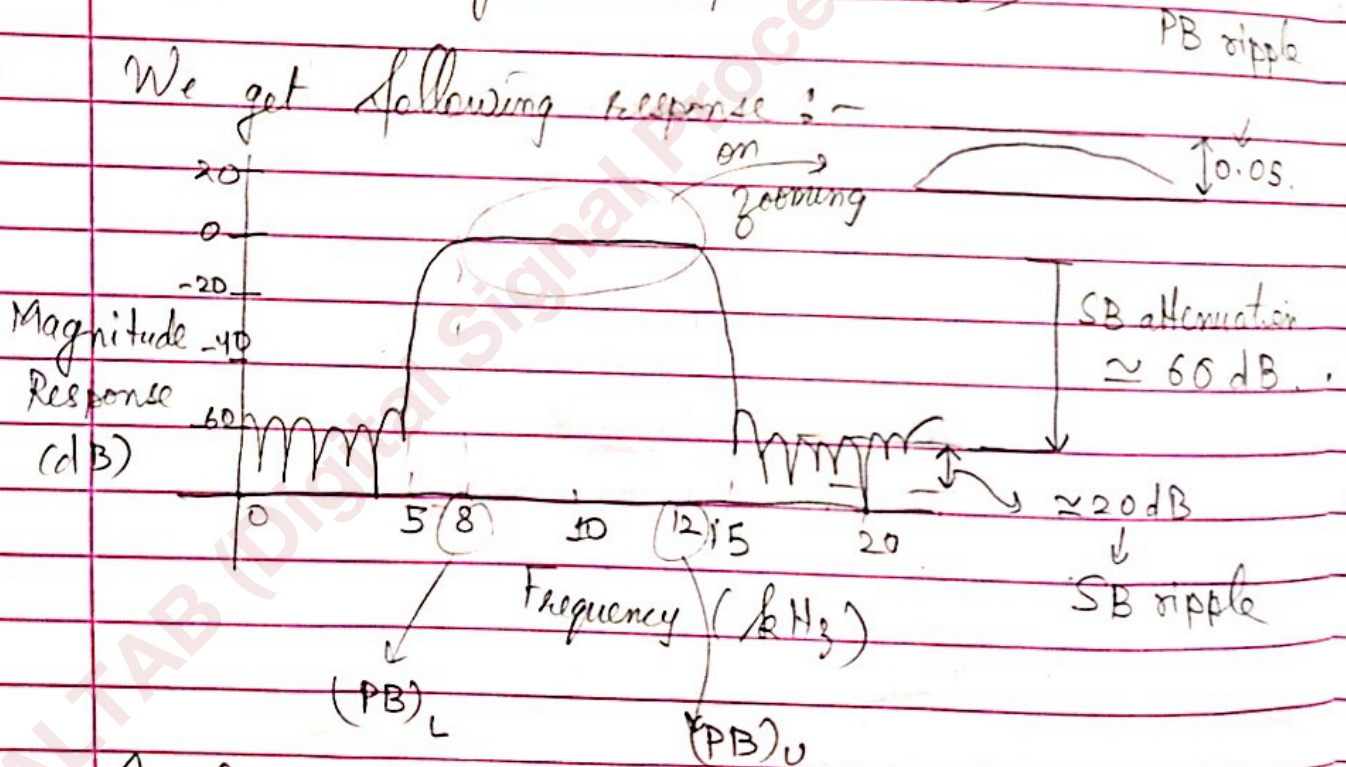
Now, find corresponding freq with these dB values.

Then, plot dB ($h(\omega)$) vs freq

Using MATLAB:

```
[H, f] = freqz(hn, 1, 512, fs);
mag = 20 * log10(abs(H));
plot(f, mag), grid on
xlabel('Frequency (Hz)');
ylabel('Magnitude Response (dB)');
```

We get following response :-



In theory, finding PB & SB ripples

PB : $20 \log(1 + S_p) = 0.01$, given.

So, $S_p \approx 0.008$. (We got 0.05)

& $20 \log(S_s) = 0.001$.

So, $S_s \approx 60$ dB

(we got ≈ 20 dB)

→ Now, finding impulse response,
use :-

$$\text{impz}(h_n, 1)$$

we get the values of coeff. at diff^r values
of n . ∴ center



Counting them, we find one coeff. in center
& 26 coeff. on either side of it. So,
53 coeff. implemented.

(2) Using Kaiser Window :-

SB attenuation as found before,

$$\text{from } S_c = 60 \text{ dB}$$

Now, for Kaiser window, for Attenuation(A) > 50

$$\beta = 0.1102(A - 8.7)$$

$$\& N \geq \frac{A - 7.95}{4.36 \Delta f}$$

Using this, we get $N \approx 58$.

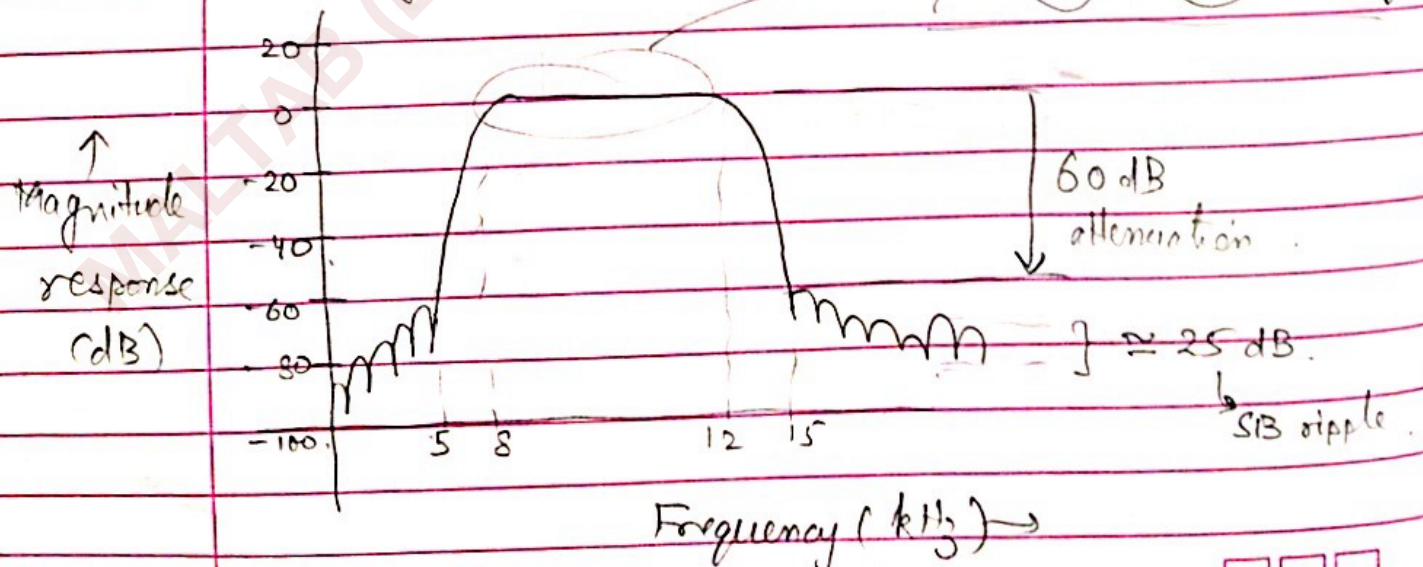
Now, continuing with same program,

```

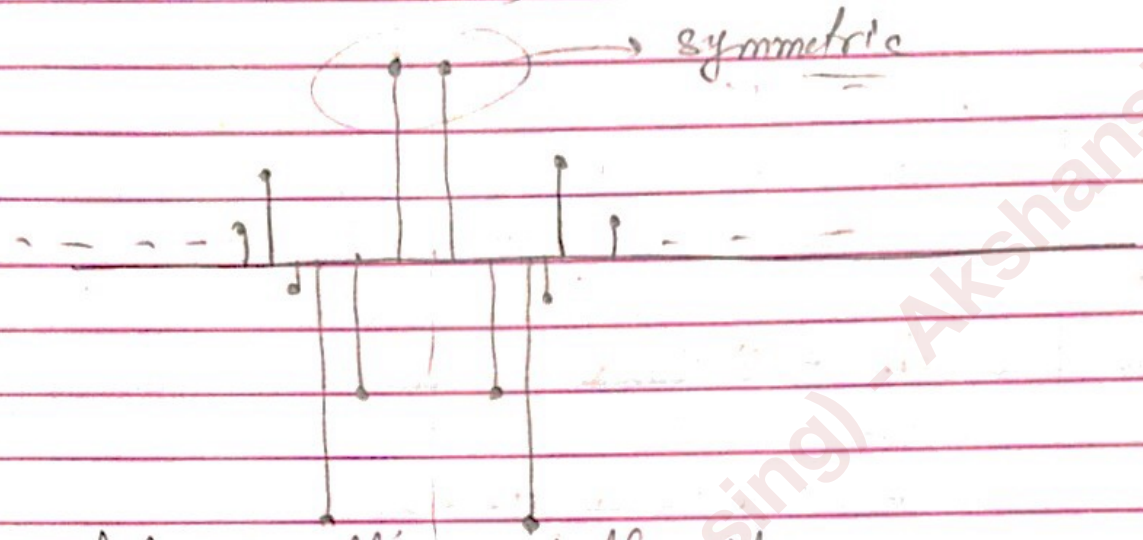
N = 58 ;
beta = 5.65 ;
hn = fir4(N-1, fc, kaiser(N, beta));
[H, f] = freqz(hn, 1, 512, Fs);
mag = 20 * log10(abs(H));
subplot(4, 2, 1) % Making all plots & parts
                  in same plot
plot(f, mag), grid minor; % frequency response
xlabel('Frequency (Hz)');
ylabel('Magnitude Response (dB)');

% Finding impulse response :-
subplot(4, 2, 2);
impz(hn, 1);
    
```

we get :-



Impulse response, got from command:-
 $N = 58$ (even)

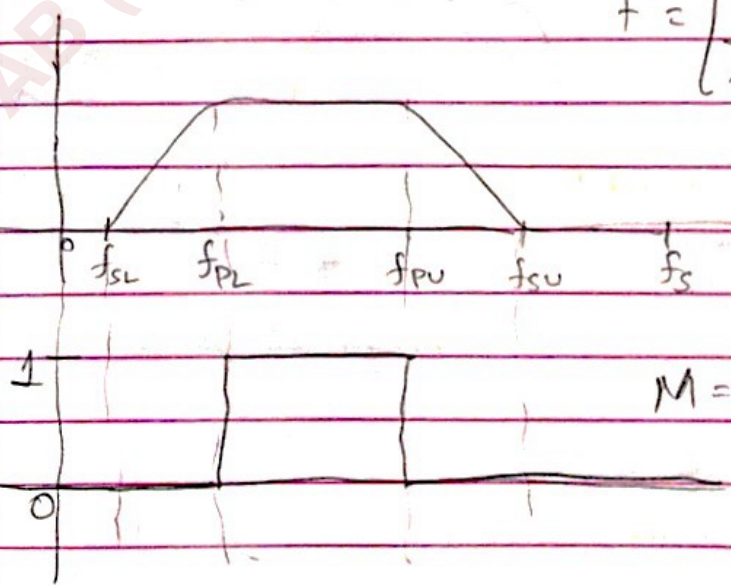


Total 29 coeff. on both sides

(3) Using optimal method:-

In this filter, we find an array of all normalised frequencies. let the array be F .
 Now, we make another array considering the case that its ideal. let the array be M .
 So :-

$$F = \left[\begin{array}{cccccc} 0 & f_{sl} & f_{pl} & f_{pu} & f_{su} & f_s \\ f_s & f_s & f_s & f_s & f_s & f_s \end{array} \right]$$



$$M = [0 \ 0 \ 1 \ 1 \ 0 \ 0]$$

Commands :

$$F = [5000, 8000, 12000, 15000]$$

$$M = [0, 1, 0]$$

from 5k to 8k

from 8k to 12k

from 12k to 15k

$$dp = 0.01;$$

$$ds = 0.001;$$

$$dev = [ds, dp, ds];$$

$$[N1, FO, MO, W] = \text{remezord}(F, M, dev, fs)$$

$$[H, f] = \text{freqz}(b, 1, 1024, fs);$$

for determining order

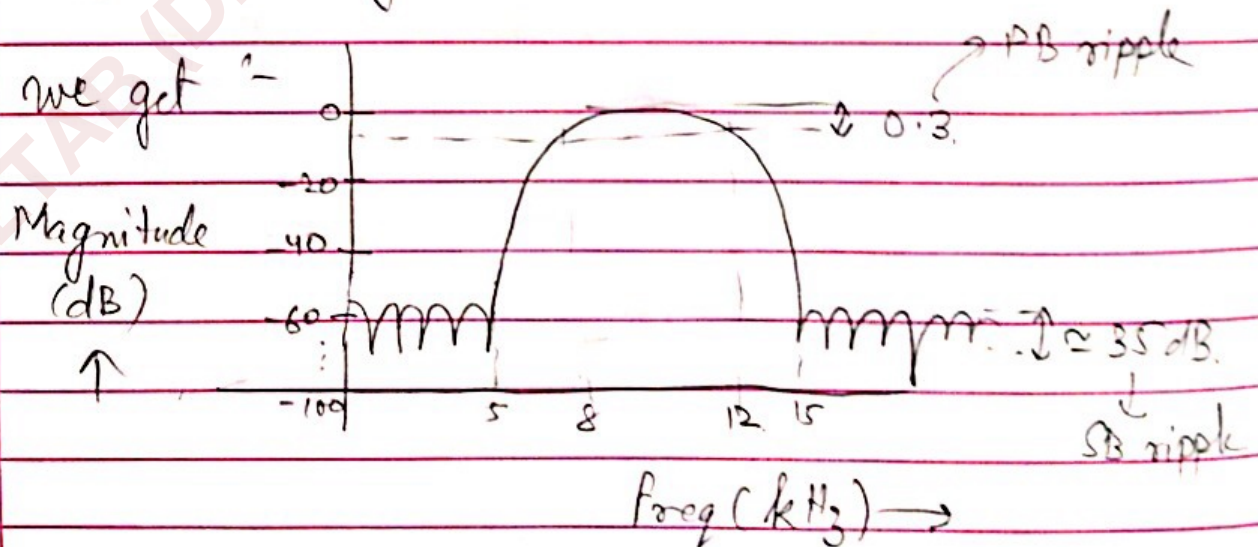
$$[b, delta] = \text{remez}(N1, FO, MO, W);$$

$$* \text{mag} = 20 * \log_{10}(\text{abs}(H));$$

plot(f, mag), grid, minor;

xlabel('Frequency (Hz)');

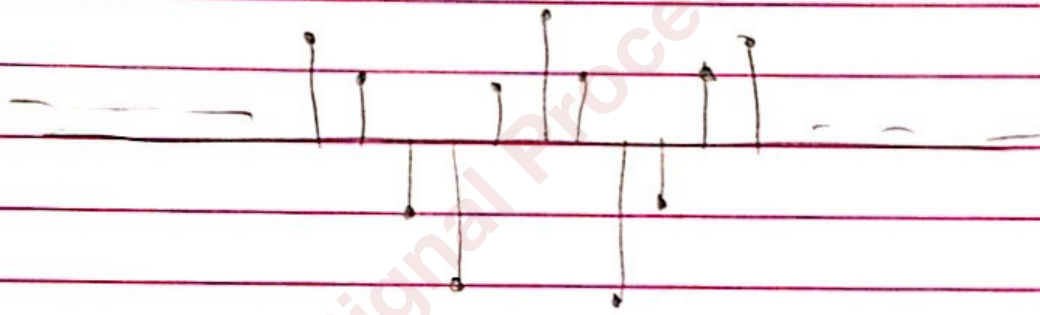
ylabel('Magnitude (dB)');



Impulse response

$\text{impz}(b, 1)$

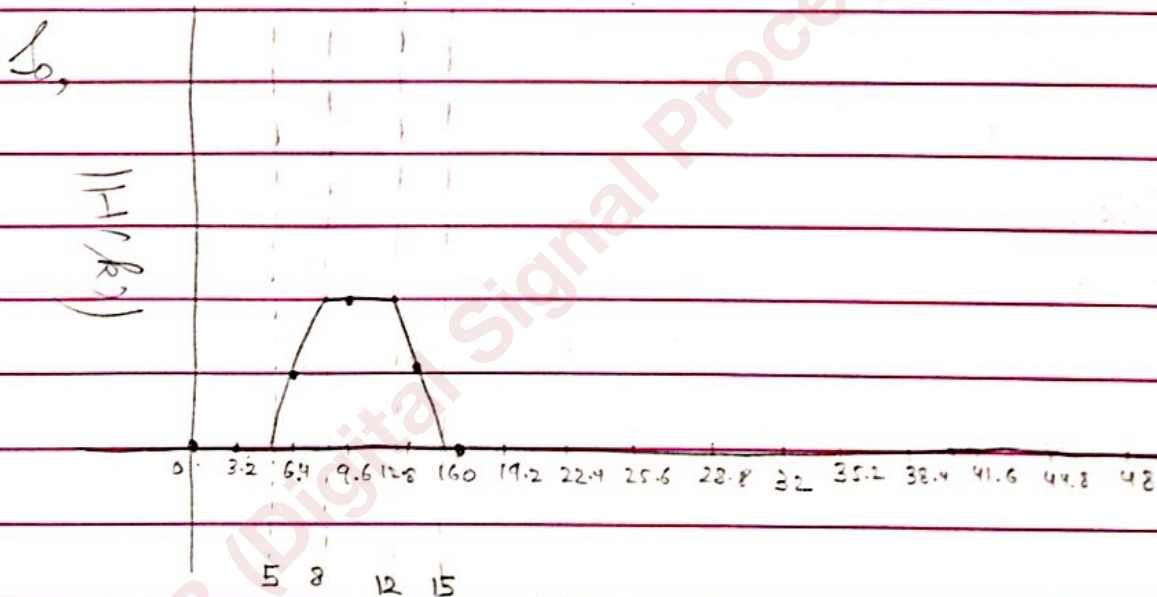
For $N = 40$, we get



(4) Using Frequency Sampling method :-

Assuming $N=15$ i.e., a 15 pt. FIR filter, we have

Now, with $f_s = 48 \text{ kHz}$, distance ^{freq. difference} b/w each samples = $\frac{48}{15} = 3.2 \text{ kHz}$.



Page No

So, we have

$$|H(k)| = \begin{cases} 0 & k=0, 1 \\ 0.41793 & k=2 \\ 1 & k=3 \\ 0.404058 & k=4 \\ 0 & k=5, 6, 7 \end{cases} \quad \text{(values taken from table 7.11)}$$

normalizing freq. points w.r.t. half of sampling freq. :-

$$0, \frac{1}{7}, \frac{2}{7}, \frac{3}{7}, \frac{4}{7}, \frac{5}{7}, \frac{6}{7}, 1 \quad \text{(taking half of 15 pts due to symmetry)}$$

$$F_s = 48000;$$

$$N = 15; \quad \therefore \text{but we are using } N = 15$$

$$fd = [0 \quad 1/7 \quad 2/7 \quad 3/7 \quad 4/7 \quad 5/7 \quad 6/7 \quad 1];$$

$$hd = [0 \quad 0 \quad 0.41793 \quad 1 \quad 0.404058 \quad 0 \quad 0 \quad 0];$$

$$h_n = \text{fir2}(N-1, fd, hd);$$

$$[H, f] = \text{freqz}(h_n, 1, 512, F_s)$$

plot(f, abs(H), grid on

xlabel('Frequency (Hz)');

ylabel('Magnitude');

we get

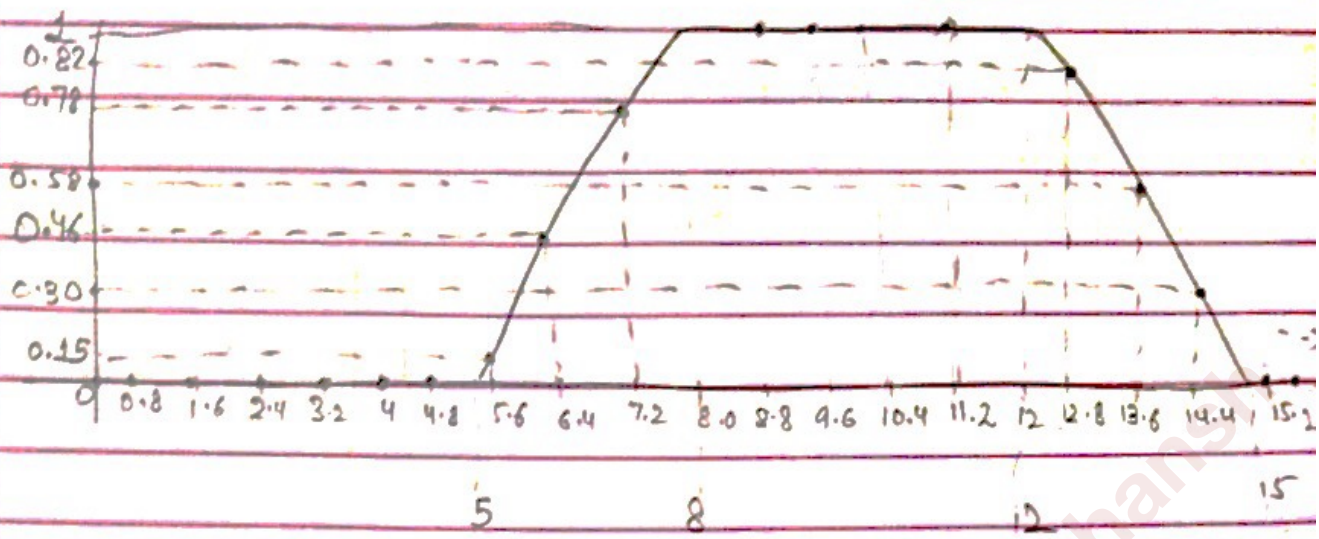


Now,

* Actual work : Taking $N = 58$.

So, 58 point FIR filter. So, we take $\frac{58}{2} = 29$ samples.

Now, with $f_s = 48 \text{ kHz}$, distance b/w each sample = $\frac{48}{58} \approx 0.8 \text{ kHz}$



Normalised freq points are

$$\frac{0}{29}, \frac{1}{29}, \frac{2}{29}, \frac{3}{29}, \dots, \frac{27}{29}, \frac{28}{29}, 1$$

OR $f_d = [0 \quad 1/29 \quad 2/29 \quad 3/29 \quad \dots \quad 28/29 \quad 1]$

$f_d = \text{zeros}(1, 29)$

for $i = 0:28$

$f_d(i+1) = f_d(i+1) + (i * 0.8)$

end ; $f_d = f_d ./ 22.4 ;$

$F_s = 48000 ;$ for normalising \rightarrow only needed for "for loop"

Now,

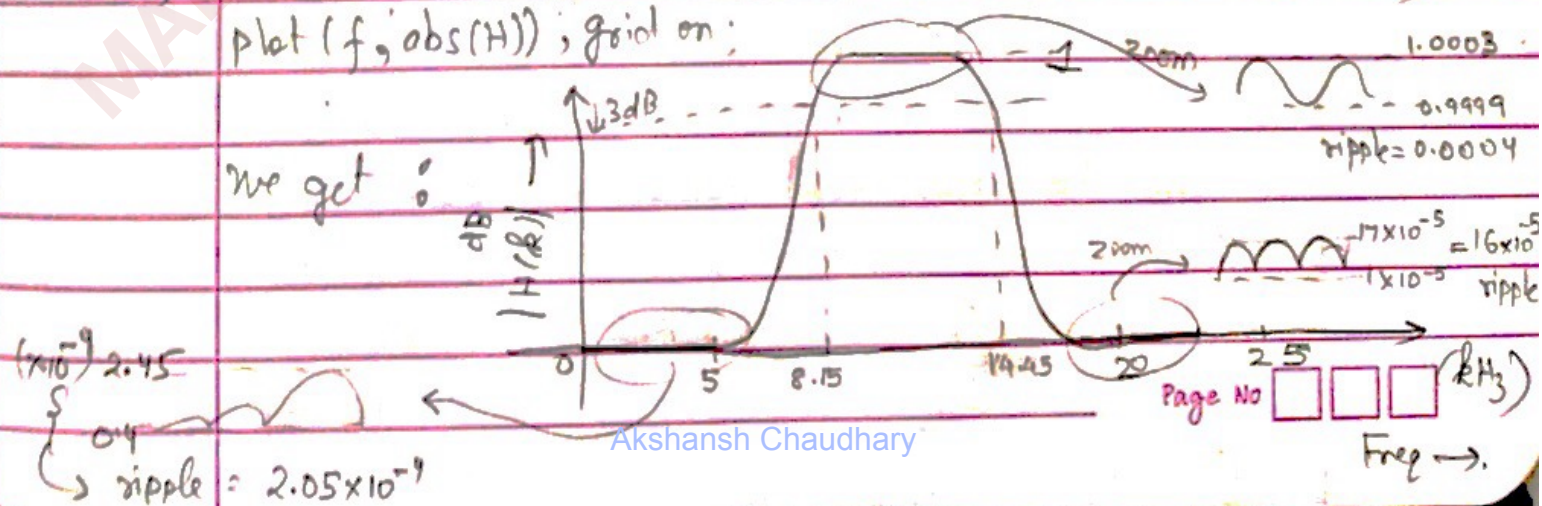
$$H_d = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & (0.15) & (0.46) & (0.78) \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & (0.82) & (0.58) & (0.30) \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

The values in () lie in the Transⁿ band

Now, $h_n = \text{fir2}(N-1, f_d, H_d) ; [H, f] = \text{freqz}(h_n, 1, 512, F_s) ;$

Plot $(f, \text{abs}(H)) ; \text{grid on} ;$

we get :

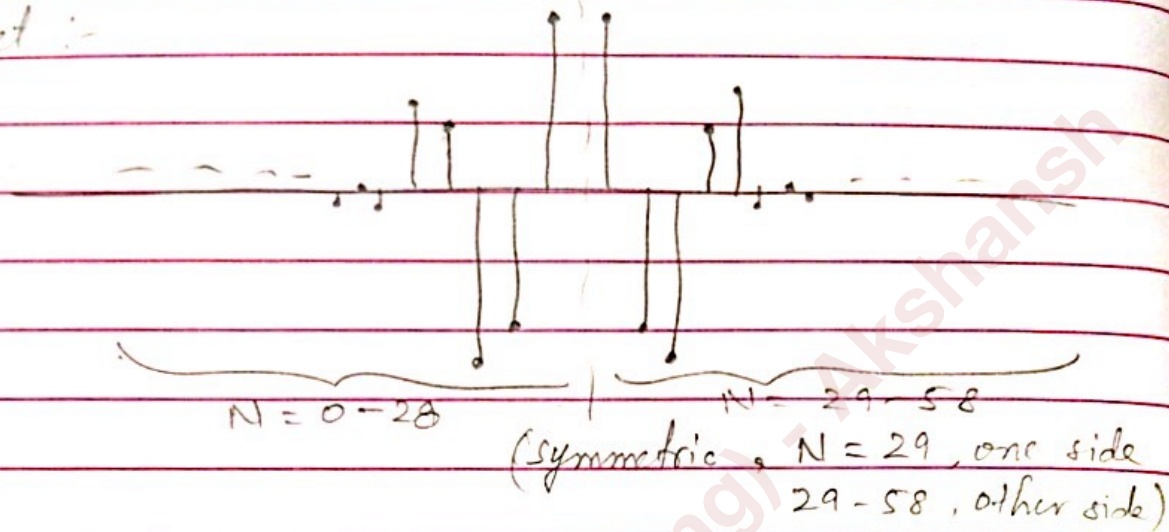


Finding Impulse response

Cmd :-

```
impz(hn);
```

we get :-



Observations :

- ✓ Frequency sampling method is giving less lower ripples in PB as well as SB.
- ✓ The values for cut off freq. of PB & SB are nearly same, as given in the question
- ✓ Value of $N=58$ was taken as the no. of samples corresponding to the value that was got in Kaiser window.
- ✓ The attenuation is 100% i.e., corresponding to the values taken in "Hd". \Rightarrow Frequency sampling method gives a more ideal curve., because, we get :-

magnitude = 1	:	for PB	}	ideal
0	:	for SB		
- ✓ The PB cut off freq. seen 3dB down, we see

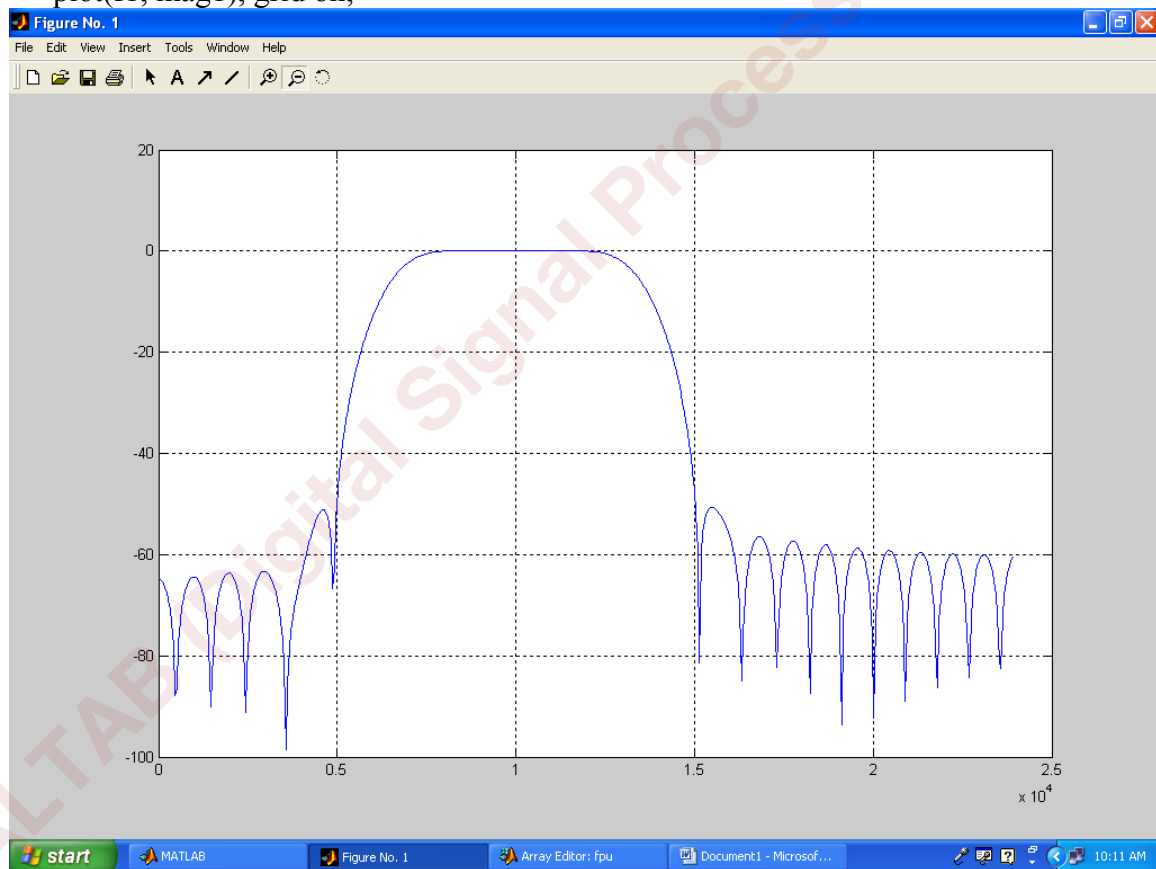
PB \rightarrow $f_{p2} = 8.15 \text{ kHz}$	\rightarrow given 8
$f_{p0} = 14.45 \text{ kHz}$	\rightarrow given 12

Assignment 6

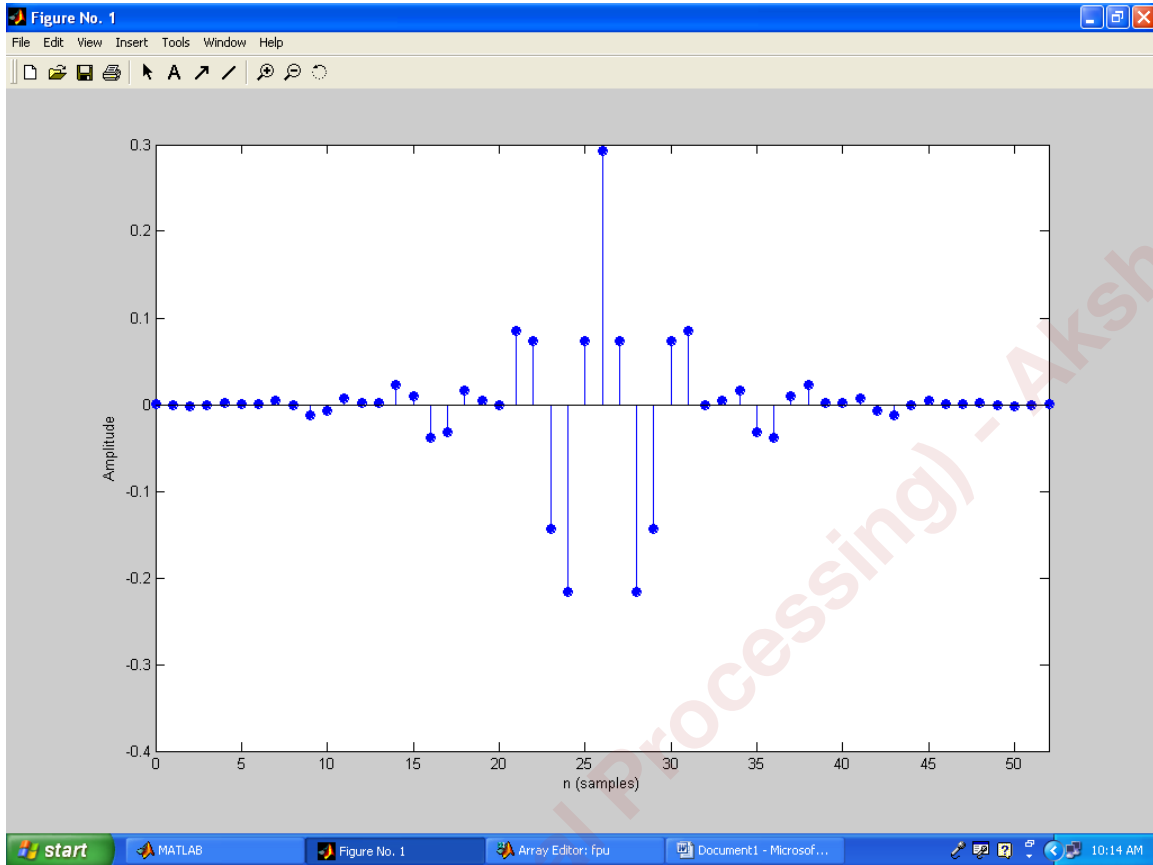
Q. 7.32

1.

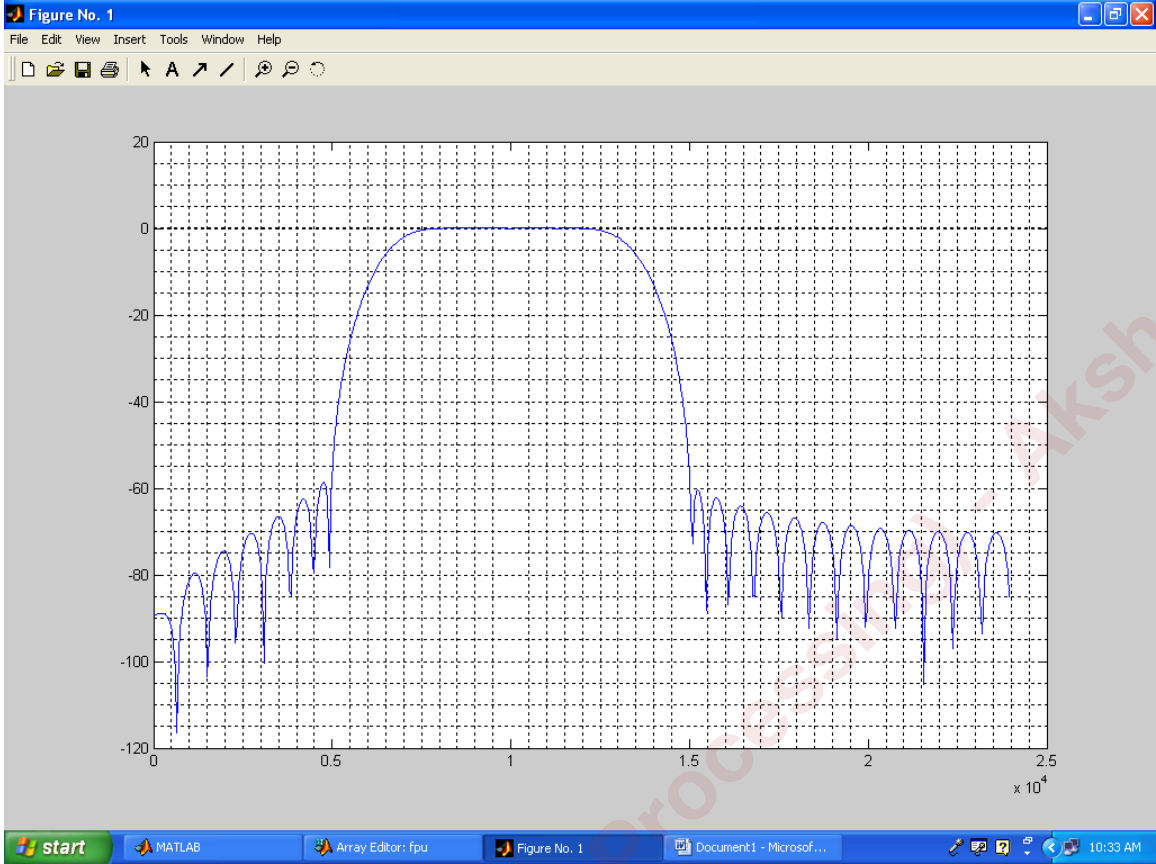
```
fpl=13/48;  
>> fpu=27/48;  
>> fsl=12/48;  
>> fsu=15/48;  
>> fc=[fpl fpu];  
>> N1=53;  
>> hd=fir1(N1-1, fc, boxcar(N1));  
>> wn=hamming(N1);  
>> hn1=fir1(N1-1, fc, wn);  
>> fs=48000;  
>> [H1,f1]=freqz(hn1, 1, 512, fs);  
>> mag1=20*log10(abs(H1));  
>> plot(f1, mag1), grid on;
```



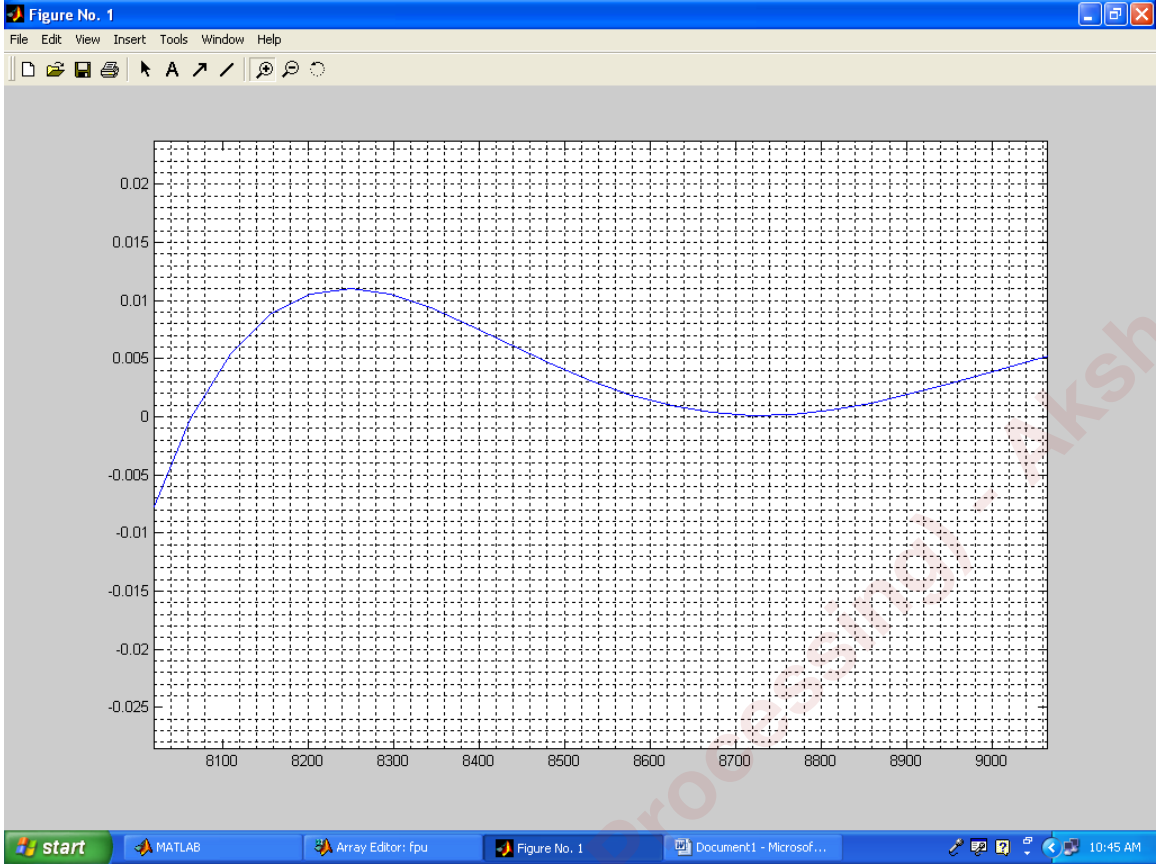
```
>> impz(hn1,1)
>>
```

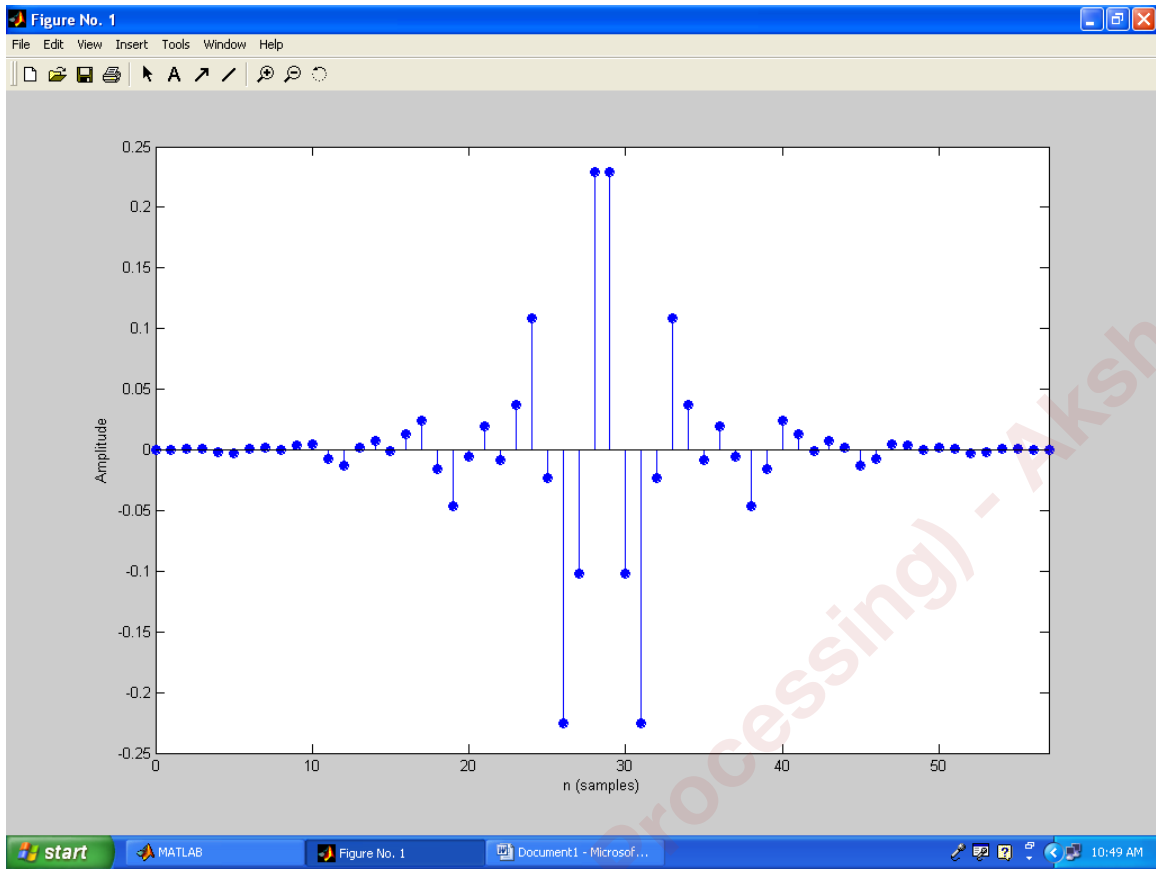


```
2.
N2=58;
>> beta=5.65;
>> hn2=fir1(N2-1, fc, kaiser(N2, beta));
>> [H2, f2]=freqz(hn2, 1, 512, fs);
>> mag2=20*log10(abs(H2));
>> plot(f2, mag2, 'red'), grid minor;
```



MALTAB (Digital Signal Processing) Akshansh



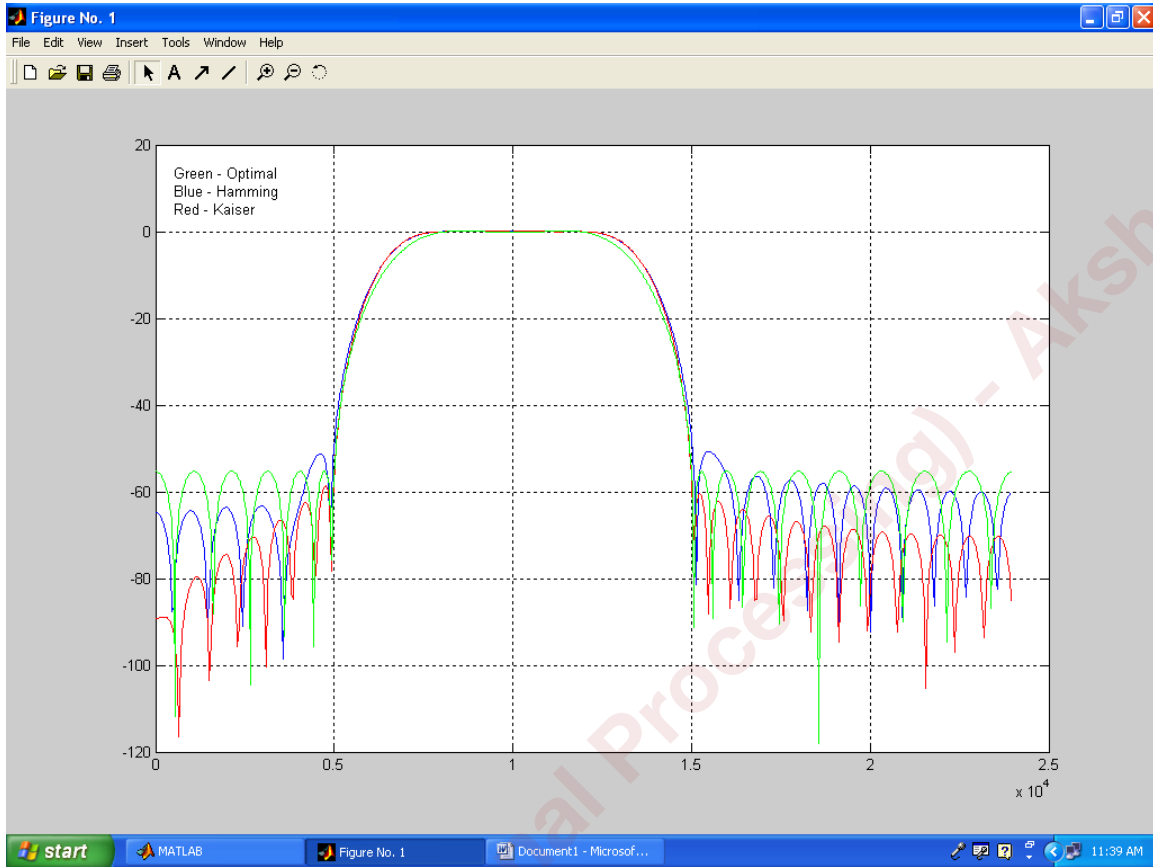


```

3.
> F=[5000, 8000, 12000, 15000];
>> M=[0 1 0];
>> dp=0.01;
>> ds=0.001;
>> dev=[ds dp ds];
>> [N3, F0, M0, W]=remezord(F, M, dev, fs);
>> [b delta]=remez(N3, F0, M0, W);
>> [H3, f3]=freqz(b, 1, 1024, fs);
>> mag3=20*log10(abs(H3));
>> plot(f3, mag3, 'green'), grid minor;

```

Plotting all freq. responce on same graph



MATLAB Assignment 7

Digital Signal Processing

9/12/13 Assignment - 7 (Lab 8)
Multirate Digital Signal Processing

$$F_s = 5000;$$

$$A = 2;$$

$$B = 1;$$

$$f_1 = 50;$$

$$f_2 = 100;$$

$$t = 0 : 1/F_s \cdot L;$$

$$x = A \cos(2\pi f_1 t) + B \cos(2\pi f_2 t);$$

% Taking 1000 samples.

stem(x(1:1000))

(a) xlabel('Discrete time, nT');

ylabel('Input signal level');

% Now, decimating by a factor of 10 so, 100 samples

y = decimate(x, 10);

stem(y(1:100));

(b) xlabel('Discrete time, nT/10');

ylabel('Decimated output signal level');

% Now, interpolating signal by factor of 4

y1 = interp(y, 4);

stem(y1(1:400));

(c) xlabel('Discrete time, 4*nT');

ylabel('Decimated output signal level');

Using function



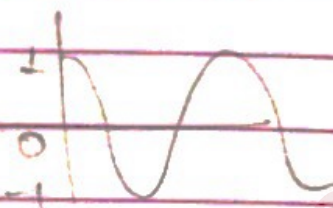
(S1) File > New > file
(Tab opens)

function name (~)

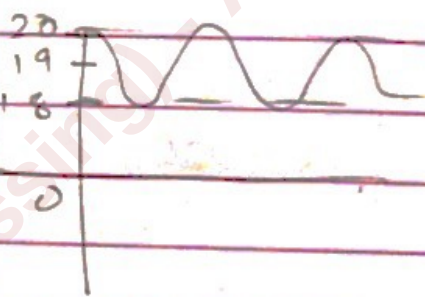
}

end

$$y = \sin x$$



$$y = 20 + \sin x$$

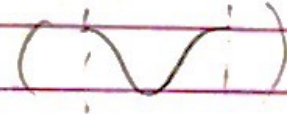


(S2) Save it.

Calling function

In cmd. window :

name ←

How to see? → See in one cycle ()

Original



Decimated



Interpolated.



Assignment 7

Decimation and Interpolation

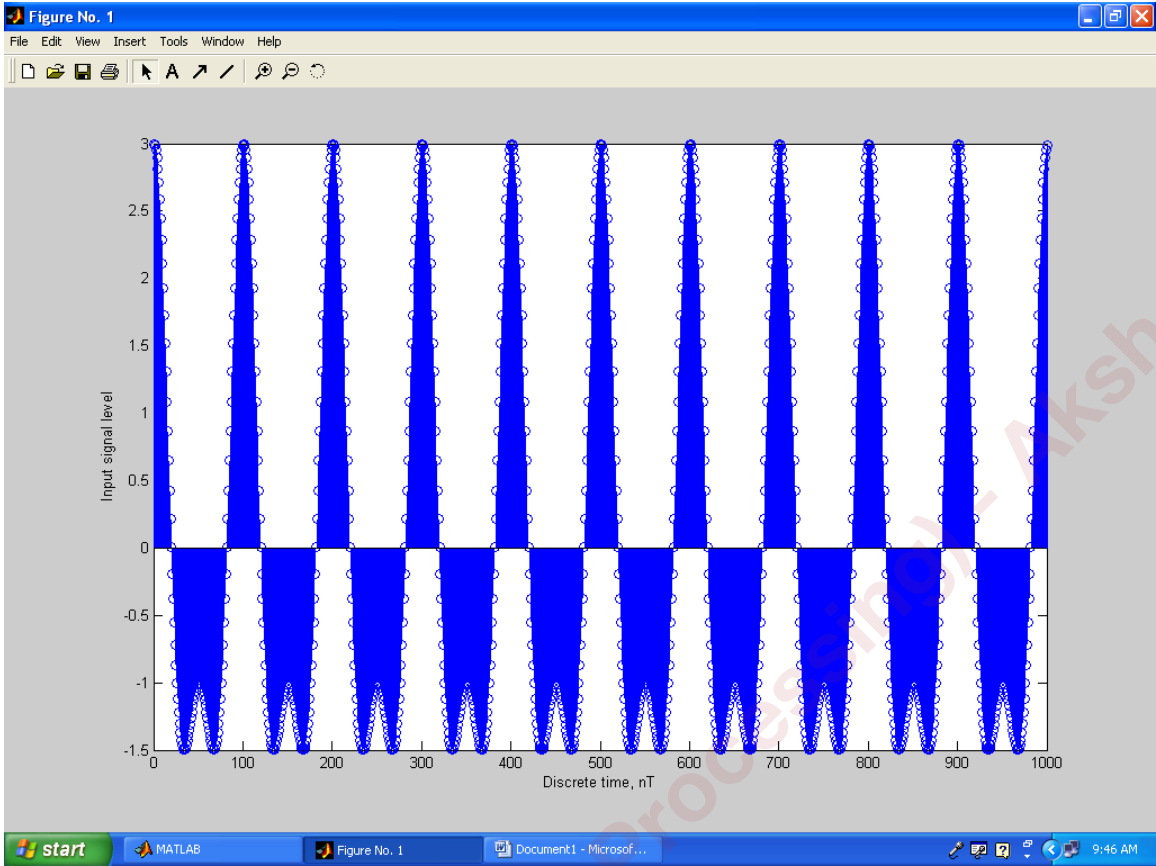
9.12.13

Commands –

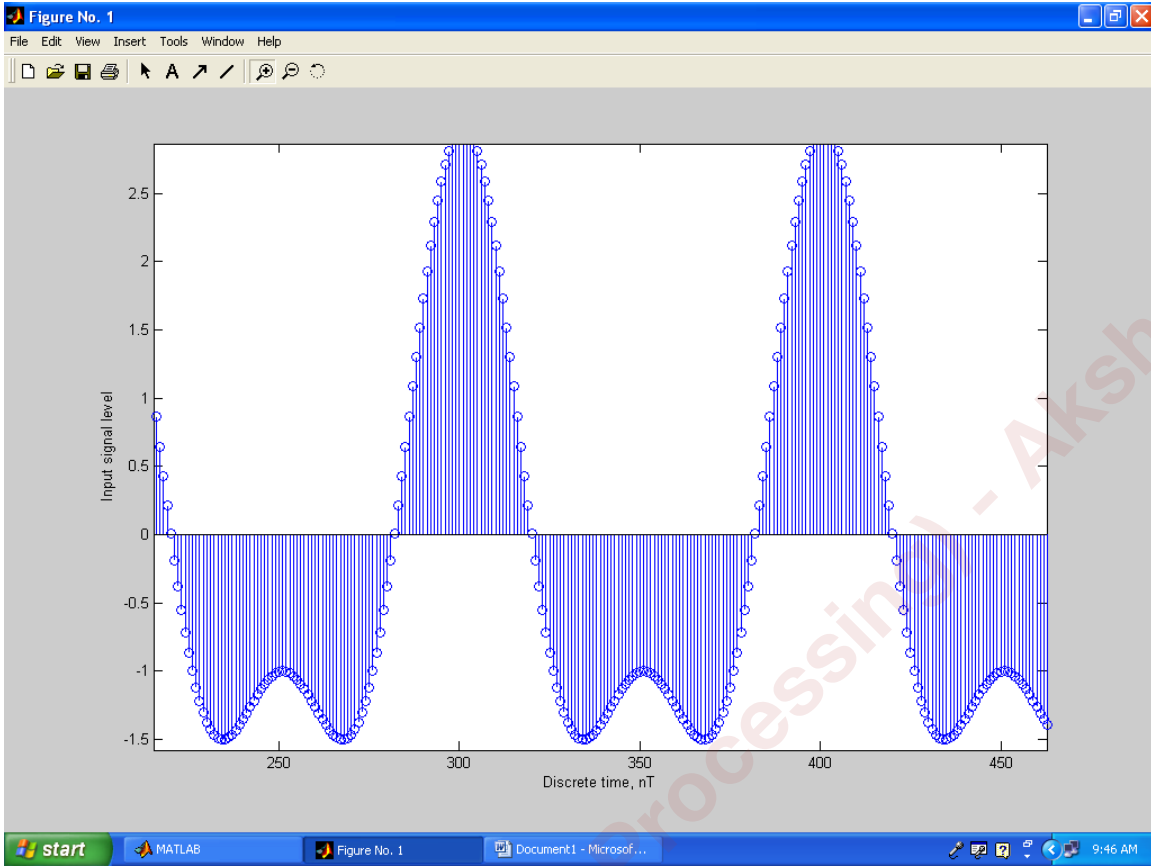
```
>> Fs=5000;
>> A=2;
>> B=1;
>> f1=50;
>> f2=100;
>> t=0:1/Fs:1;
>> x=A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:1000))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>
>>
>> %Now, decimating for part b.
>> y=decimate(x,10);
>> subplot(3,1,2)
>> stem(y(1:100))
>> xlabel('Discrete time, nT/10')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
>>
```

Graphs -

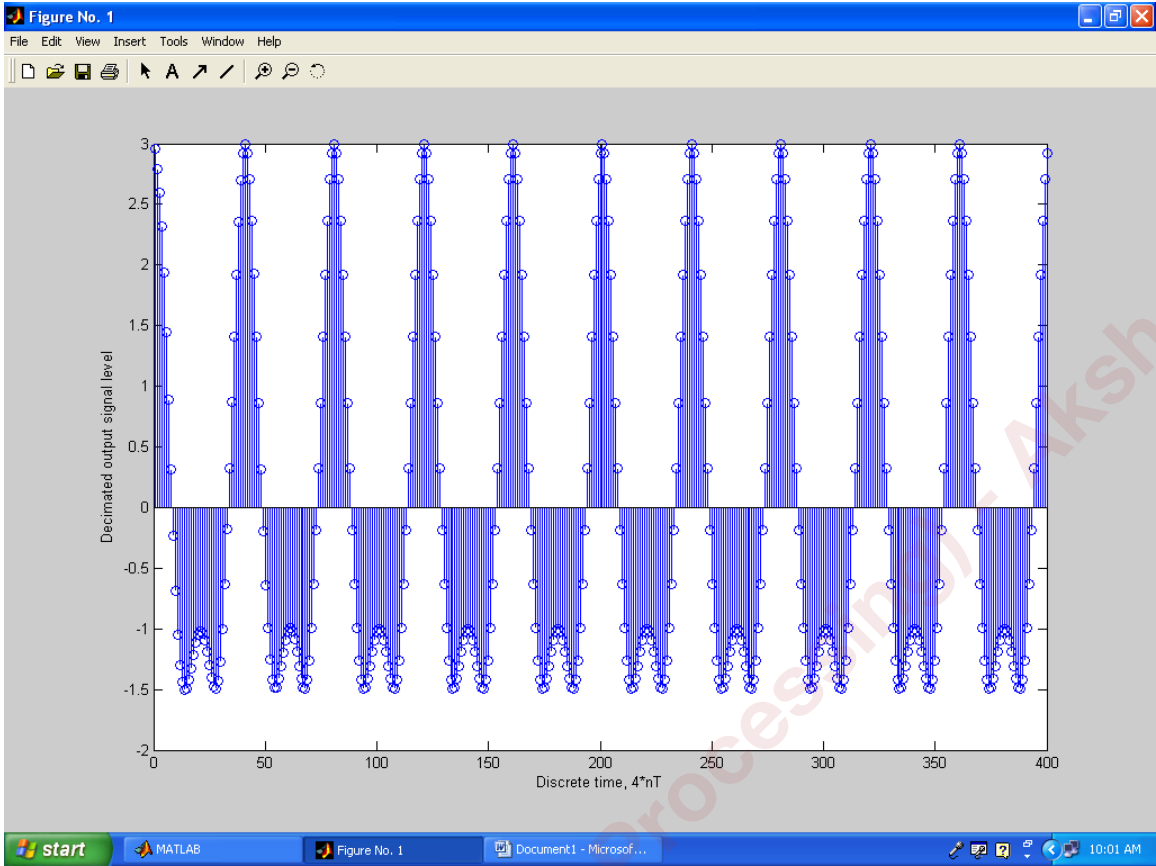
Part a – 1000 samples



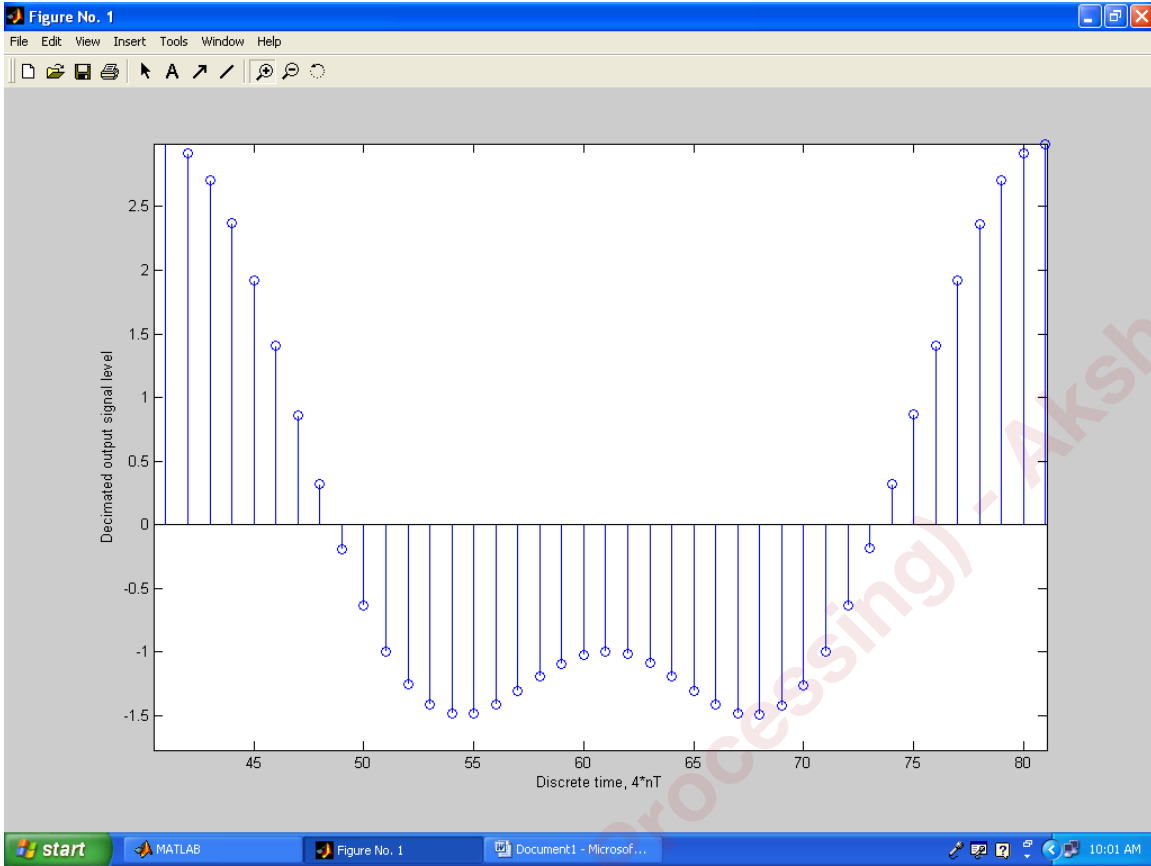
Zooming –



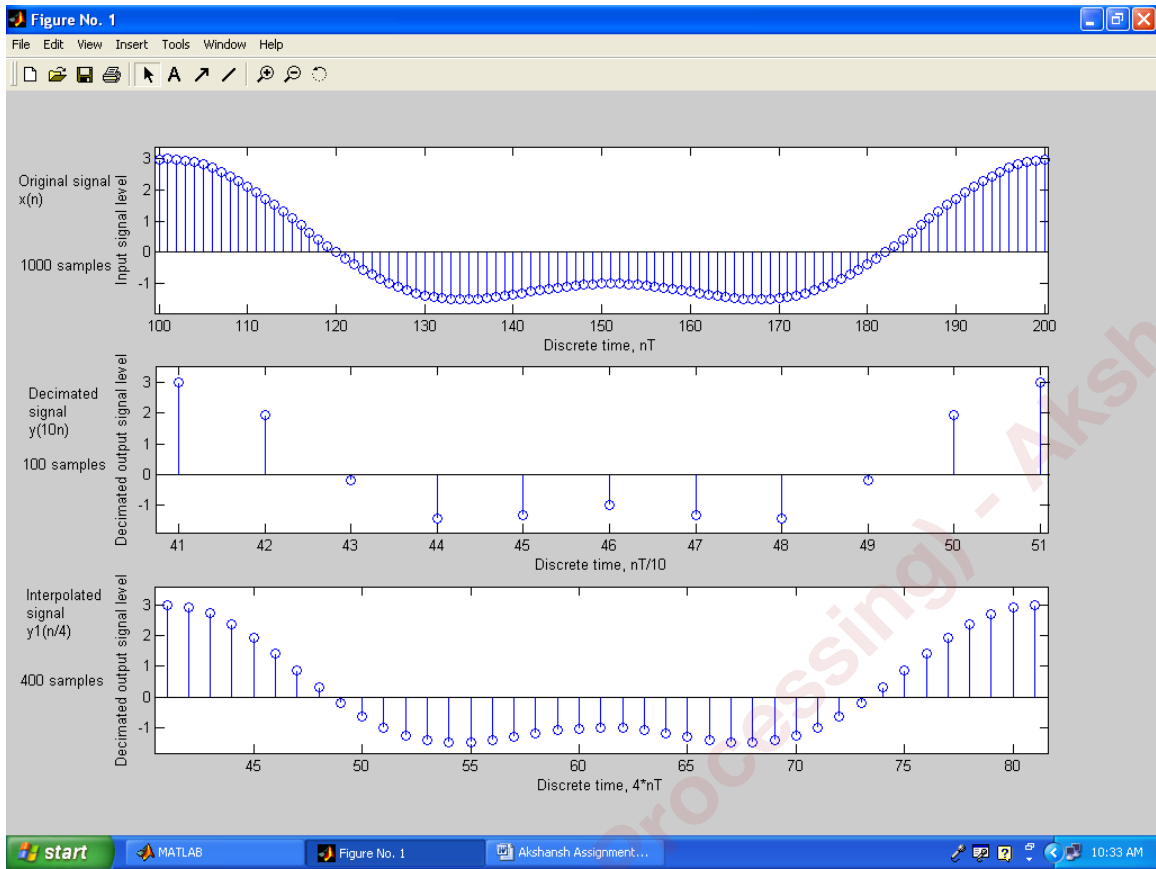
Part b – Decimation (1000/10.e. 100 samples)



Zooming –



Combined graph-
Seeing the change in the number of samples in one cycle.



OBSERVATIONS:

Change 1

```

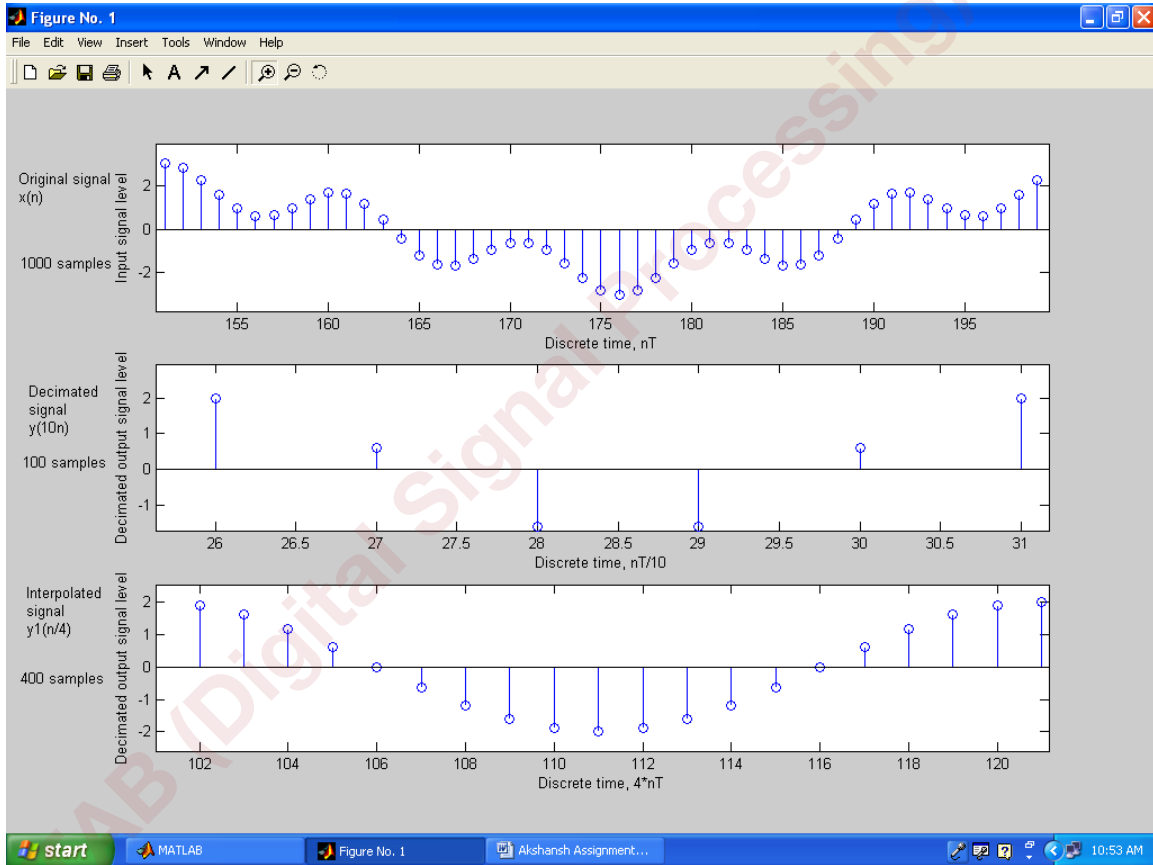
>> Fs=5000;
>> A=2;
>> B=1;
>> f1=100
>> f2=500;
>> t=0:1/Fs:1;
>> x=A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:1000))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>

```

```

>>
>> %Now, decimating for part b.
>> y=decimate(x,10);
>> subplot(3,1,2)
>> stem(y(1:100))
>> xlabel('Discrete time, nT/10')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
>>

```



Change 2

```

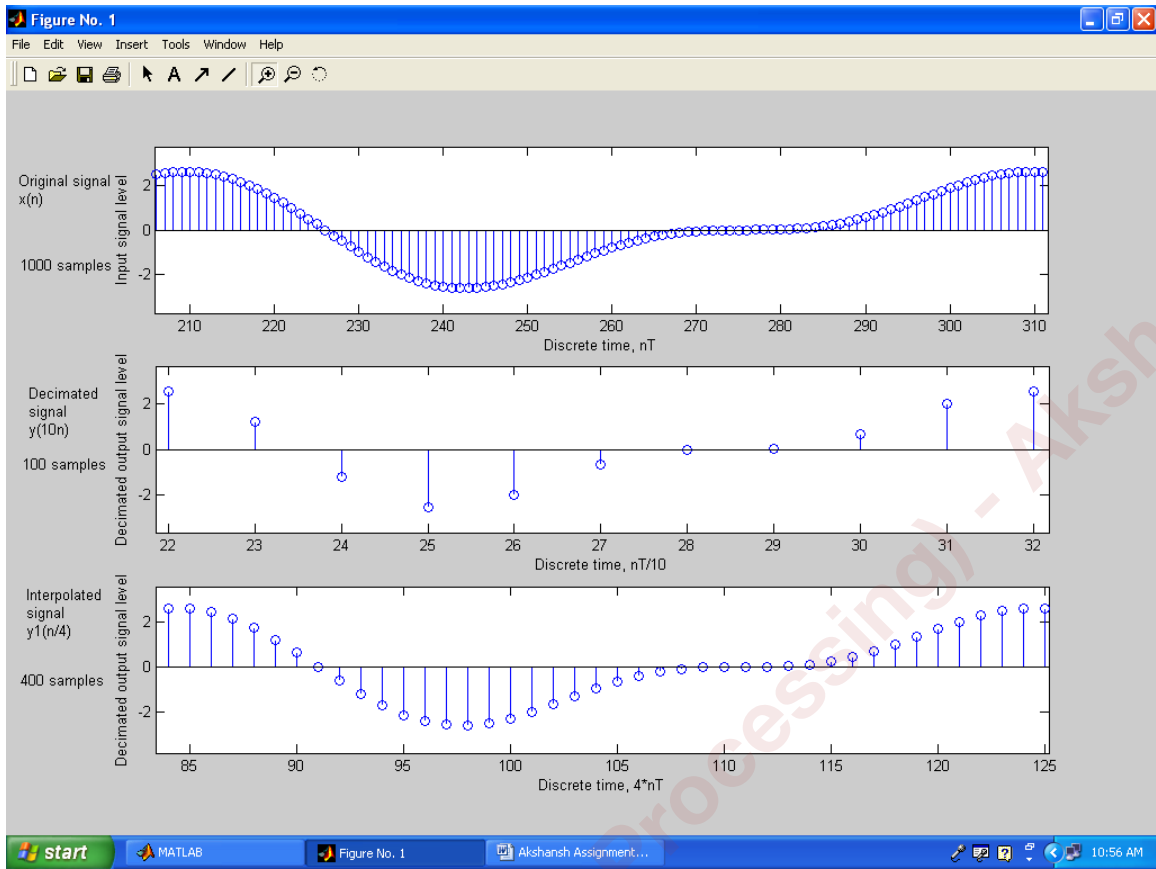
Fs=5000;
>> A=2;

```

```
>> B=1;
>> f1=50;
>> f2=100;
>> t=0:1/Fs:1;

>> x=A*cos(2*pi*f1*t)+B*sin(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:1000))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>
>>
>> %Now, decimating for part b.
>> y=decimate(x,10);
>> subplot(3,1,2)
>> stem(y(1:100))
>> xlabel('Discrete time, nT/10')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
```

MALTBAB (Digital Signal Processing) - Akshansh



Change 3

$F_s=5000$;

>> A=**50**;

>> B=**-10**;

>> f1=50;

>> f2=100;

>> t=0:1/Fs:1;

>> x=A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);

>> subplot(3,1,1)

>> stem(x(1:1000))

>> xlabel('Discrete time, nT')

>> ylabel('Input signal level')

>>

>>

>> %Now, decimating for part b.

>> y=decimate(x,10);

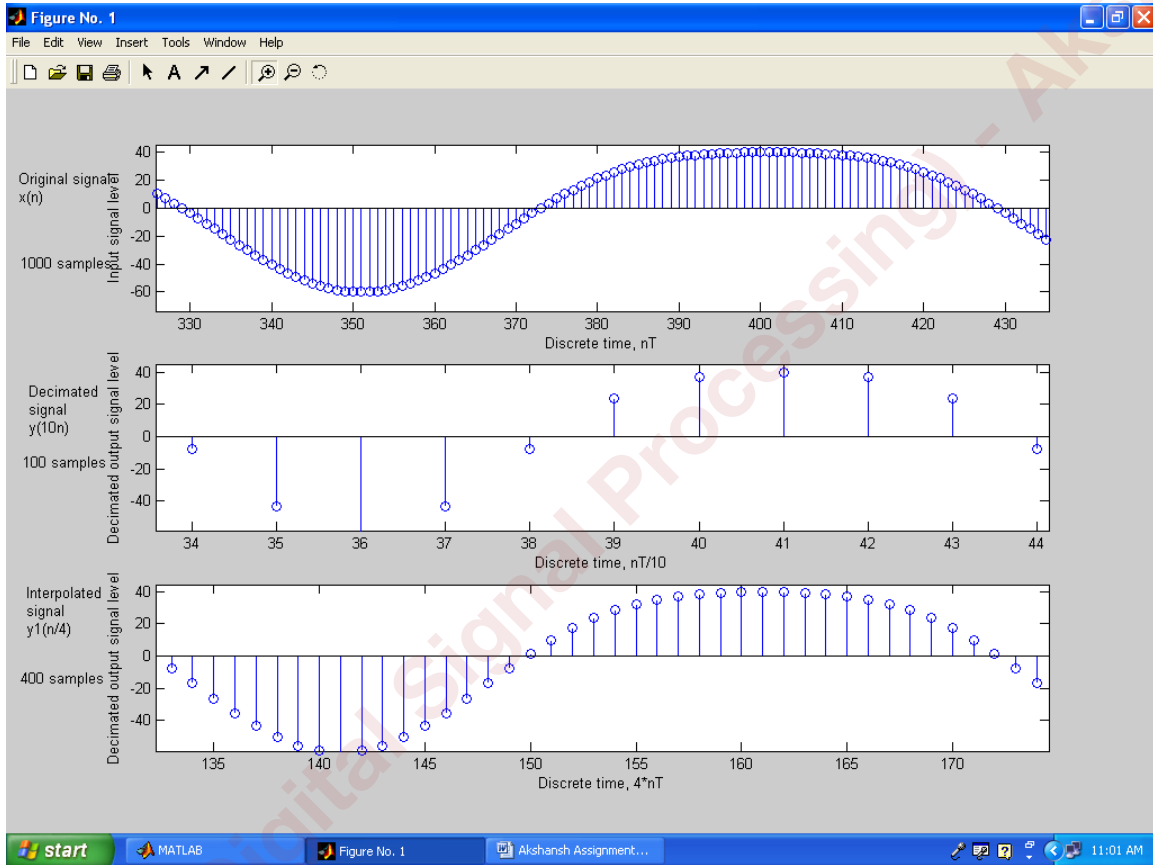
>> subplot(3,1,2)

>> stem(y(1:100))


```

>> xlabel('Discrete time, nT/10')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
>>

```



Change 4

Idea – No. of samples taken should always be less than the sampling frequency that we take.

```

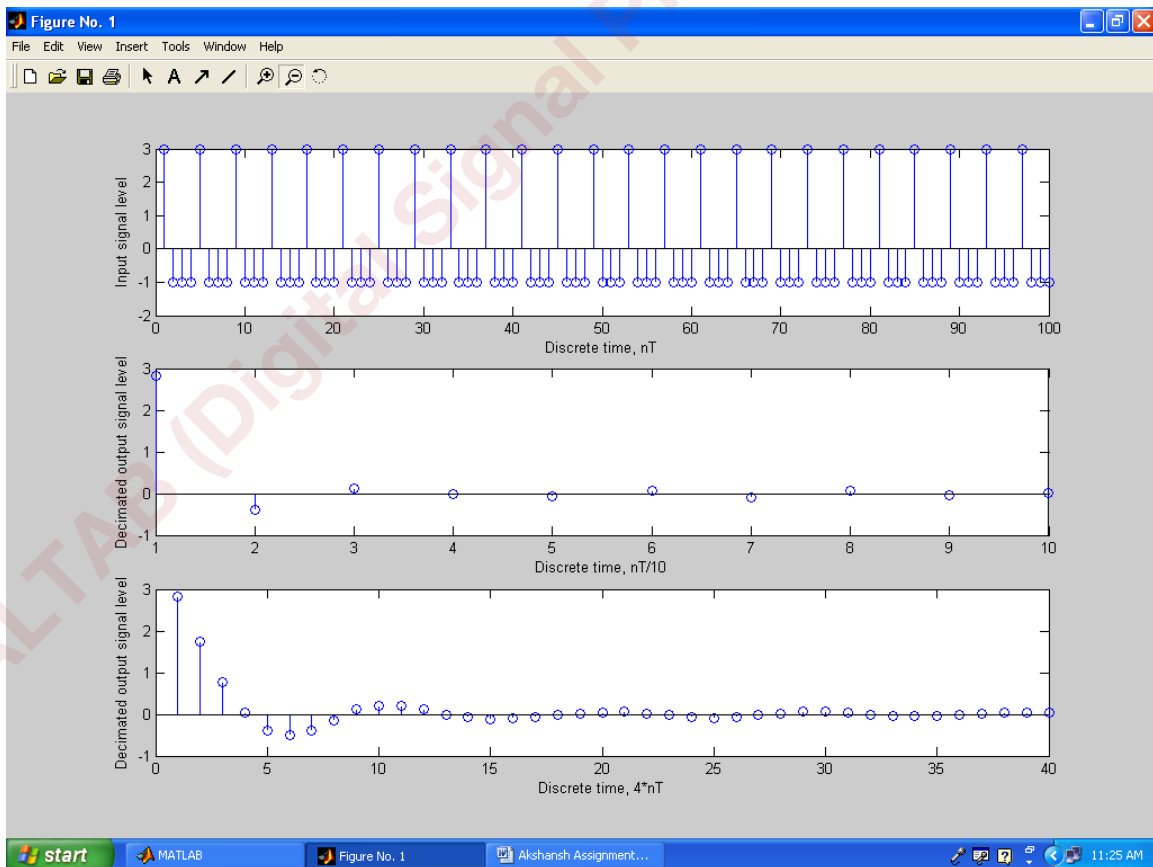
Fs=200;
>> A=2;
>> B=1;
>> f1=50;
>> f2=100;
>> t=0:1/Fs:1;

```

```

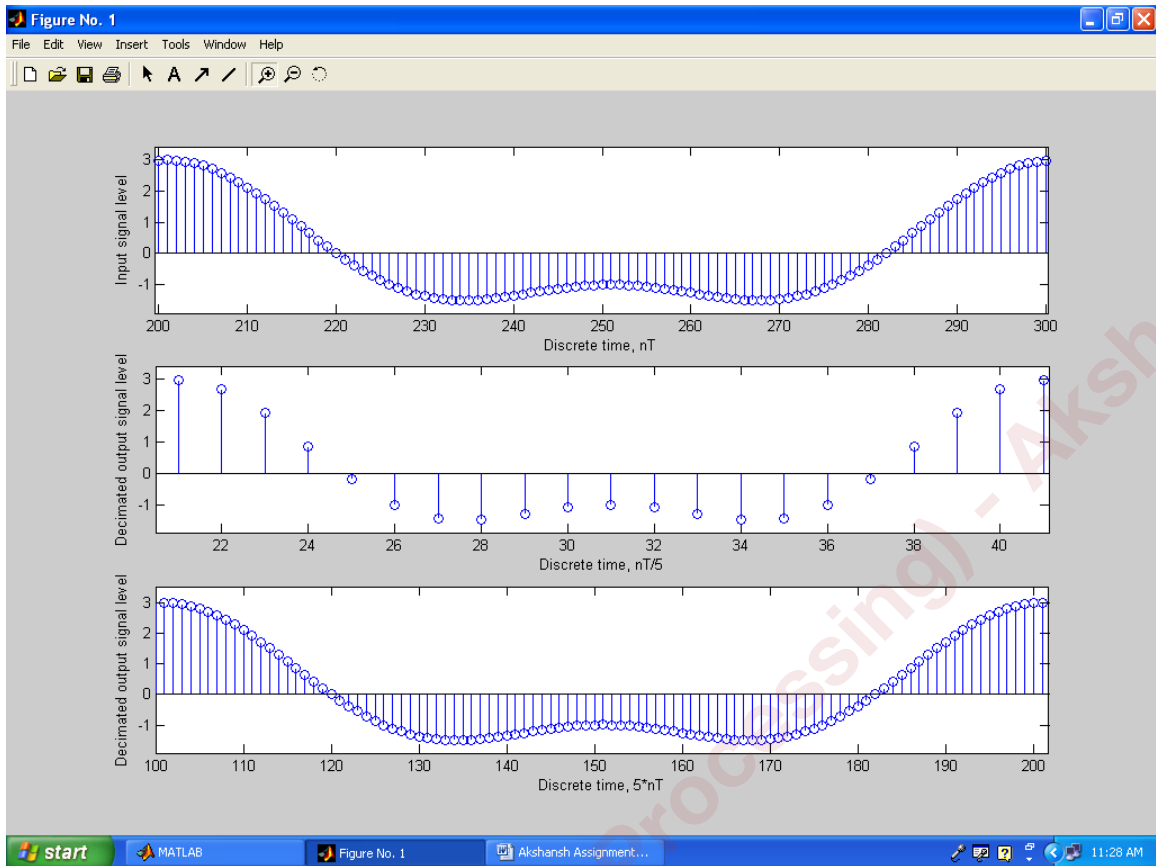
>> x=A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:100))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>
>>
>> %Now, decimating for part b.
>> y=decimate(x,10);
>> subplot(3,1,2)
>> stem(y(1:10))
>> xlabel('Discrete time, nT/10')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:40))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
>>

```



Change 5

```
>> Fs=5000;
>> A=2;
>> B=1;
>> f1=50;
>> f2=100;
>> t=0:1/Fs:1;
>> x=A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:1000))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>
>>
>> %Now, decimating for part b.
>> y=decimate(x,5);
>> subplot(3,1,2)
>> stem(y(1:100))
>> xlabel('Discrete time, nT/5')
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,5);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 5*nT')
>> ylabel('Decimated output signal level')
```



Change 6

```

Fs=5000;
>> A=2;
>> B=1;
>> f1=50;
>> f2=100;
>> t=0:1/Fs:1;

>> x=5+A*cos(2*pi*f1*t)+B*cos(2*pi*f2*t);
>> subplot(3,1,1)
>> stem(x(1:1000))
>> xlabel('Discrete time, nT')
>> ylabel('Input signal level')
>>
>>
>> %Now, decimating for part b.
>> y=decimate(x,10);
>> subplot(3,1,2)
>> stem(y(1:100))
>> xlabel('Discrete time, nT/10')

```

```
>> ylabel('Decimated output signal level')
>>
>> %Now, interpolating for part c.
>> y1=interp(y,4);
>> subplot(3,1,3)
>> stem(y1(1:400))
>> xlabel('Discrete time, 4*nT')
>> ylabel('Decimated output signal level')
```

